

Constraining dust grain porosity via debris disk observations

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Introduction

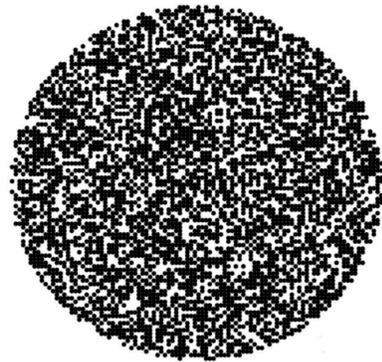
In the analysis of debris disk observations dust grains are often considered as homogeneous, compact spheres, although it is expected that dust particles possess complex, irregular shapes and inclusions of various materials and voids. In addition, recent studies based on high-contrast, high-resolution imaging polarimetry show that the measured data cannot be reproduced by compact, spherical dust grains. Usually, only very weak constraints on the dust grain properties can be derived directly. Our goals:

- Calculation of the blowout size of porous grains
- Deriving an approximation function for the blowout size
- Investigation of the effect of porosity on disk modelling results

Porous dust: Model

- Silicate dust grains with spherical shape and voids
- Porosity \mathcal{P} defines volume fraction of vacuum
- Parameter space: $\mathcal{P} = 0.0 \dots 0.9$ ($\Delta = 0.1$)
- Effective medium theory with Bruggeman mixing rule

$$(1 - \mathcal{P}) \frac{\epsilon_{\text{astrosil}} - \epsilon_{\text{eff}}}{\epsilon_{\text{astrosil}} + 2\epsilon_{\text{eff}}} + \mathcal{P} \frac{\epsilon_{\text{vacuum}} - \epsilon_{\text{eff}}}{\epsilon_{\text{vacuum}} + 2\epsilon_{\text{eff}}} = 0$$



Cut through dust grain with $\mathcal{P} = 0.4$; from Kirchsclager and Wolf (2013)

- Optical cross sections and asymmetry factor g calculated with MIE X (Wolf and Voshchinnikov, 2004)

Blowout size

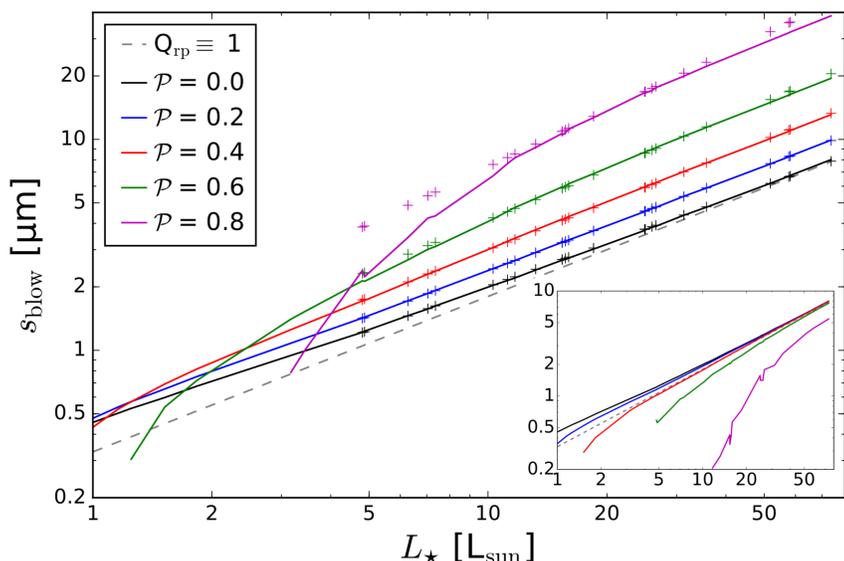
- Radiation pressure F_{rp} reduces gravitational attraction F_{grav}
- If $\frac{F_{\text{rp}}}{F_{\text{grav}}} = \beta \geq 0.5$: particles are removed by radiation pressure
- Blowout size s_{blow} : Grain radius for which $\beta = 0.5$

Analytical approximation function

$$\frac{s_{\text{blow}}}{1 \mu\text{m}} = \left(\frac{3.5 \text{ g cm}^{-3}}{\rho} \right) a_1 (1 - \mathcal{P})^{b_1} \cdot \left(\frac{L_{\star}}{L_{\odot}} \right)^{a_2 (1 - \mathcal{P})^{b_2}}$$

with

$$\begin{aligned} a_1 &= 0.414 \pm 0.004 \\ b_1 &= -0.508 \pm 0.025 \\ a_2 &= 0.685 \pm 0.002 \\ b_2 &= -0.168 \pm 0.008 \end{aligned}$$



Blowout size s_{blow} as a function of stellar luminosity for different porosities \mathcal{P} . The crosses show results of the analytical approximation function.

