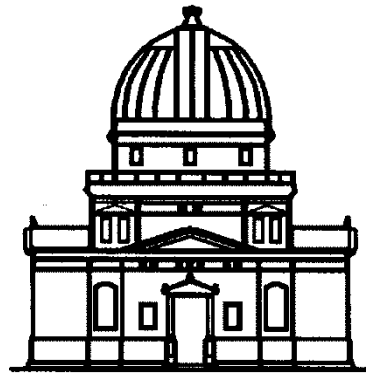


# Evolution of Galaxies:

Other galaxies, Abundance gradients,  
Mass-Metallicity



Observatoire astronomique  
de Strasbourg

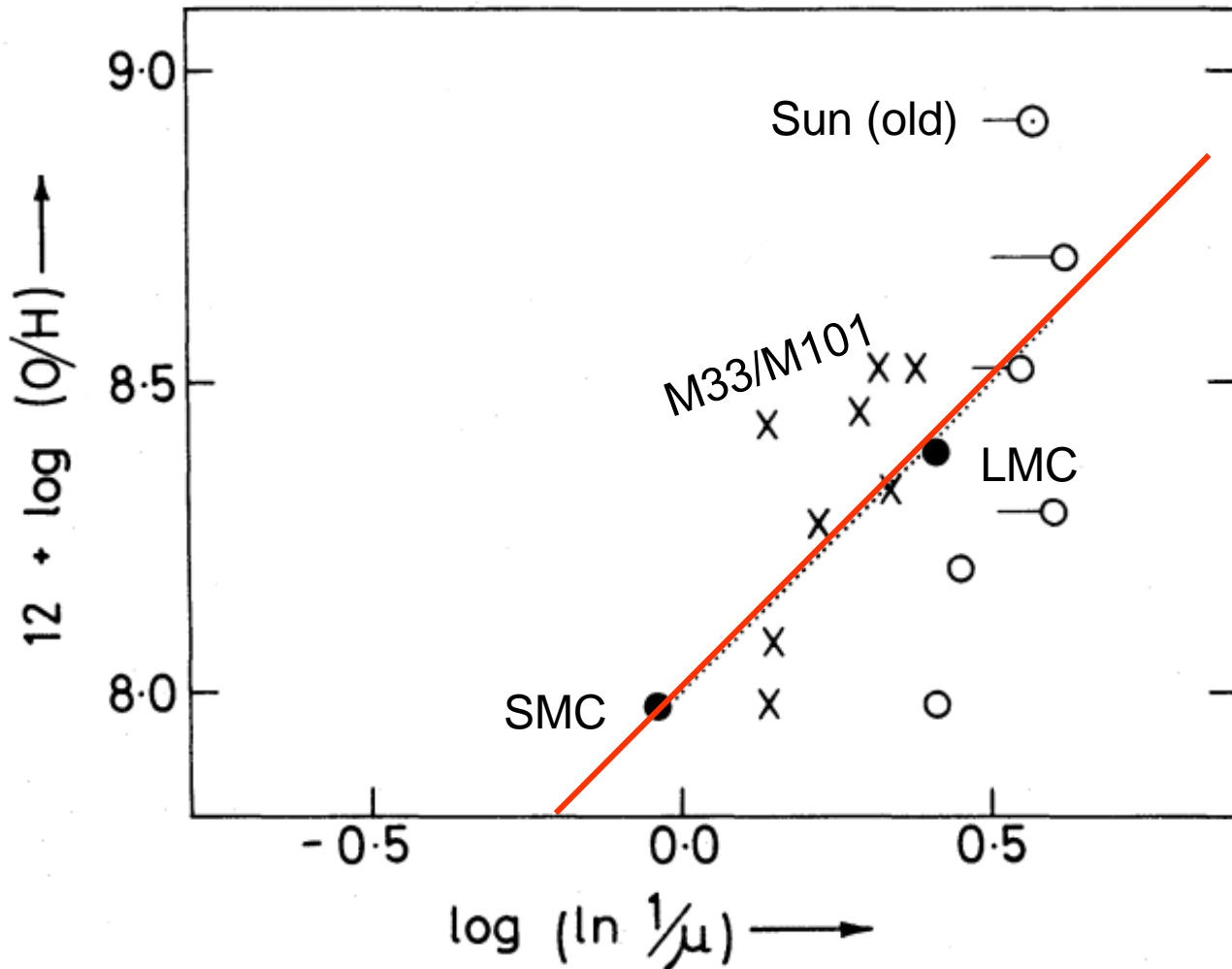
J.Köppen      joachim.koppen@astro.unistra.fr

<http://astro.u-strasbg.fr/~koppen/JKHome.html>

# Irregular galaxies

- Abundances: HII regions → uniform composition  
good test-beds for chemical evolution,  
but single events (SN) can disrupt dwarf galaxy
- $f_{\text{gas}}-Z$  relation:
  - low effective yield  $0.2 Z_{\text{sun}}$  + large scatter
  - steep IMF? SN-driven galactic winds? Accretion?

# Magellanic clouds have same yield

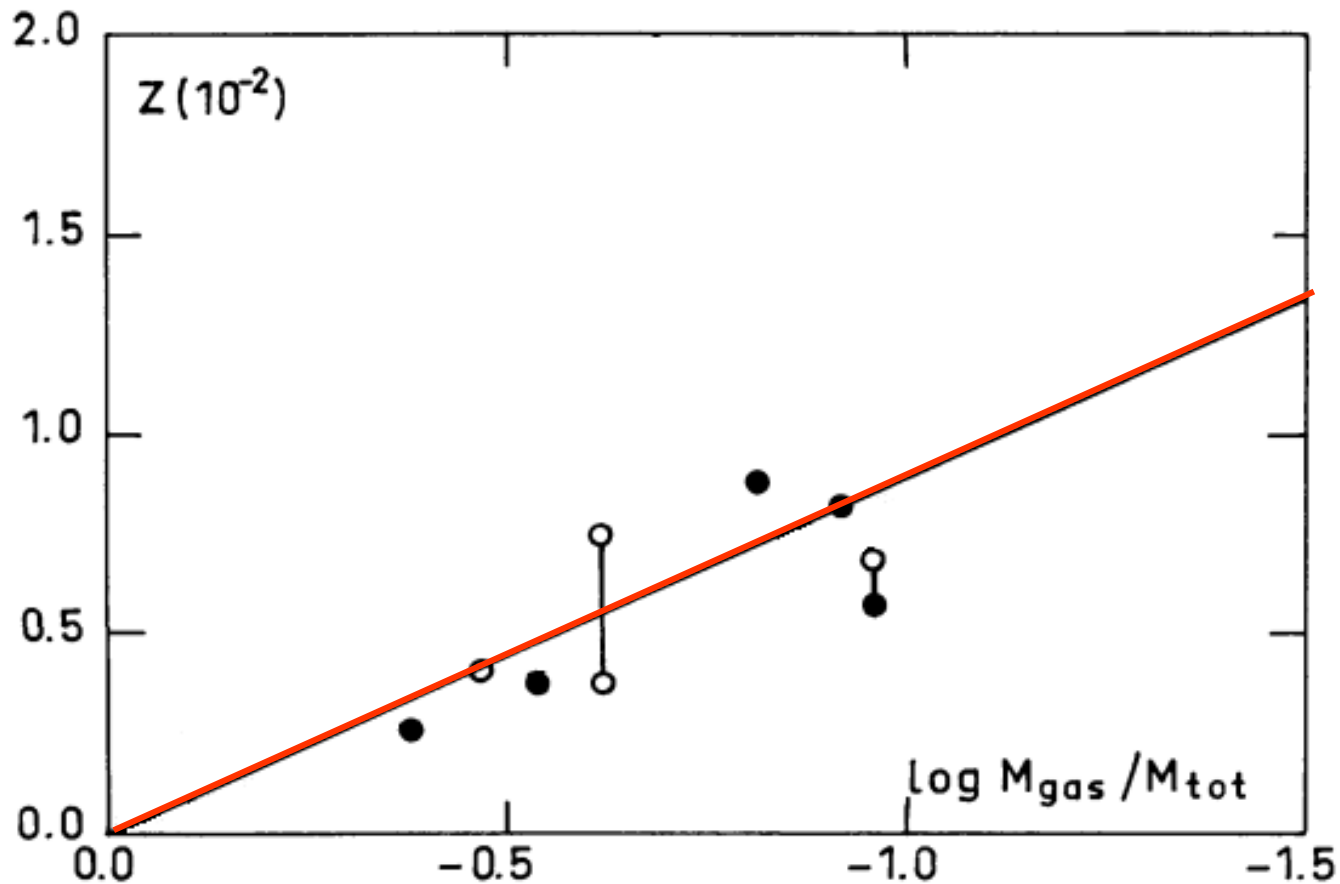


Pagel et al. 1978

$y = 0.003$

lower than MWG

# This agrees with other Irrs, too

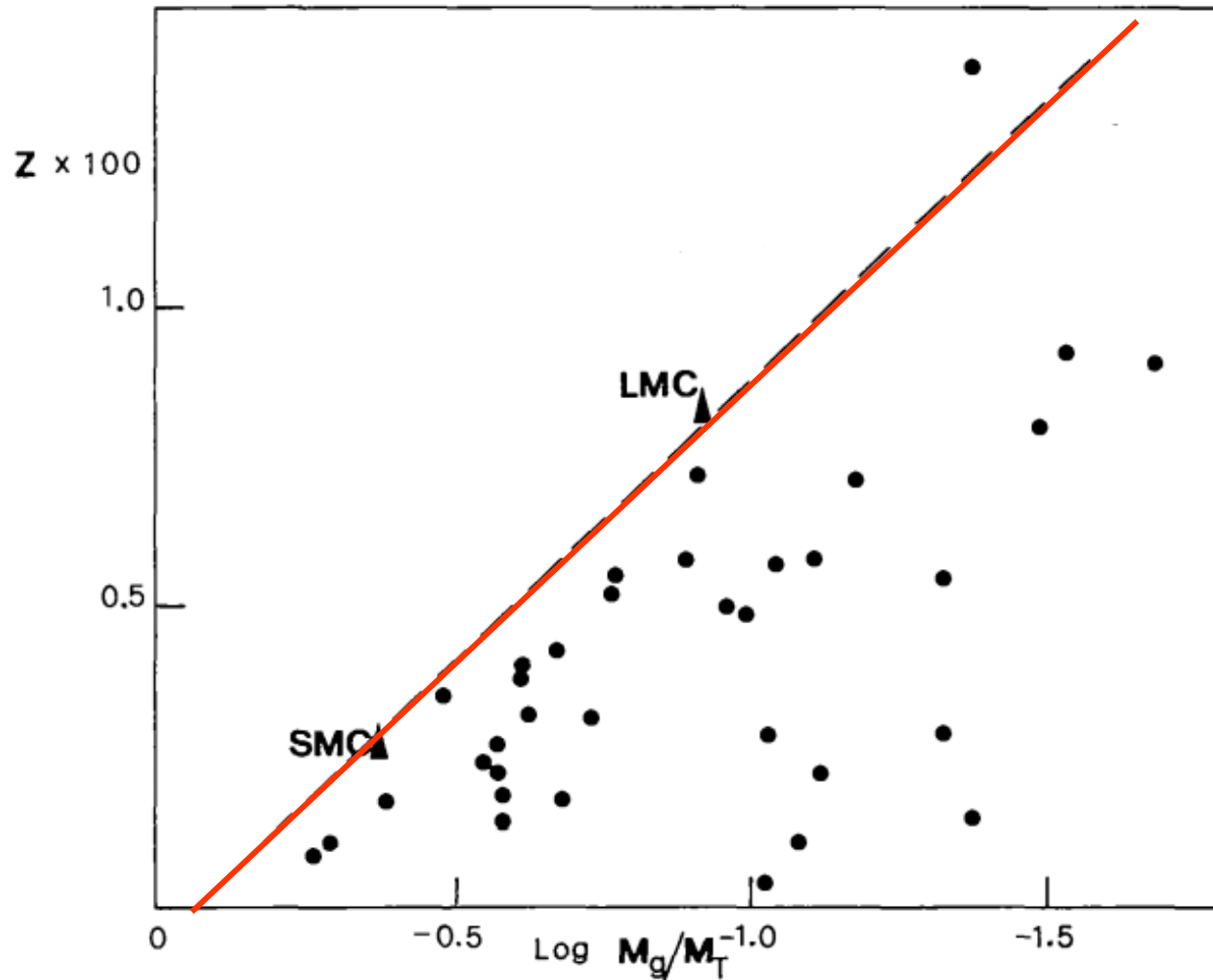


Lequeux et al. 1979

$y = 0.003$

lower than MWG

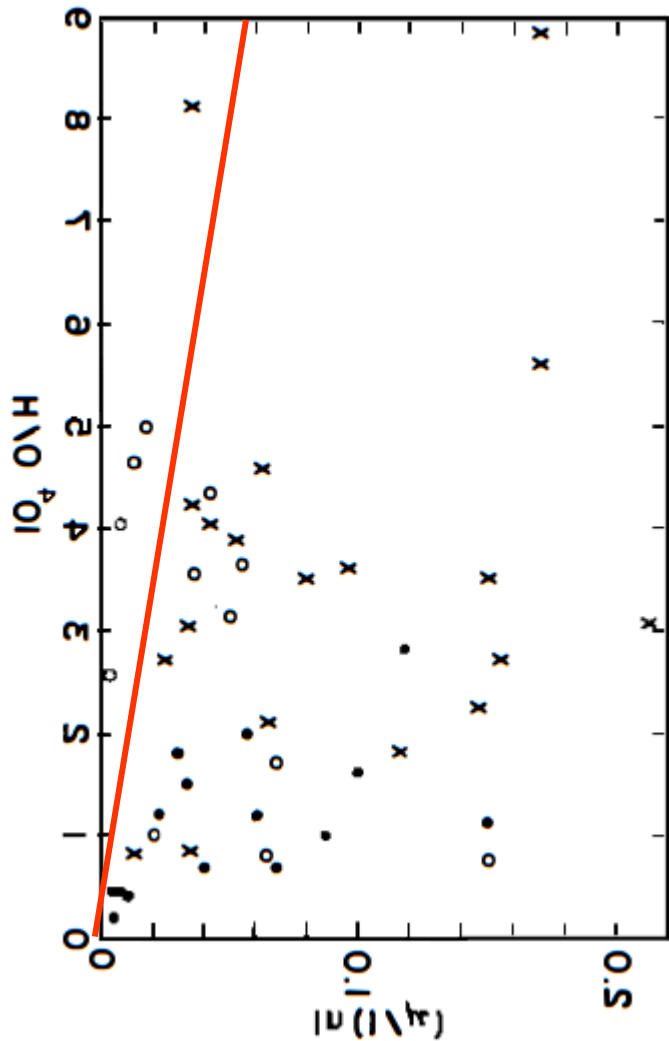
# Are the MCs special?



Matteucci+Chiosi 1983

Other irregulars need lower yields, e.g. by Infall, galactic winds

# Irregulars have large scatter



Gallagher+Hunter 1984

No systematic behaviour of different types of irregulars

NB. Abundances are estimated from empirical relations (strong line methods), because weak  $[\text{OIII}] \lambda 4363$  cannot be observed...

# Irregular galaxies

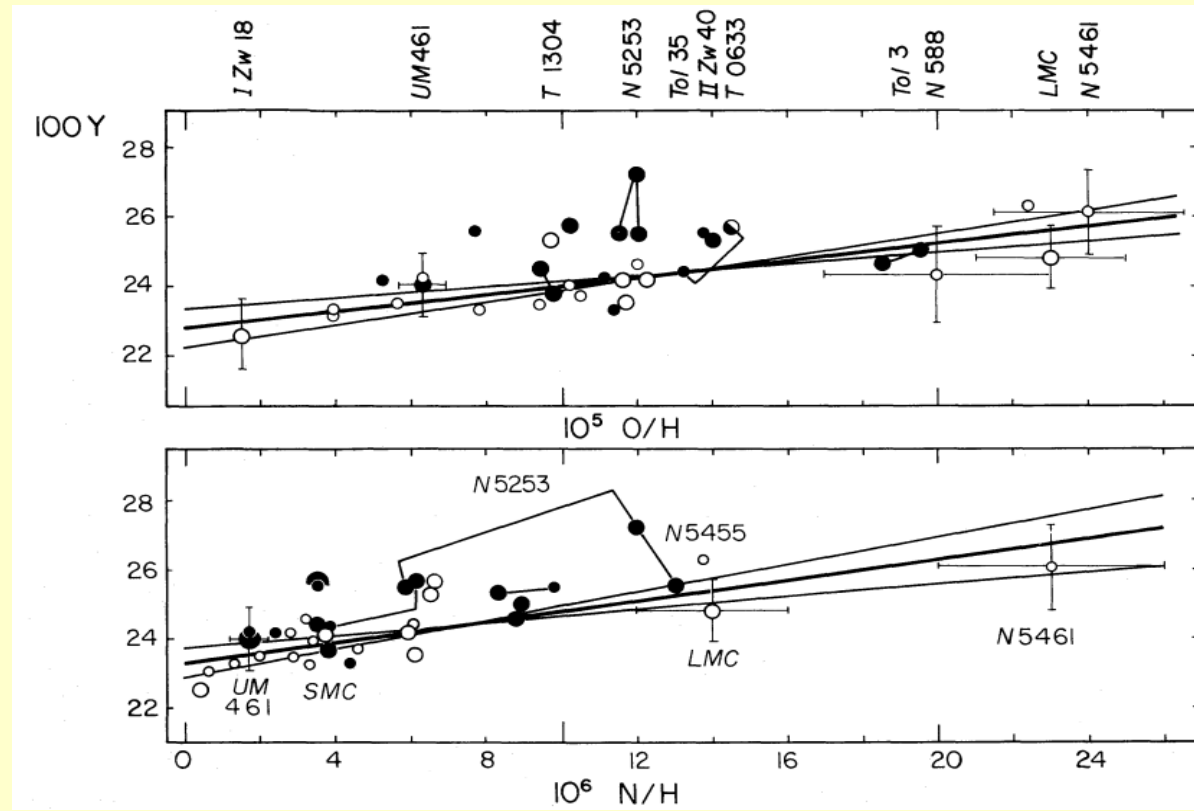
- Abundance ratios:

- $dY/dZ \approx 3..4 > y_{\text{He}}/y_Z \approx 2$  (stellar nucleo)

- Maeder92:  $m > 25 M_{\text{sun}} \rightarrow$  no SN but BH

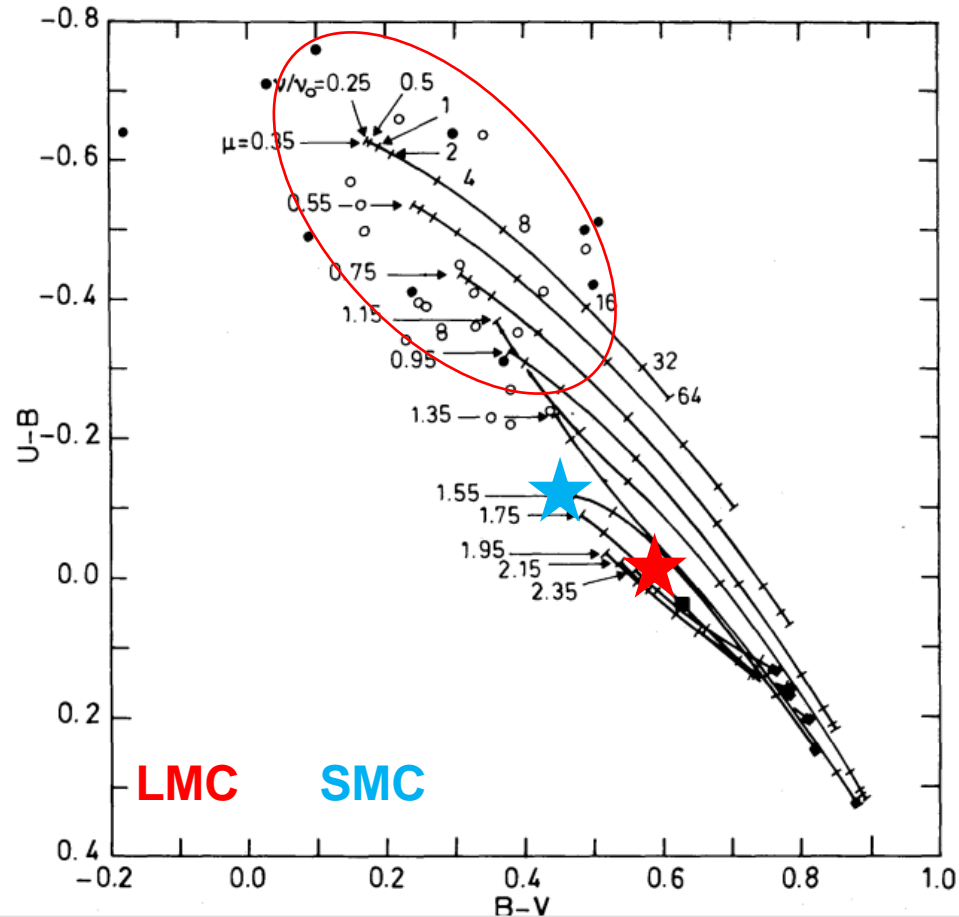
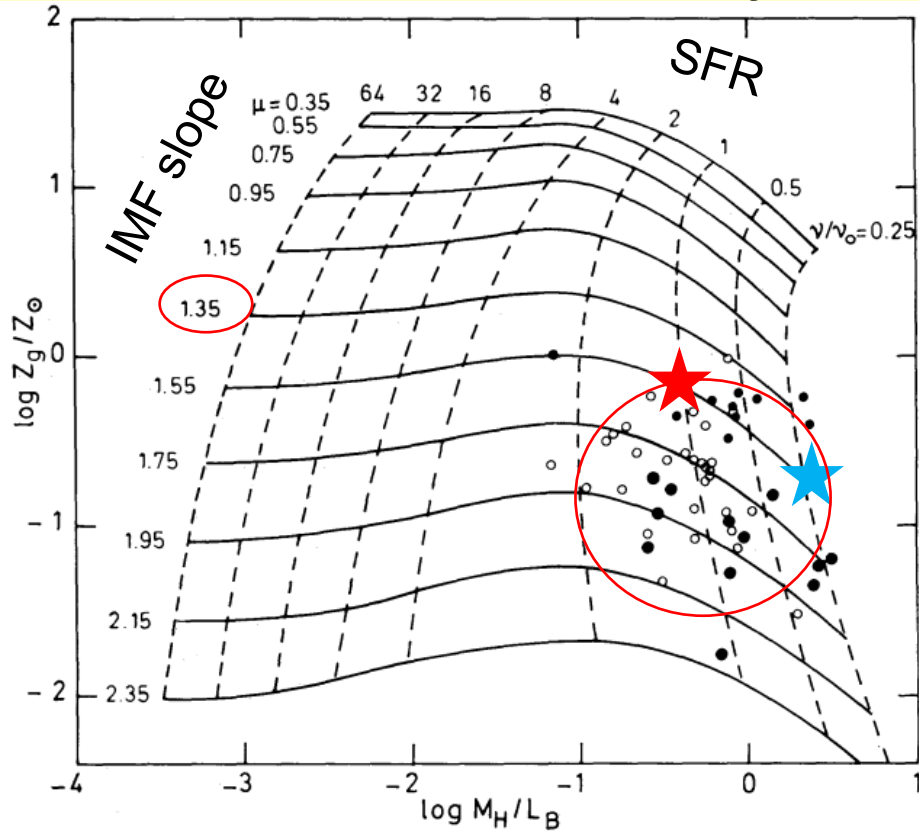
- Metal-enhanced SN-driven winds eject Z (from HMS) but not He (from IMS)

- C/O and N/O:  
see EoG\_7



# Chemistry vs. Photometry

Irregular have bluer colours than expected from models with continuous star formation histories

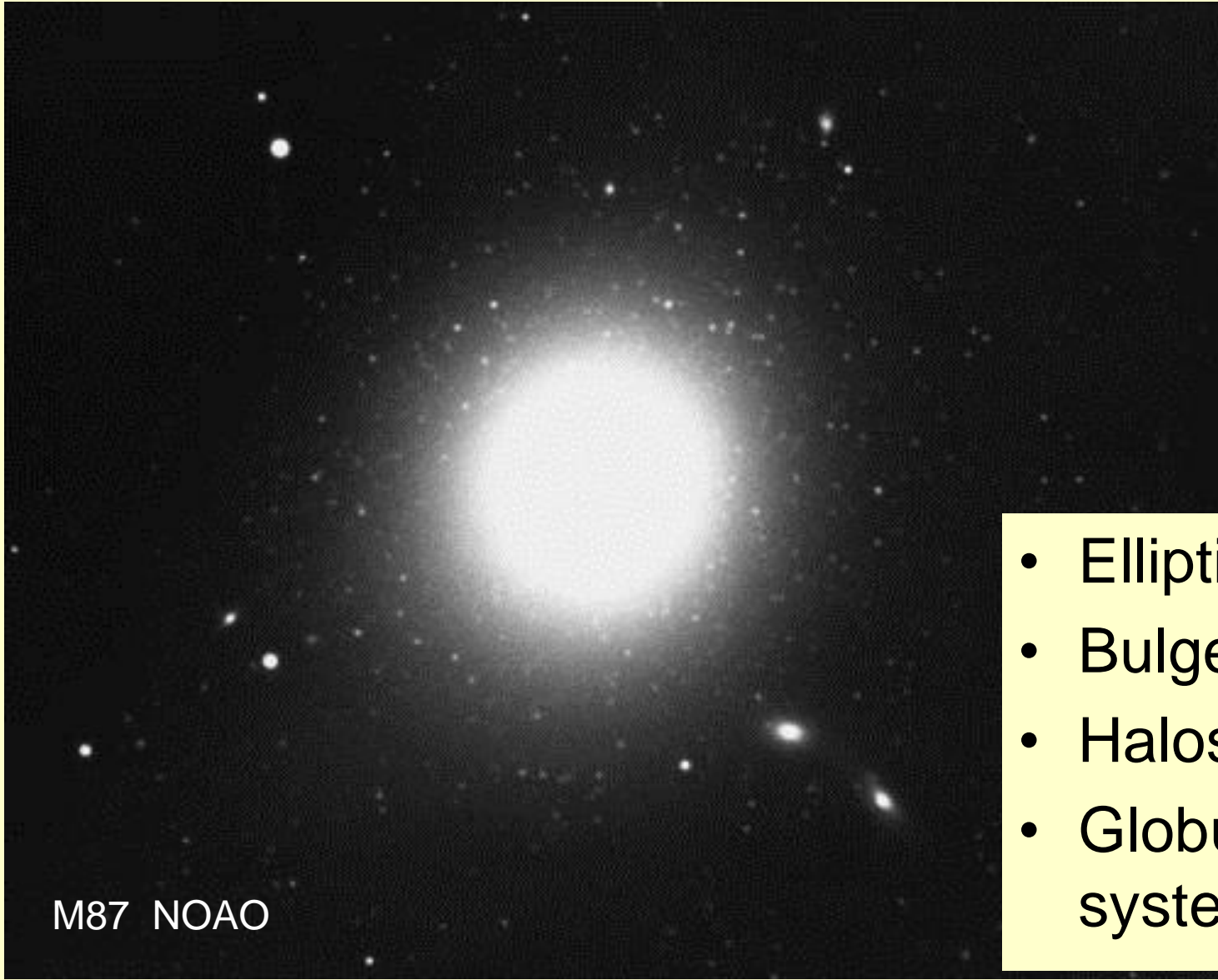


blue colours have short memory:  
influenced by recent SF  $\rightarrow$  starbursts