Porosity influences modelling results

Procedure

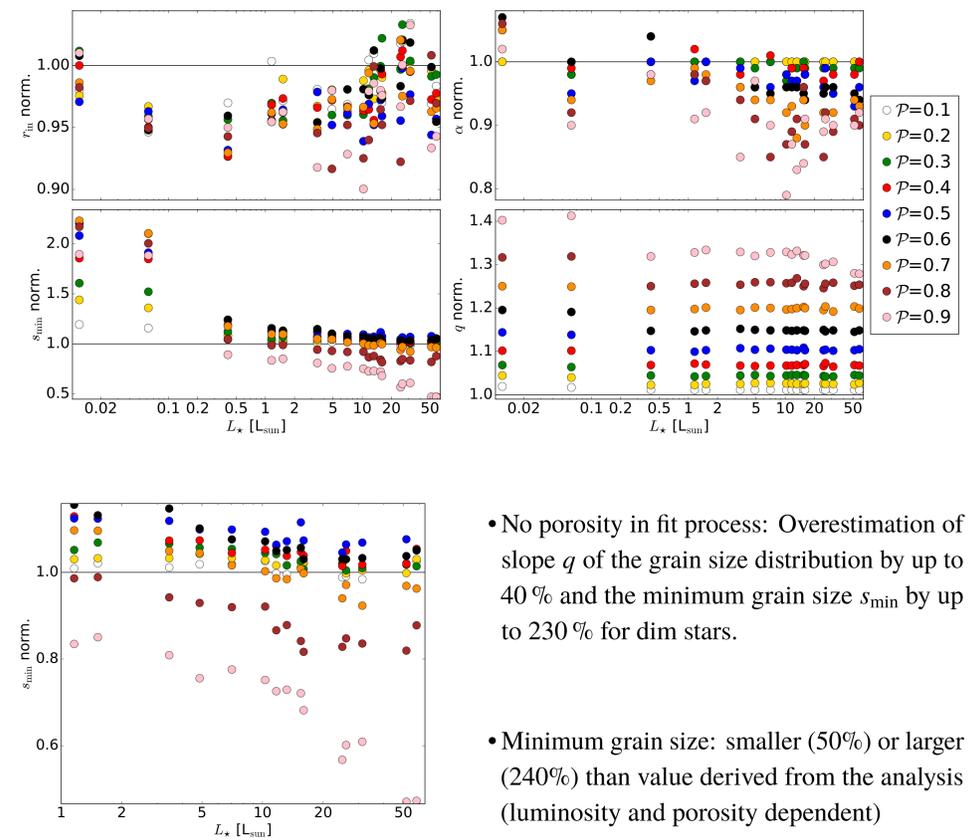
1. Calculation of the re-emission SED and images of an analytical dust distribution for different porosities \mathcal{P} ,
2. Convolution of the images with a circular Gaussian to mimic a real observation; Extraction of radial profiles; Superposition of artificial uncertainties (noise),
3. Fitting of the SED and profiles with the debris disk fitting software SAnD (Ertel et al., 2012) assuming compact dust grains, i.e. $\mathcal{P} \equiv 0.0$,
4. Comparison of the fit results of the different porosities with the initial, i.e. correct values.

Density and size distribution

- $n(s) \propto s^{-q}$, where $n \cdot ds$ is the number of particles in radius interval $[s, s + ds]$
- $r^{-\alpha}$, geometrically thin disk

Disk parameter	Sim. observation	FITTING		
		Min.	Max.	n
$M_{\text{dust}} [M_{\odot}]$	10^{-6}	scaled to fit SED best		
$R_{\text{in}} [\text{au}]$	40	5	60	2158
$R_{\text{out}} [\text{au}]$	200	100	500	1398
α	1	-1	3	80
$s_{\text{min}} [\mu\text{m}]$	3.73	0.1	10	403
$s_{\text{max}} [\mu\text{m}]$	1000	1000	1000	1
q	3.5	2	5	150
Inclination i [°]	0	0	0	1
Porosity \mathcal{P}	0.0–0.9	0.0	0.0	1

Results



- No porosity in fit process: Overestimation of slope q of the grain size distribution by up to 40% and the minimum grain size s_{min} by up to 230% for dim stars.

- Minimum grain size: smaller (50%) or larger (240%) than value derived from the analysis (luminosity and porosity dependent)

Conclusions

- Analytical expression for blowout size s_{blow} as function of stellar luminosity and porosity
- High porosities: Blowout size s_{blow} increases (factor 1.4 to 5, luminosity dependent)
- The higher the porosities, the lower $\beta = \frac{F_{\text{rp}}}{F_{\text{grav}}}$
- Grain size distribution and minimum grain size strongly depend on porosity

References

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Questions? I am somewhere close by, feel free to ask!