Arimoto + Tarrab 1990



# Spheroidal systems



M87 NOAO

- Ellipticals and S0
- Bulges
- Halos
- Globular cluster systems

# Ellipticals and Bulges

Data = integrated colours and spectra

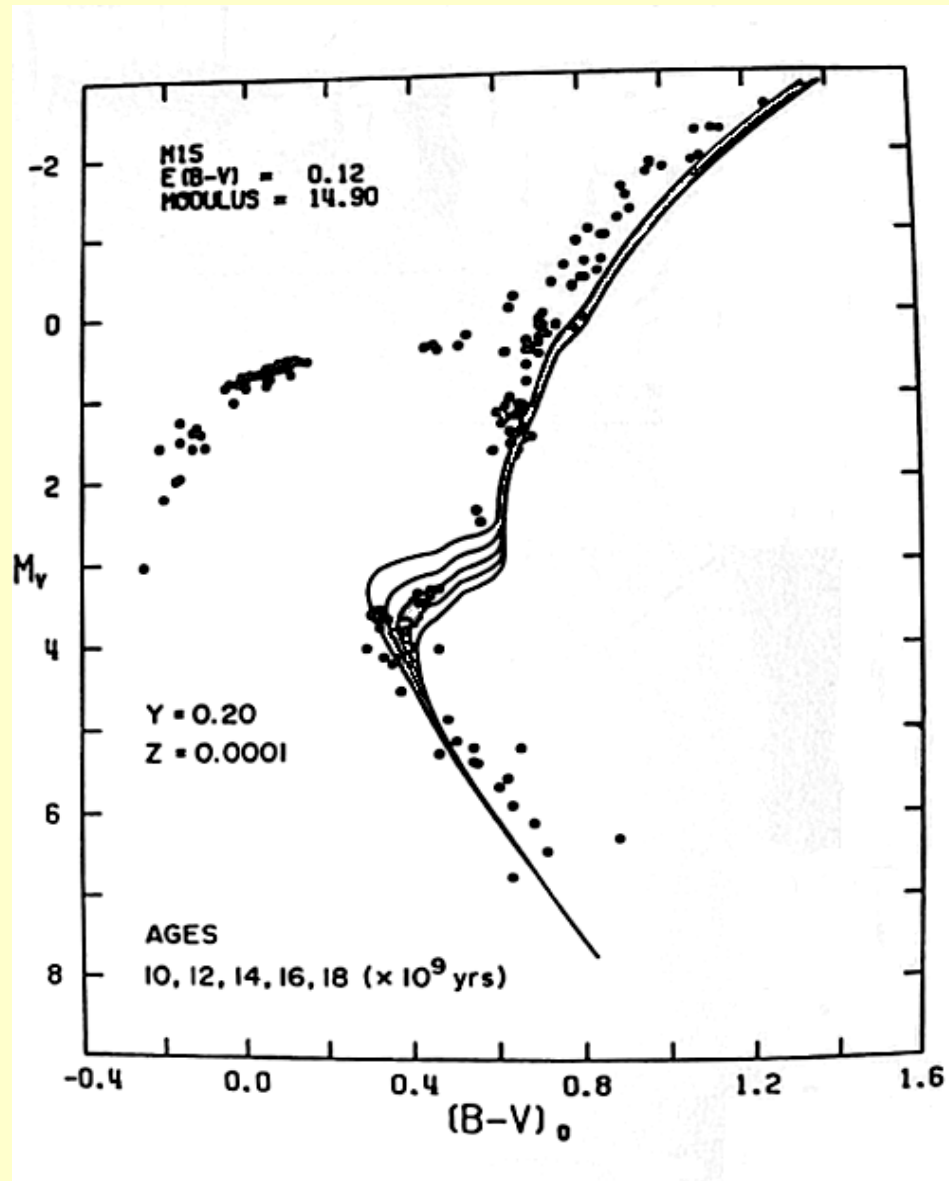
= mixture of ages & metallicities

Requires modeling (A.Lançon ...)

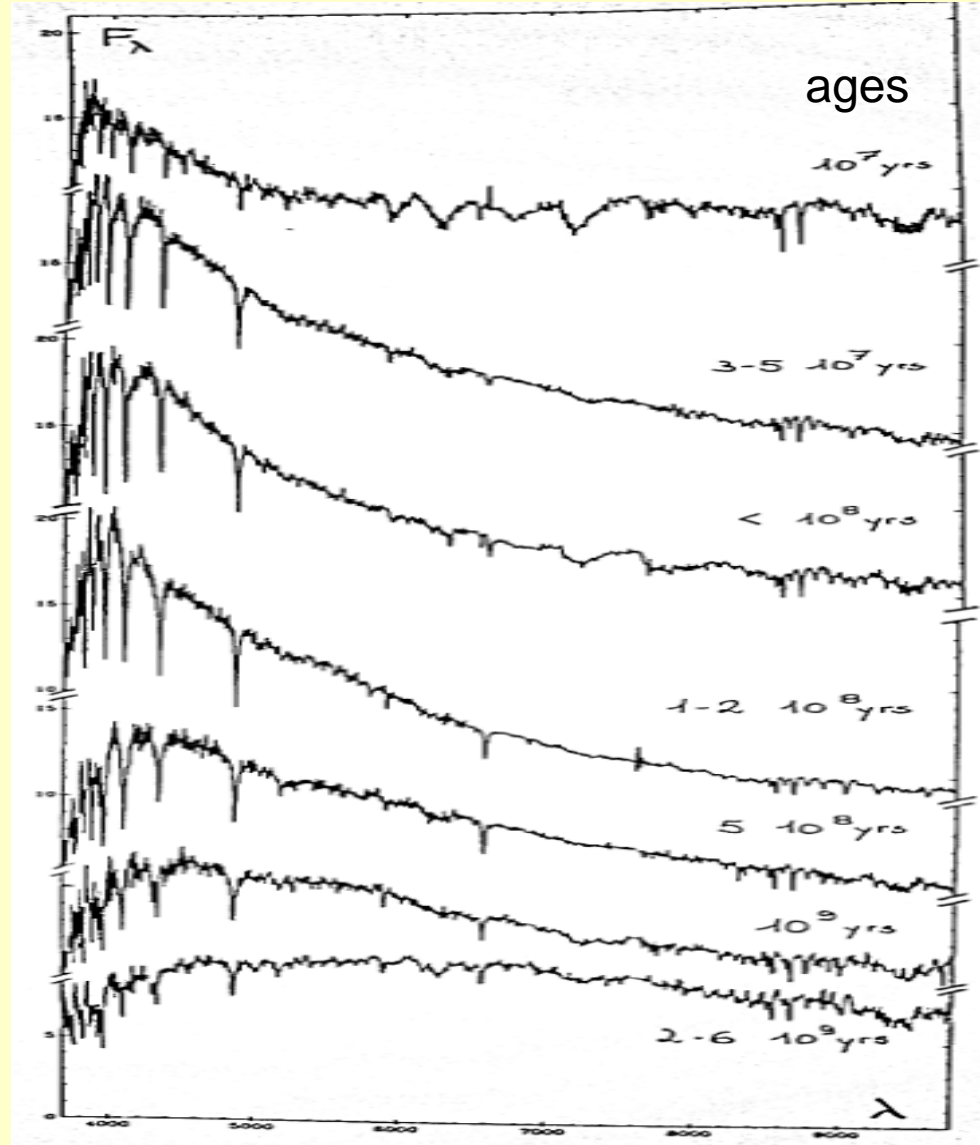
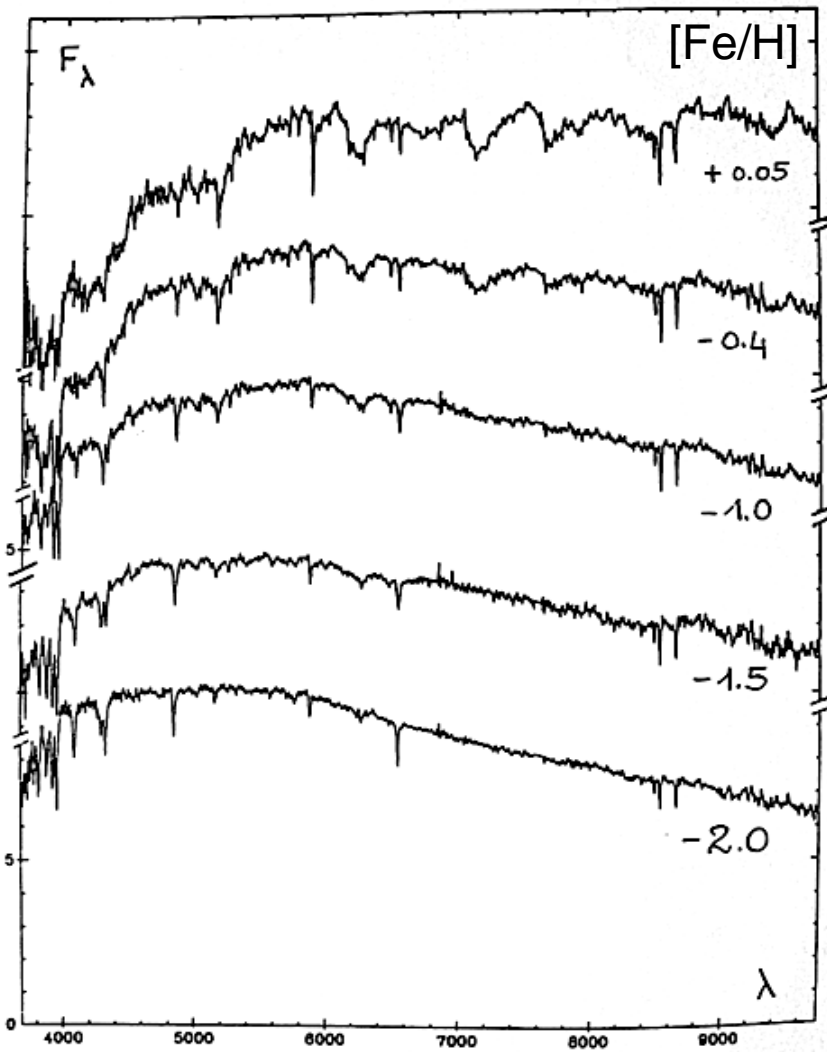
- Population synthesis: fit data by
  - SFH + AMR + IMF + isochrones + stellar spectra (theo/obs.)
  - SFH + AMR + library of observed spectra of MW+MC clusters (Z, age)
- Evolutionary population synthesis
  - SFR + infall etc + (AMR=chem.ev) + IMF + isochrones + stellar spectra
- Base = objects of single age & metallicity
  - Stellar clusters (obs.)
  - SingleStellarPopulation (theor.)

**Degeneracy**  $Mg_2 \sim (Z * age)^{0.41}$

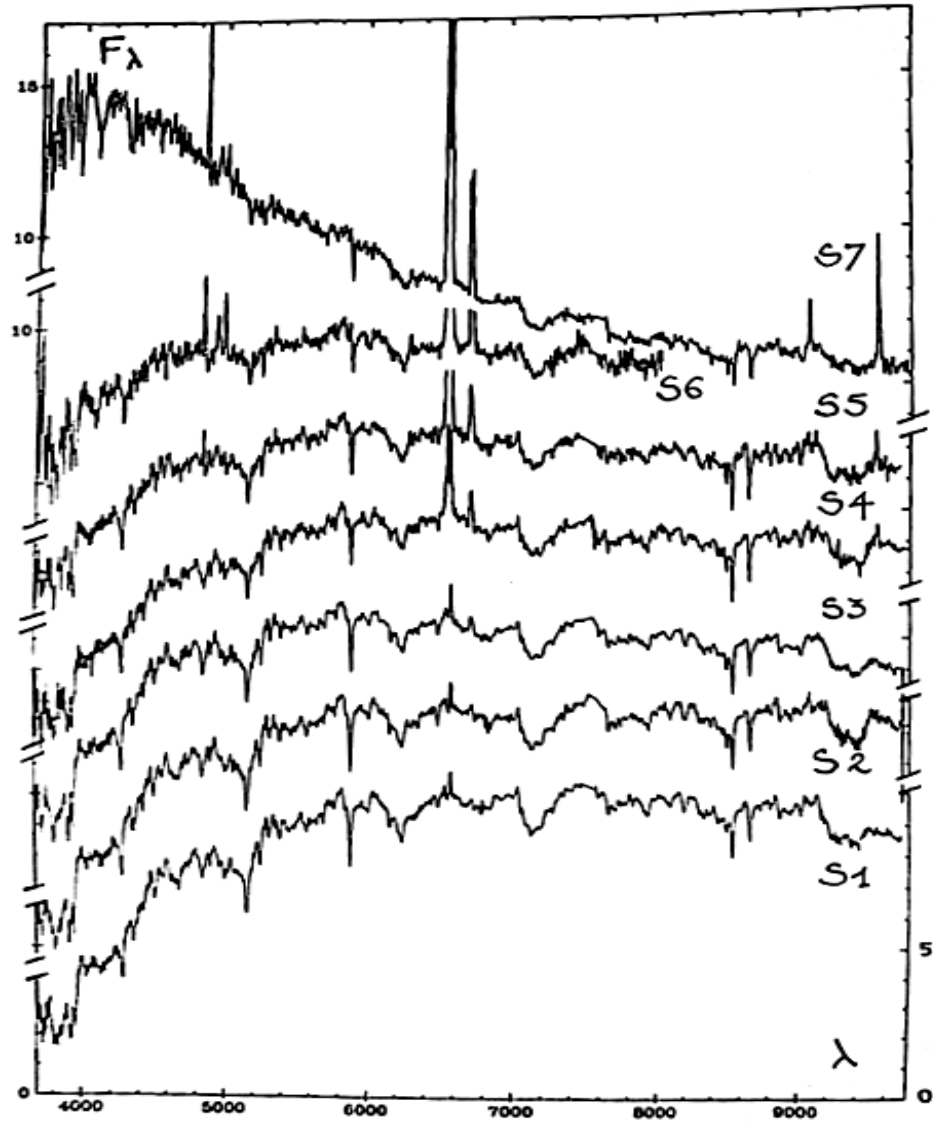
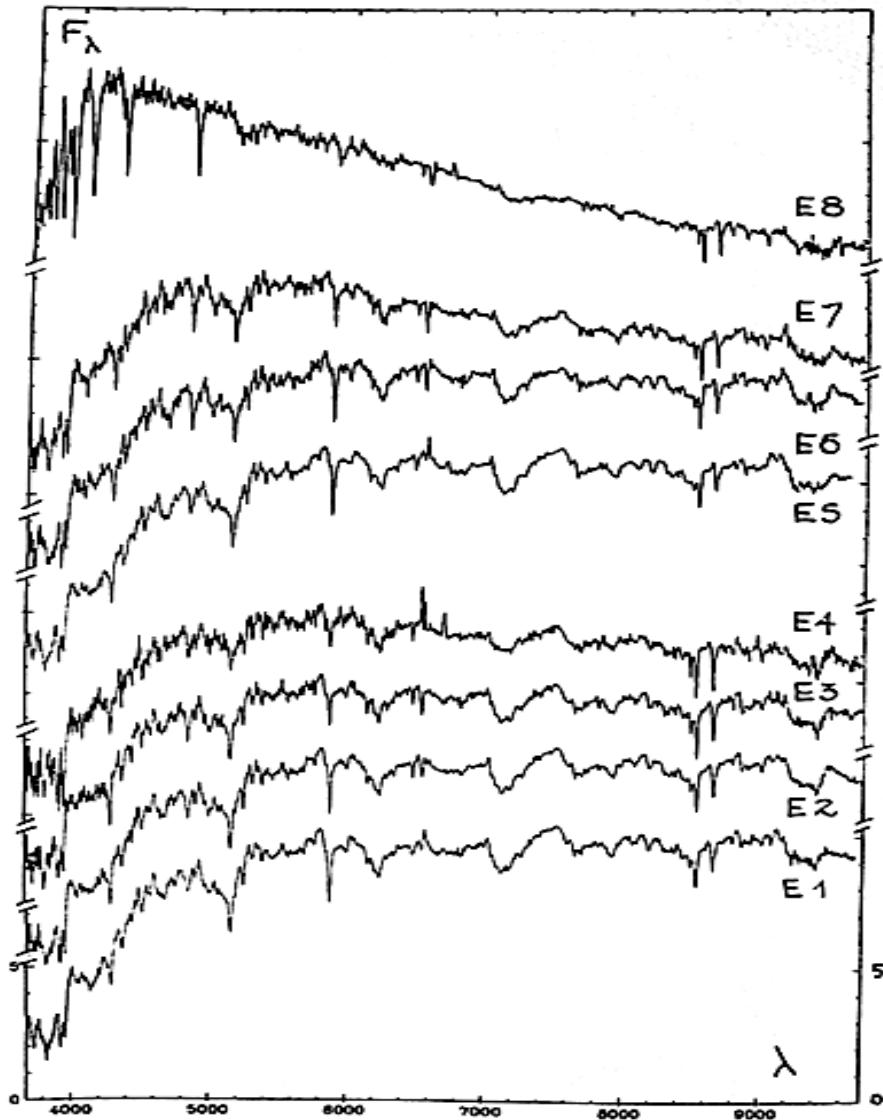
# Globular clusters are single-age populations



# Cluster spectra (Bica 1986)

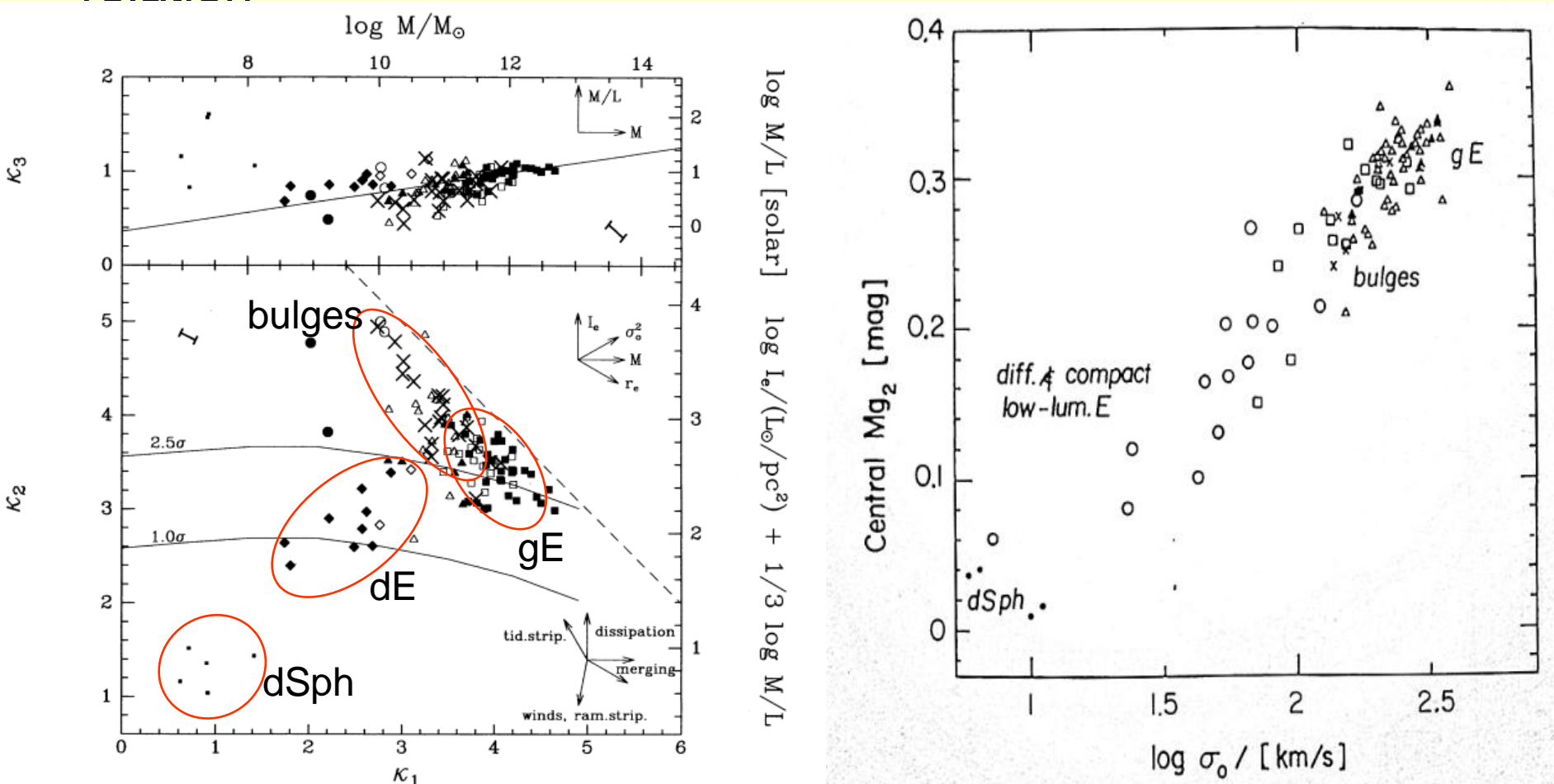


# Spectra of E and S galaxies

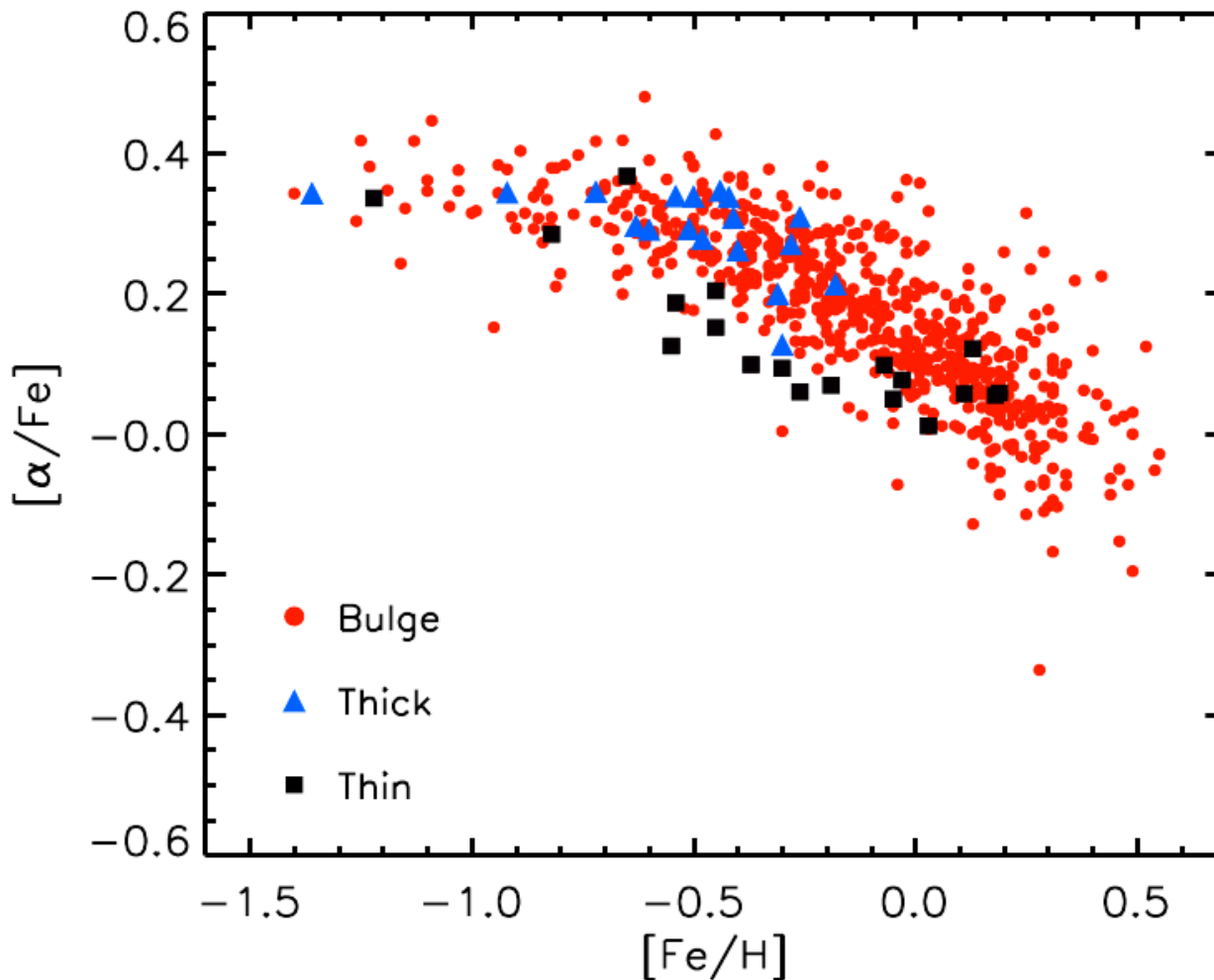


# Fundamental Plane in $(\sigma, \Sigma, R)$ space

Two sequences, but all follow the **same** mass-metallicity relation



# Galactic Bulge



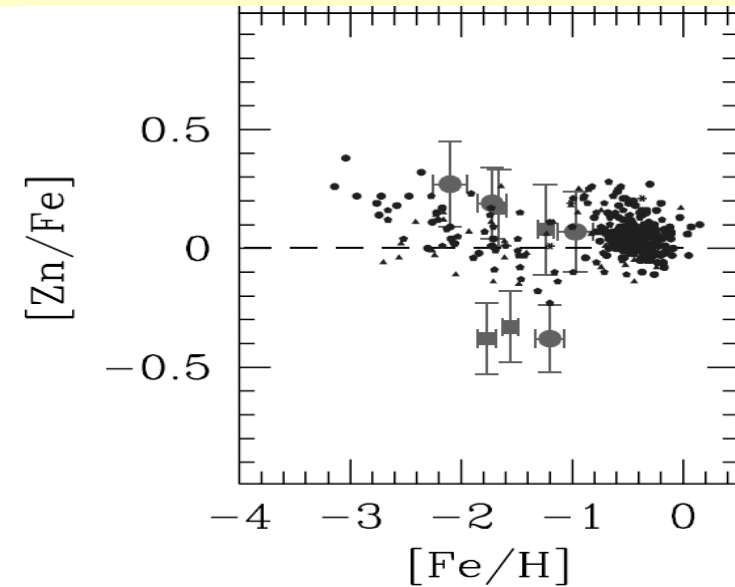
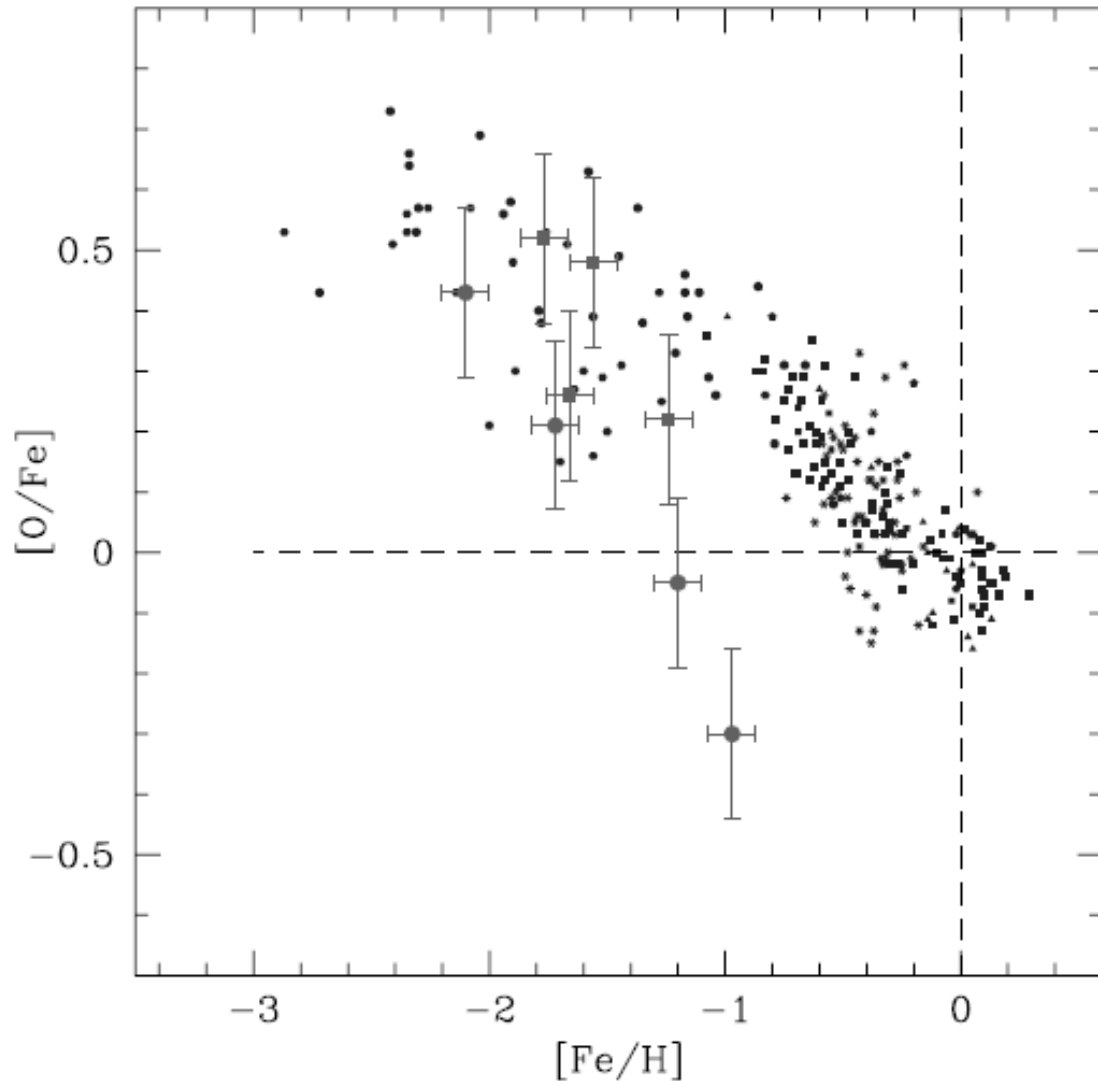
Spectro R=20000  
ESO VLT  
S/N = 40..90

Similar  $[\text{Fe}/\text{H}]$  range  
as thin disk

$[\alpha/\text{Fe}]$  is higher than  
in the disk

Thick disk:  
 $[\text{Fe}/\text{H}] = -1.5 \dots -0.2$   
 $[\alpha/\text{Fe}]$  like bulge

# Sculptor dSph galaxy



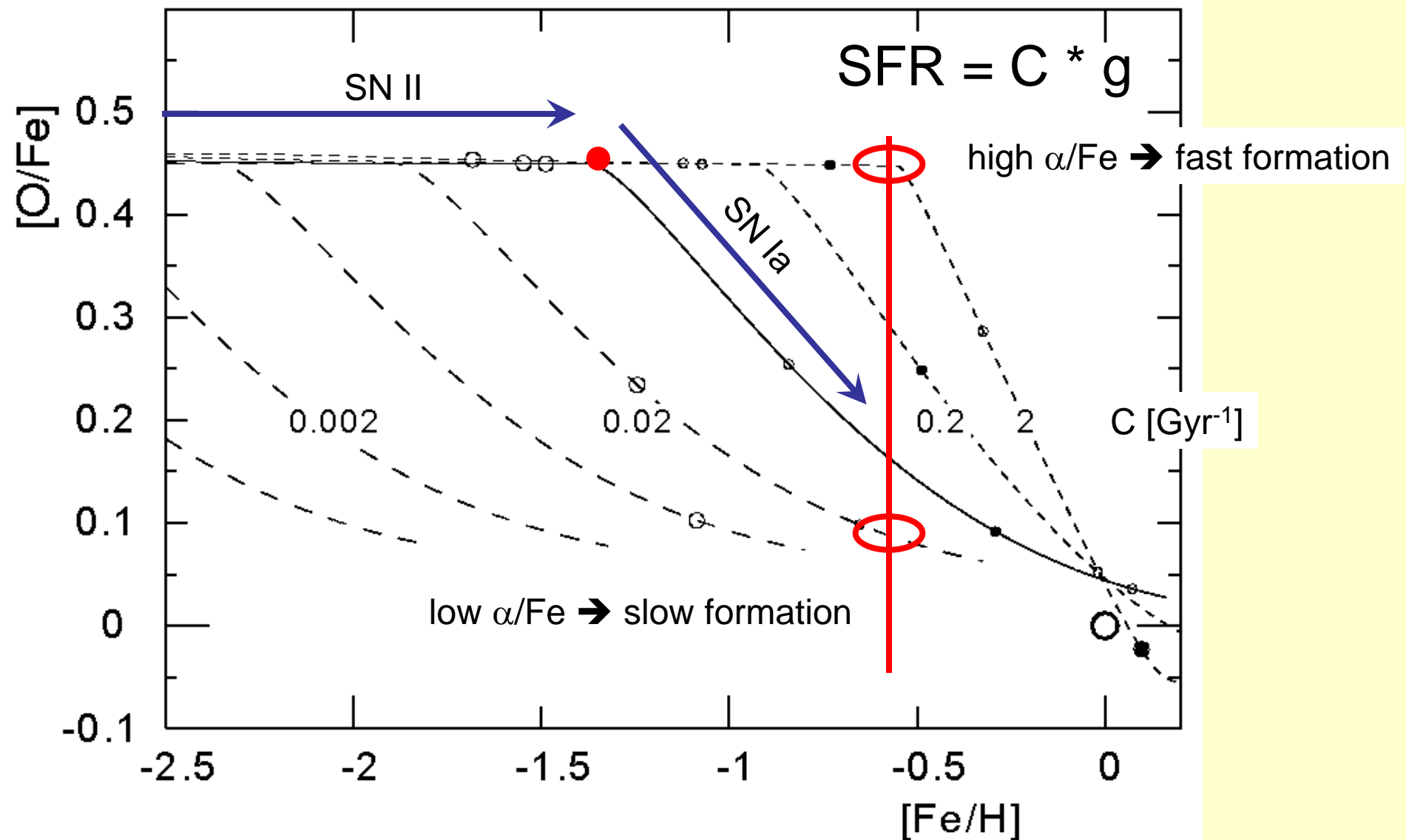
Giant stars  
compared to solar  
neighbourhood:

- ➔ lower  $\{Fe/H\}$
- ➔ steeper O/Fe-Fe/H relation!

Geisler 2005

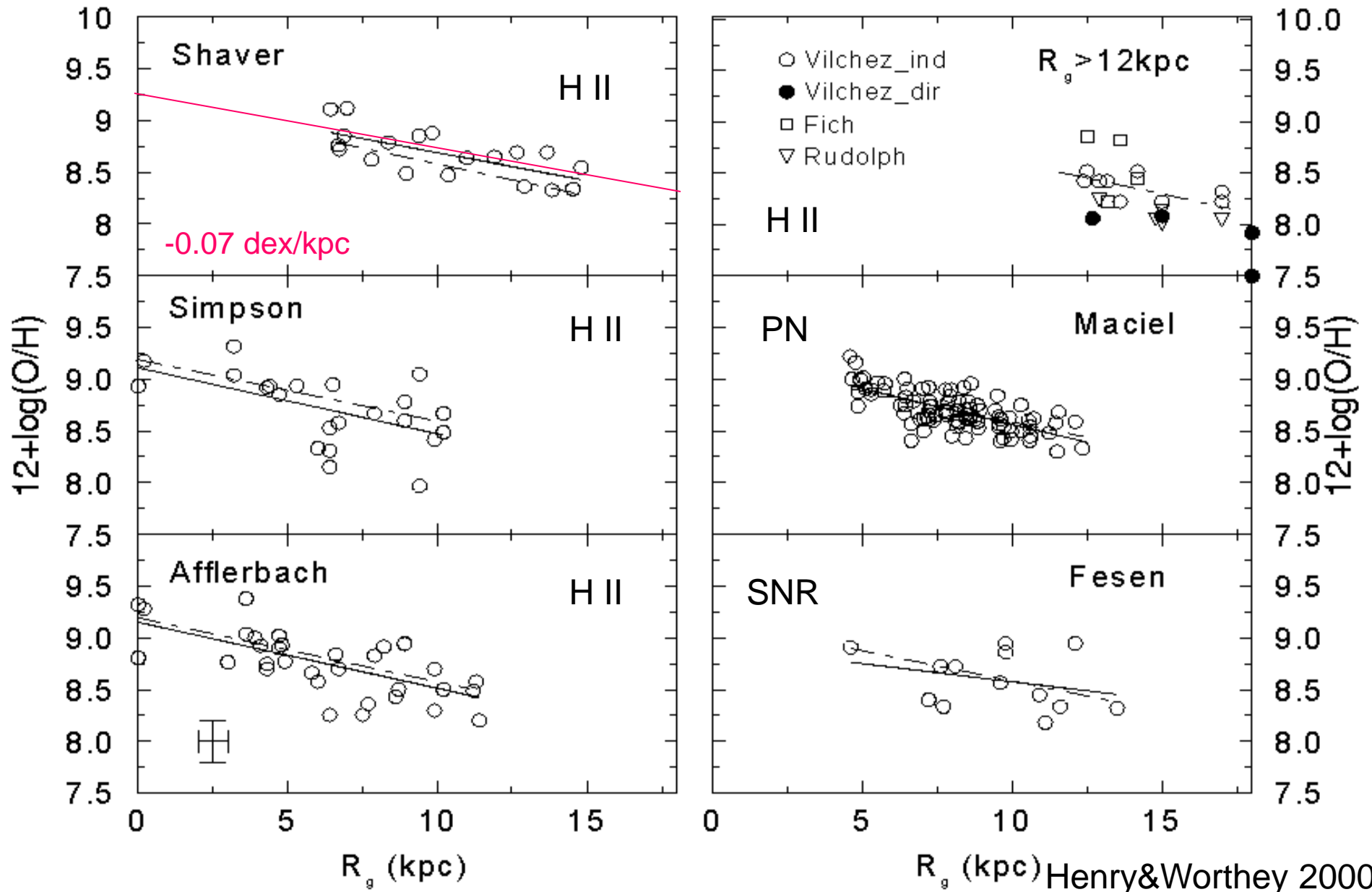


# O/Fe (or $\alpha$ /Fe) ratio measures SFR time-scale (illustrative model)

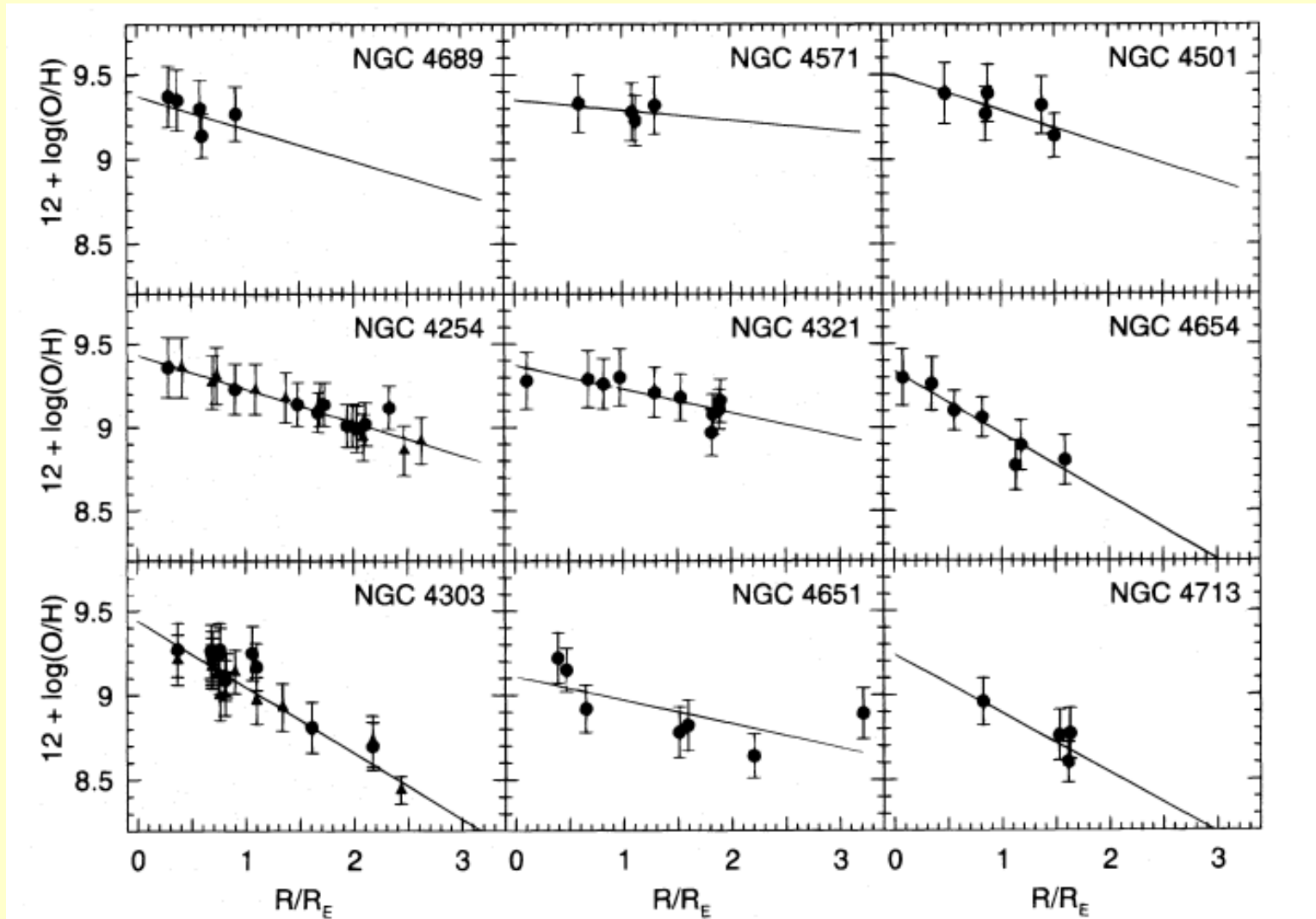


# Radial abundance gradients in disk galaxies

# e.g. the Milky Way



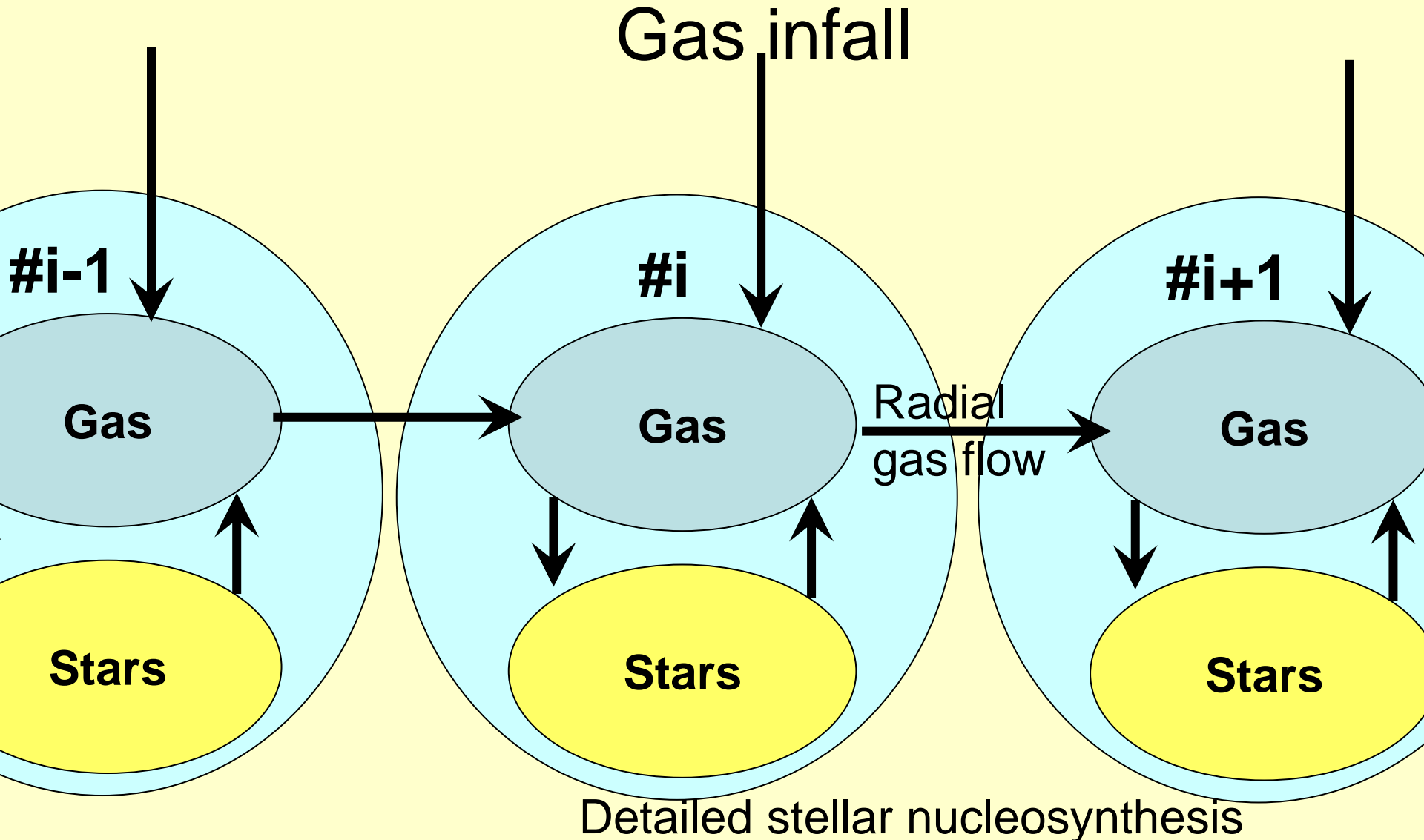
# Virgo cluster spirals



# Gradients: proposed explanations

- Gas fraction increases radially (i.e. state of evolution)
- Radial variation of SFR
- Radial variation of nucleosynthesis
- Radial variation of IMF
- Radially dependent infall → ‘dilution’
- Radial gas flows (various origins)
- ...

# Make a model for the disk



Assuming the initial conditions  $g_k = 0$ ,  $s_k = 0$ ,  $z_k = 0$ , the equations are solved by

$$g_k(t) = \sum_{i=1}^k (A_{ki}e^{-a_it} + B_{ki}e^{-b_it}), \quad (25)$$

$$s_k(t) = \alpha_k C_k \sum_{i=1}^k \left[ \frac{A_{ki}}{a_i} (1 - e^{-a_it}) + \frac{B_{ki}}{b_i} (1 - e^{-b_it}) \right] + s_k(t=0), \quad (26)$$

$$z_k(t) = \sum_{i=1}^k U_{ki}e^{-a_it} + \sum_{i=1}^k V_{ki}e^{-b_it} + \sum_{i=1}^k W_{ki} t e^{-b_it}, \quad (27)$$

# Analytical solution

where the coefficients are evaluated by recursion:

$$A_{ki} = \frac{\gamma_{k-1} A_{k-1 i}}{b_k - a_i}, \quad (28a)$$

$$B_{ki} = \frac{\gamma_{k-1} B_{k-1 i}}{b_k - b_i}, \quad (28b)$$

$$U_{ki} = \frac{D_k A_{ki} + \gamma_{k-1} U_{k-1 i}}{b_k - a_i}, \quad (28c)$$

$$V_{ki} = \frac{\gamma_{k-1} V_{k-1 i}}{b_k - b_i}, \quad (28d)$$

$$W_{ki} = \frac{\gamma_{k-1} W_{k-1 i}}{b_k - b_i}, \quad (28e)$$

for  $k > i$ , and

$$A_{kk} = \frac{f_k}{b_k - a_k}, \quad (29a)$$

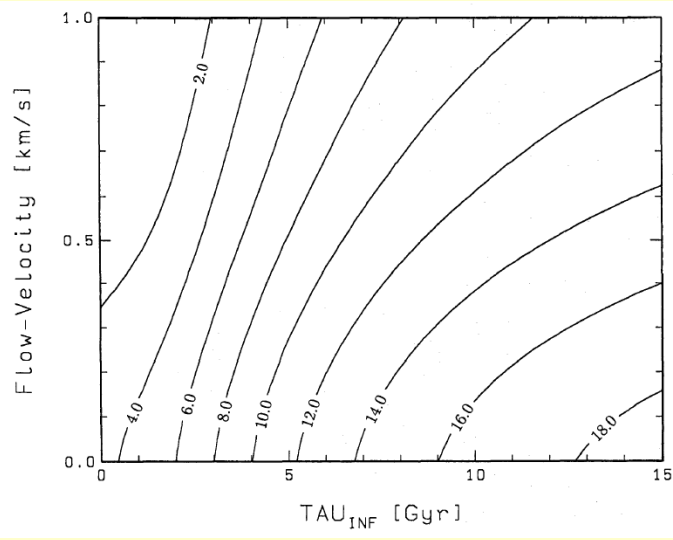
$$B_{kk} = - \sum_{i=1}^k A_{ki} - \sum_{i=1}^{k-1} B_{ki} + g_k(0). \quad (29b)$$

$$U_{kk} = \frac{D_k A_{kk} + f_k Z_f}{b_k - a_i}, \quad (29c)$$

$$V_{kk} = - \sum_{i=1}^k U_{ki} - \sum_{i=1}^{k-1} V_{ki} + z_k(0), \quad (29d)$$

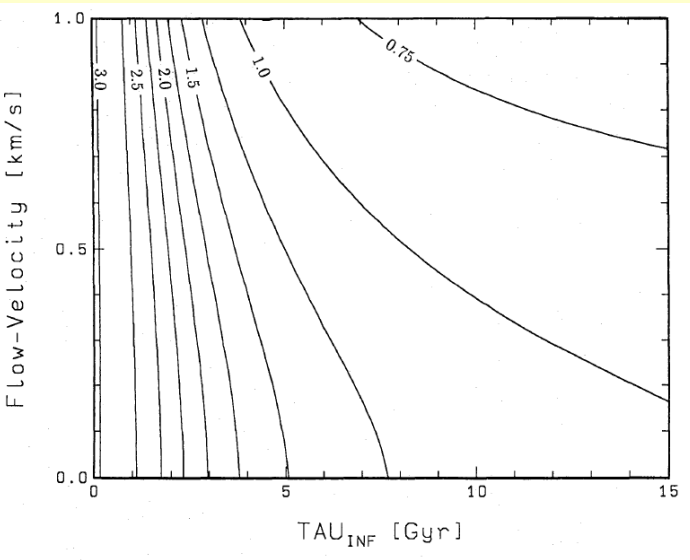
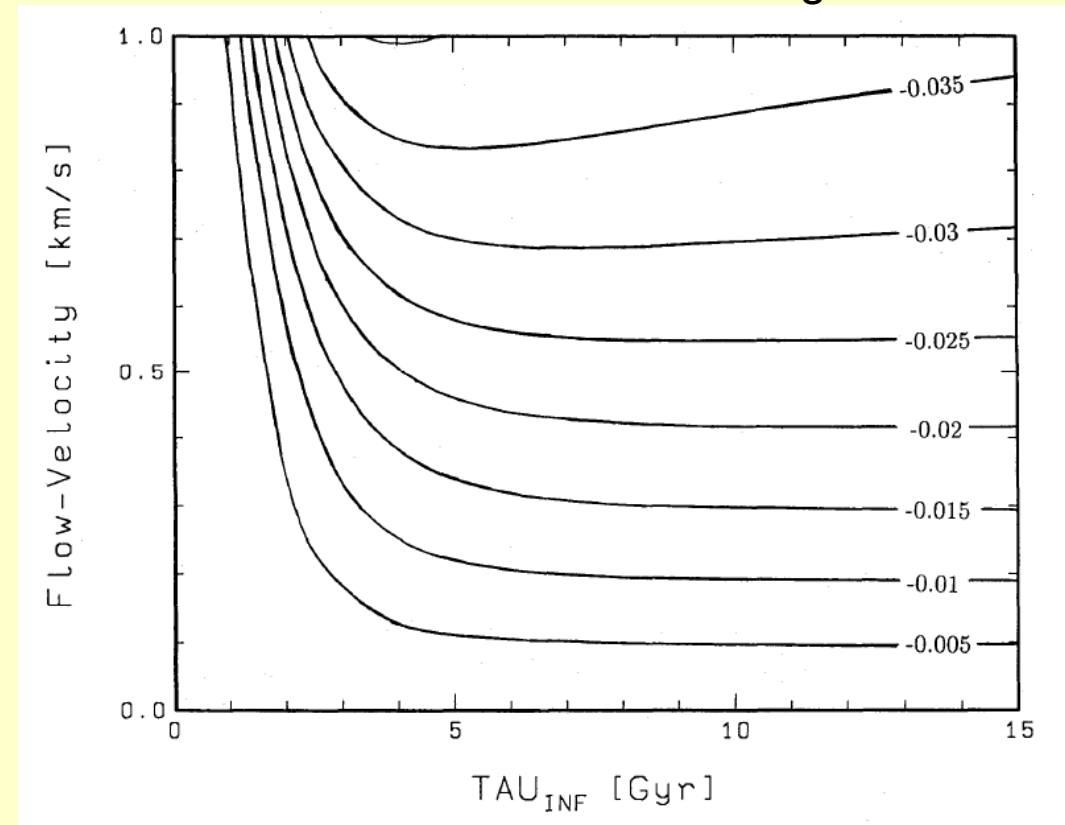
$$W_{kk} = D_k B_{kk}. \quad (29e)$$

# Easier maps



Gas surface density

Abundance gradient

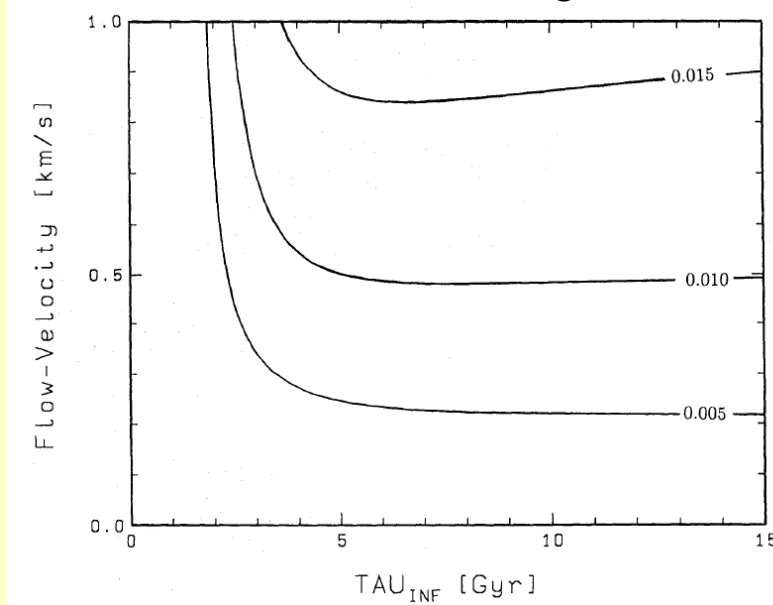
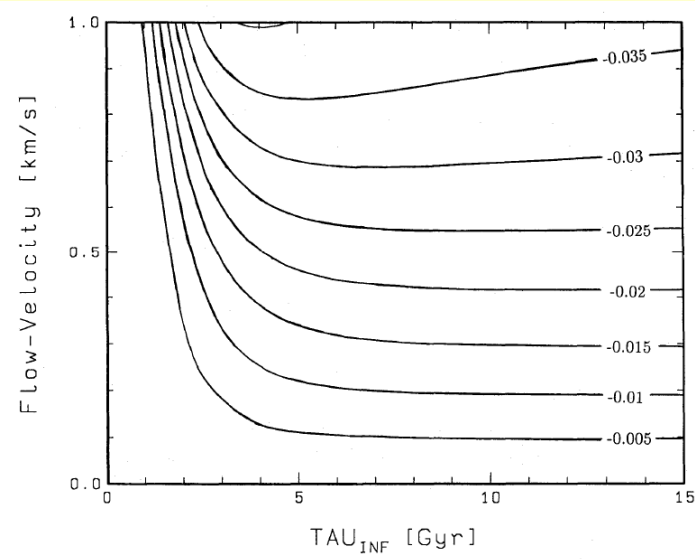


Gas metallicity

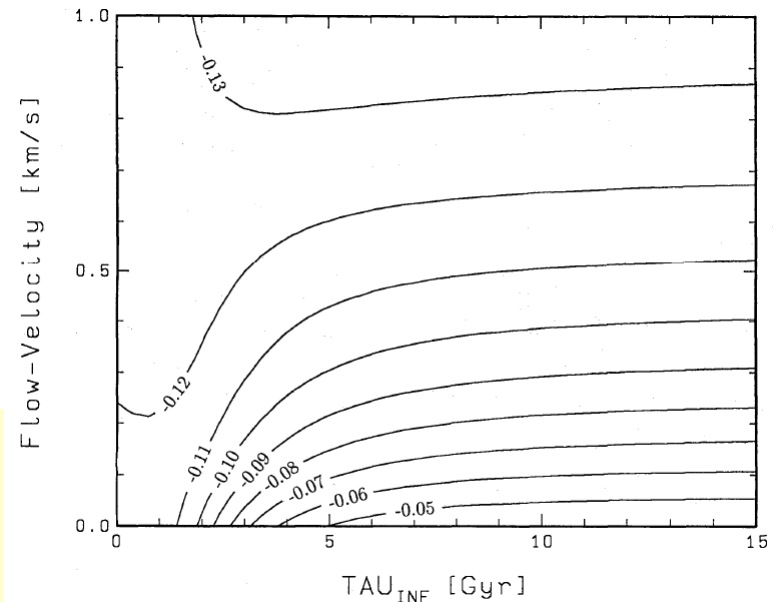


# Gradient maps: boring

With gradient in radial velocity ...



... and SFR gradient



# Let's look at the equation (IRA)

surface densities:

$$\frac{\partial g}{\partial t} + \frac{1}{r} \frac{\partial}{\partial r} (rvg) = -\alpha(r)\Psi(r, t) + f(r, t)$$

accretion

$$\frac{\partial z}{\partial t} + \frac{1}{r} \frac{\partial}{\partial r} (rvz) = -\alpha(r)Z(r, t)\Psi(r, t) + \alpha(r)y(r)\Psi(r, t) + Z^f(r)f(r, t)$$

With  $z = Zg$  one gets

$$\frac{\partial \ln Z}{\partial t} = \frac{1}{Zg} \frac{\partial z}{\partial t} - \frac{1}{g} \frac{\partial g}{\partial t} = \frac{\alpha y \Psi}{gZ} - \left(1 - \frac{Z^f}{Z}\right) \frac{f}{g} - v \frac{\partial \ln Z}{\partial r}$$

for continuously differentiable functions we have:

$$\frac{\partial}{\partial t} \left( \frac{\partial \ln Z}{\partial r} \right) = \frac{\partial}{\partial r} \left( \frac{\partial \ln Z}{\partial t} \right)$$

Time evolution of the gradient:

$$\begin{aligned} \frac{\partial}{\partial t} \left( \frac{\partial \ln Z}{\partial r} \right) = & + \frac{\alpha y \Psi}{gZ} \frac{d \ln(\alpha y)}{dr} \\ & + \frac{\alpha y \Psi}{gZ} \frac{\partial \ln(\Psi/g)}{\partial r} \\ & - \frac{f}{g} \frac{\partial \ln(f/g)}{\partial r} \\ & + \frac{\partial}{\partial r} \left( \frac{Z^f f}{Zg} \right) \\ & - \frac{dv}{dr} \frac{\partial \ln Z}{\partial r} - v \frac{\partial^2 \ln Z}{\partial r^2} \\ & - \frac{\alpha y \Psi}{gZ} \frac{\partial \ln Z}{\partial r} \end{aligned}$$

gradients grow by

yield, IMF gradient

nonlinear SFR, SFR gradient

accretion rate gradient

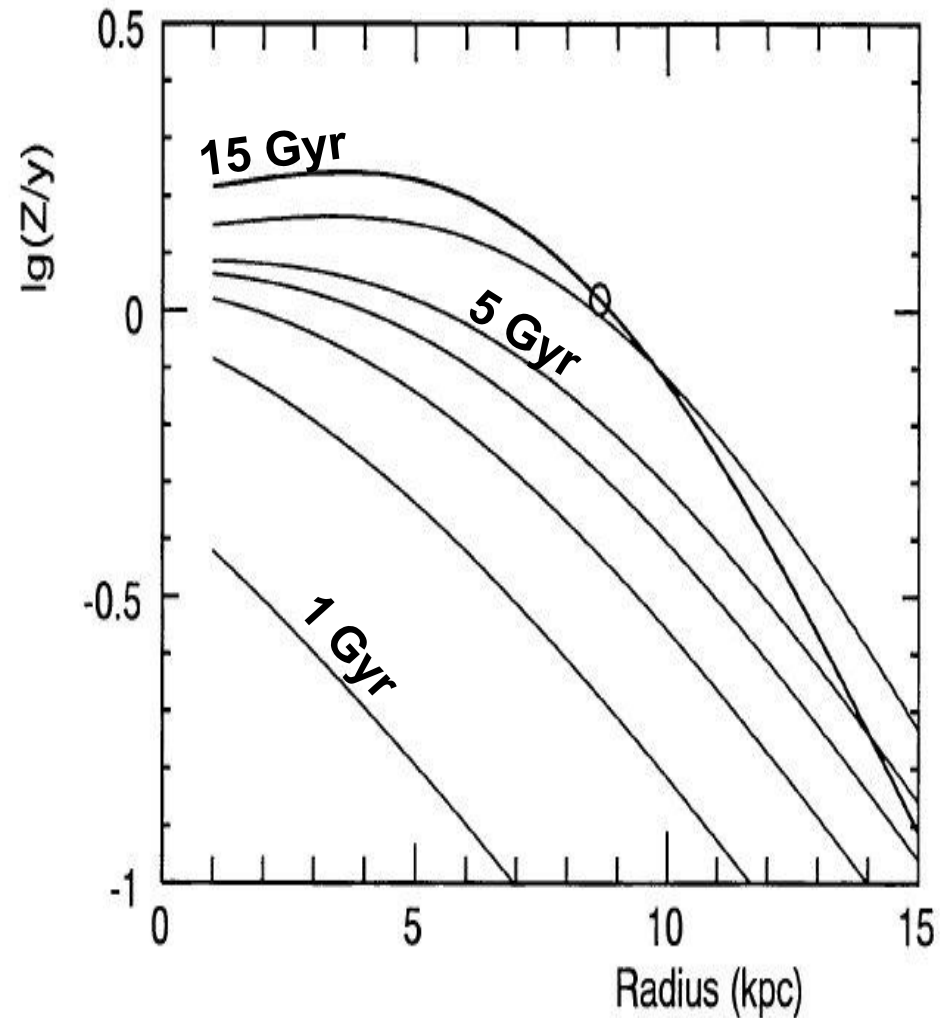
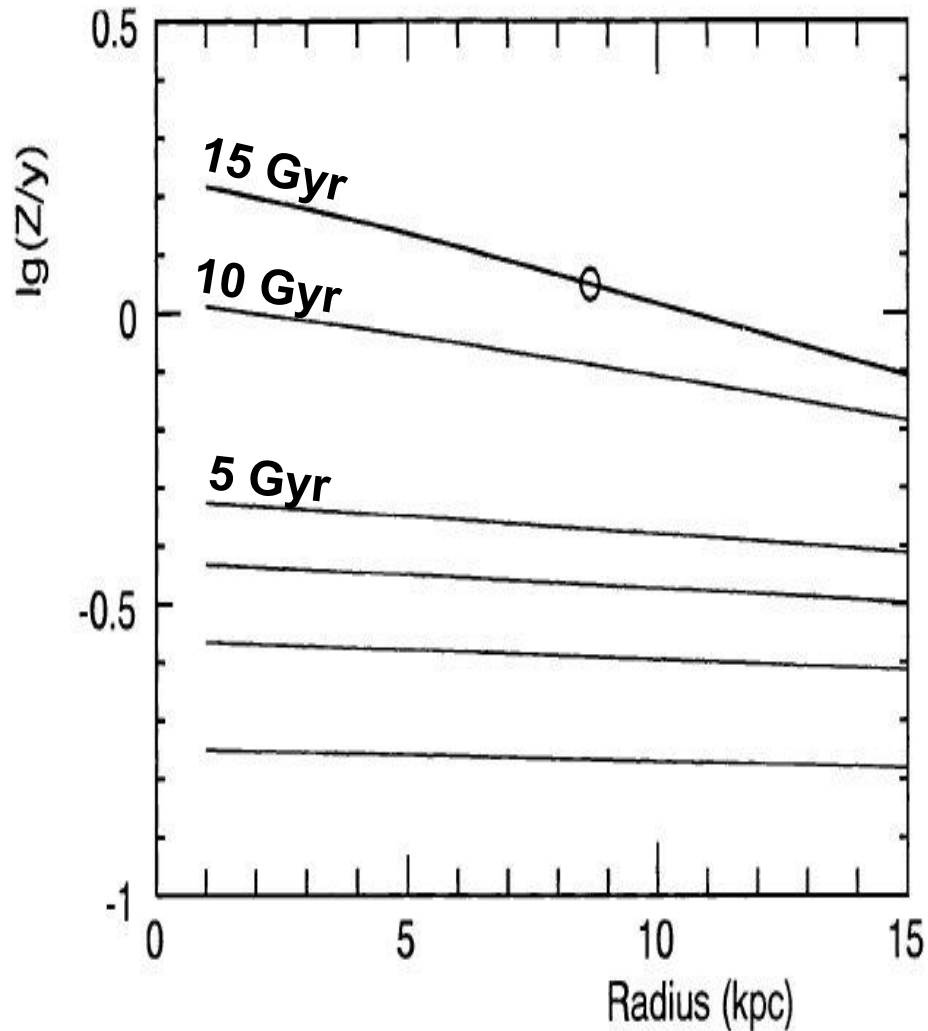
accretion metallicity gradient

radial outflows, if  $dZ/dr \neq 0$

gradients **flatten** themselves

linear SFR:

quadratic SFR:



# Gradient evolution: summary

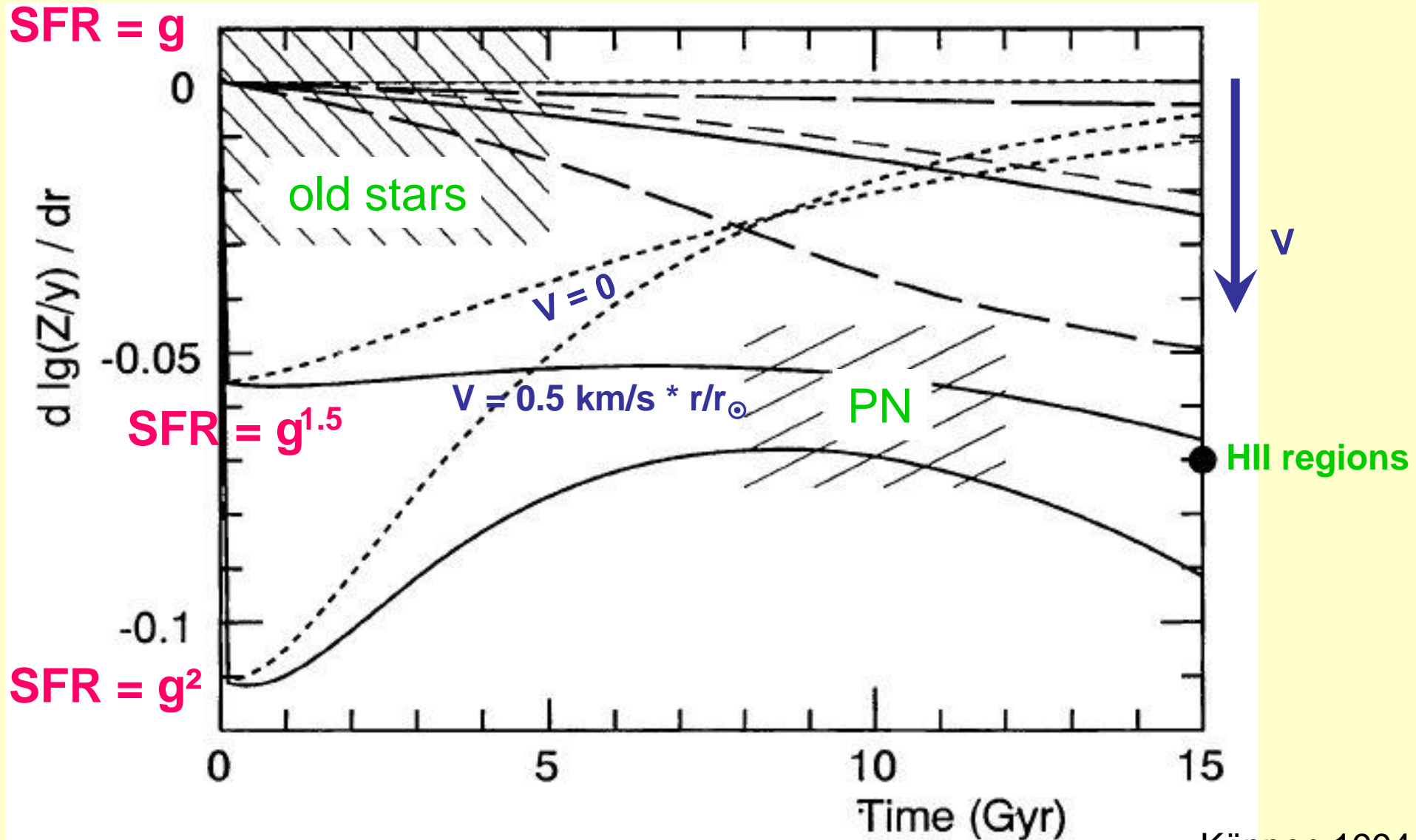
- Initial gradient by yield gradient, non-linear SFR, infall gradient:

$$d \ln Z / dr = d \ln(\alpha y \Psi/g) / dr$$

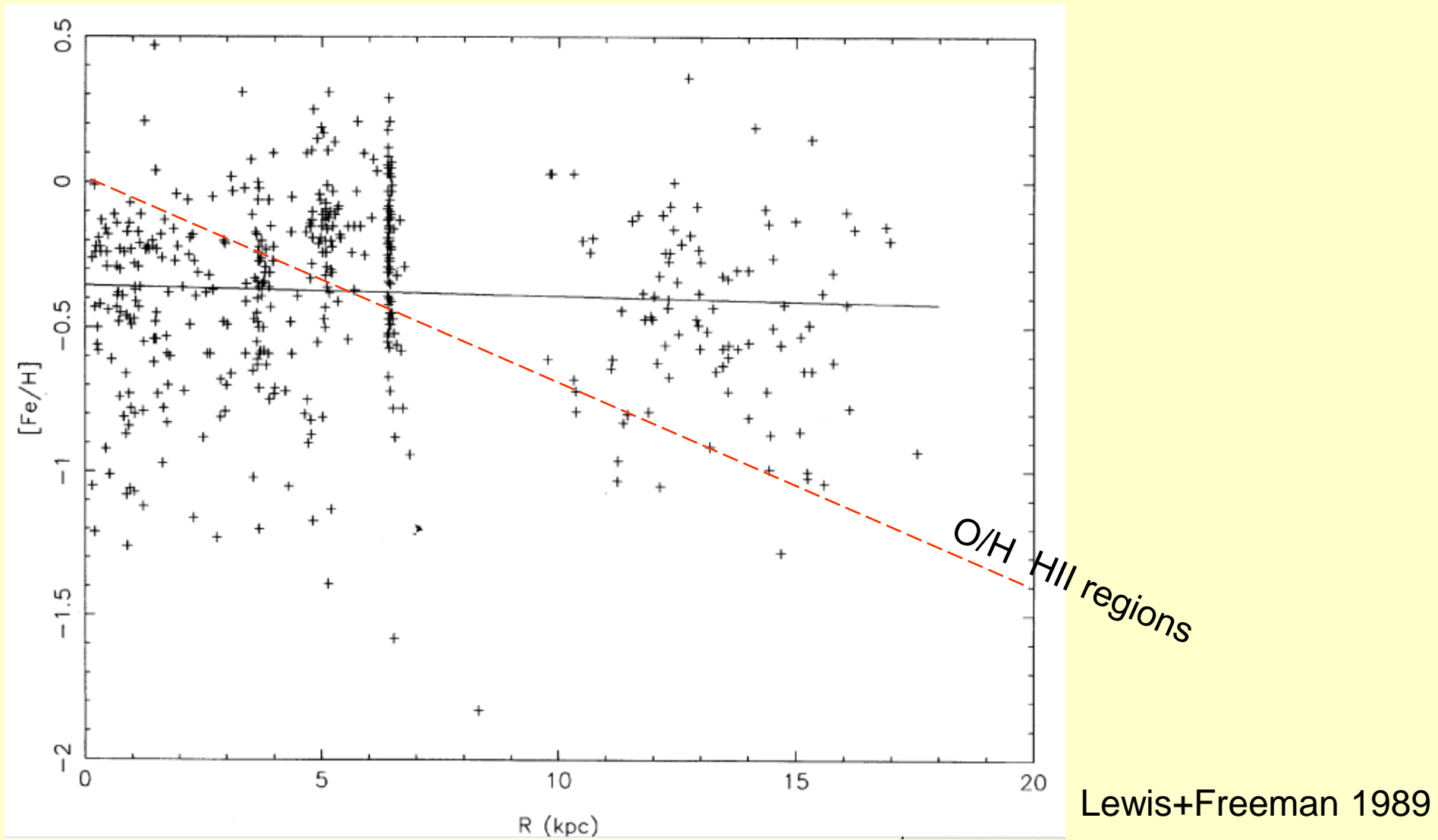
$$\{\Psi = g^n \rightarrow d \log Z / dr = -0.4343 \cdot (n-1) / r \odot\}$$

- Infall and radial flows can modify gradient in any direction
- Radial flows alone cannot make a gradient

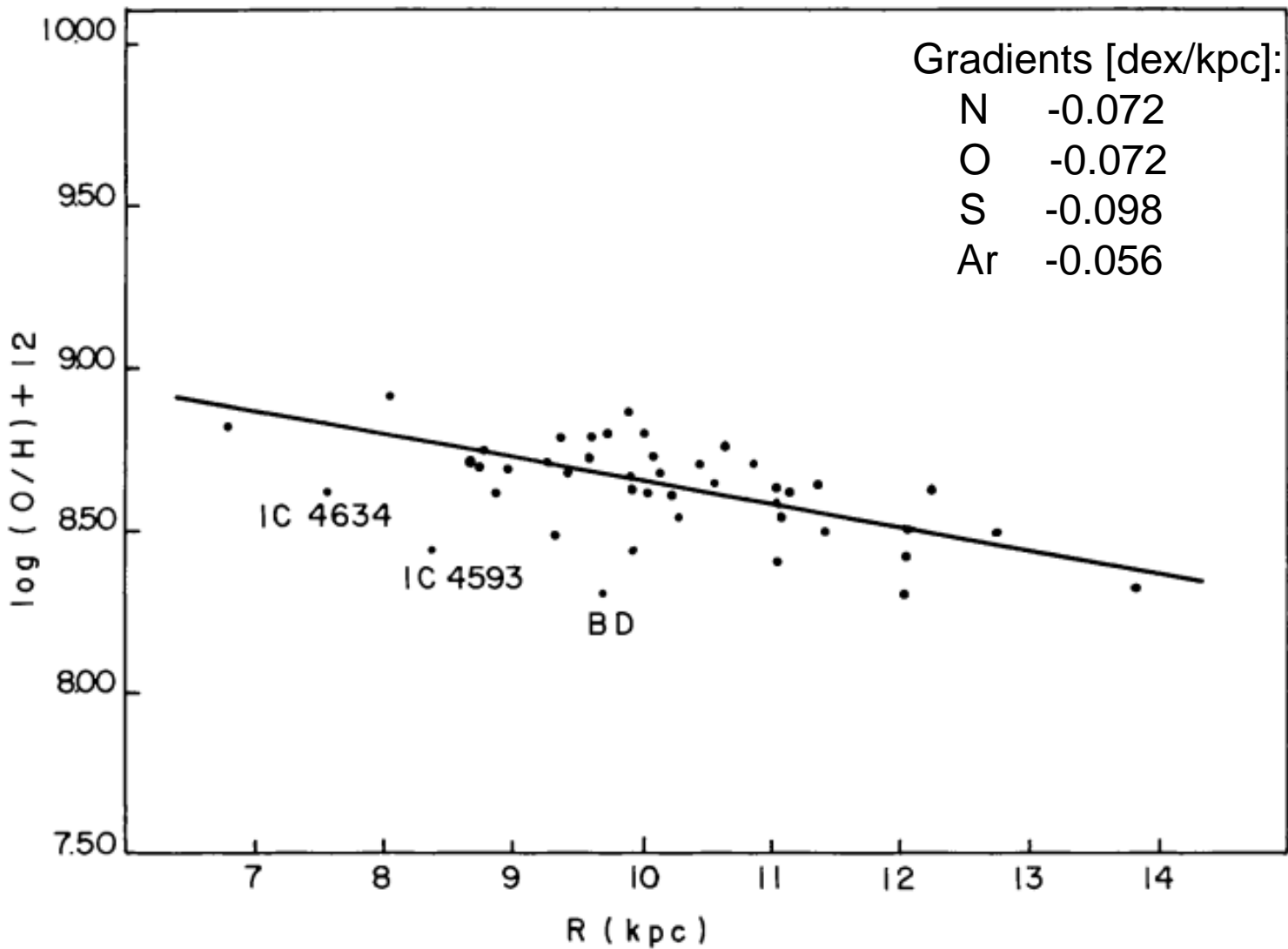
# Time evolution of gradients



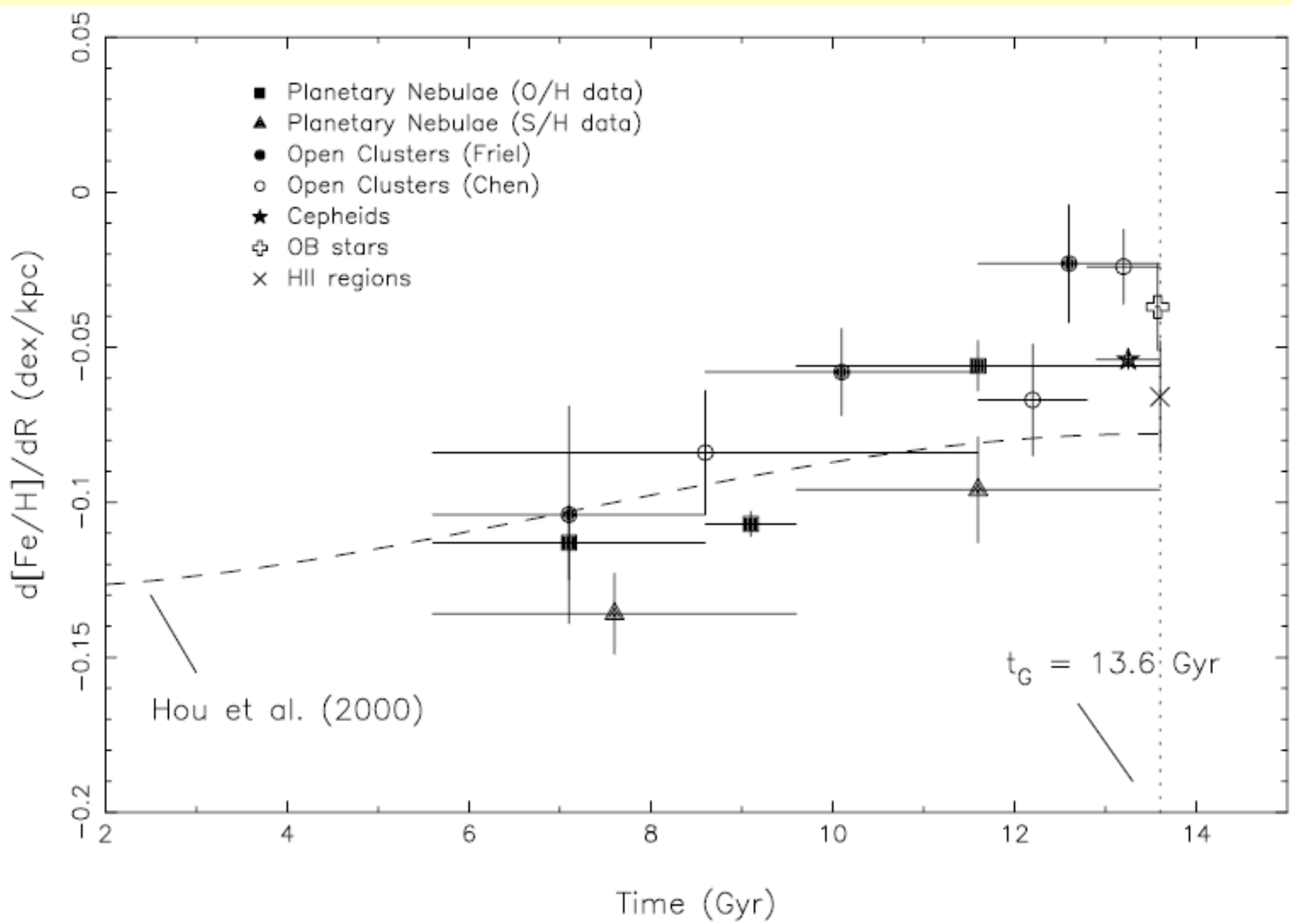
# 600 old K giants: 'no sign.slope'



# Disk Planetary Nebulae

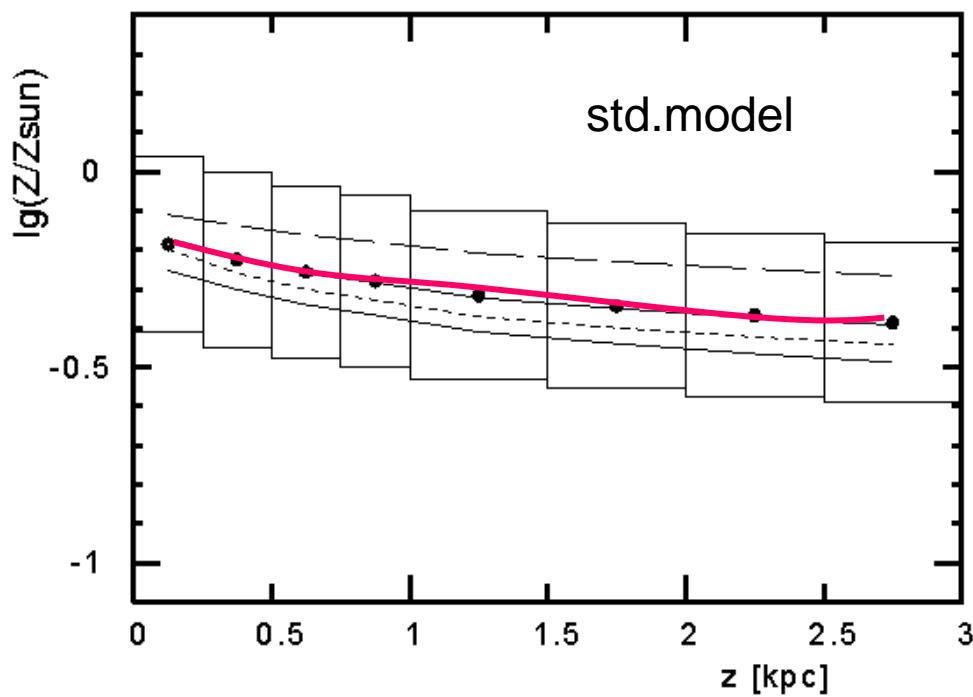
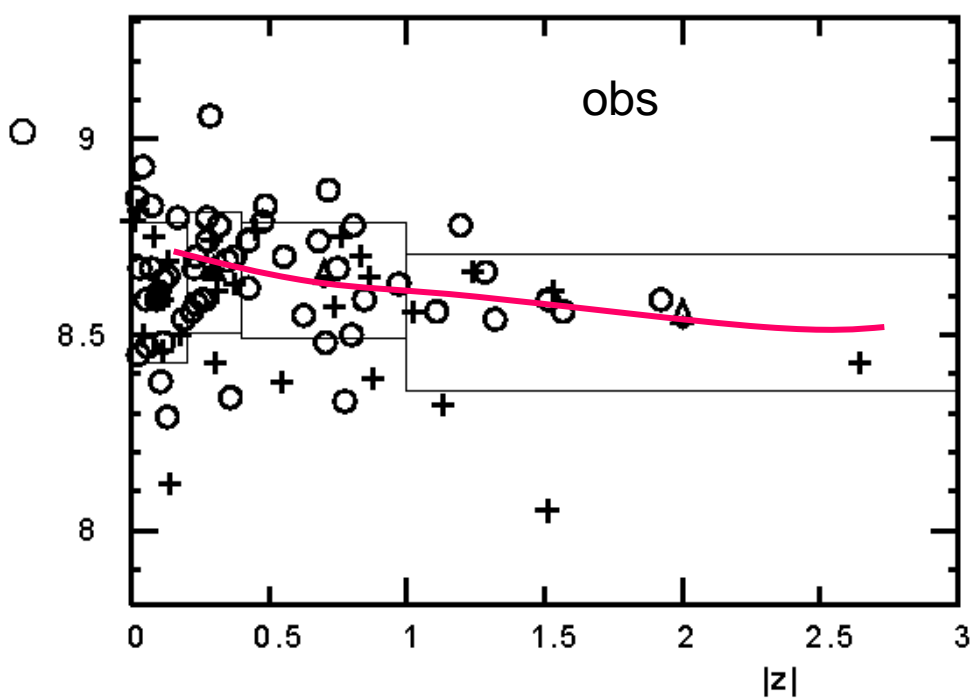




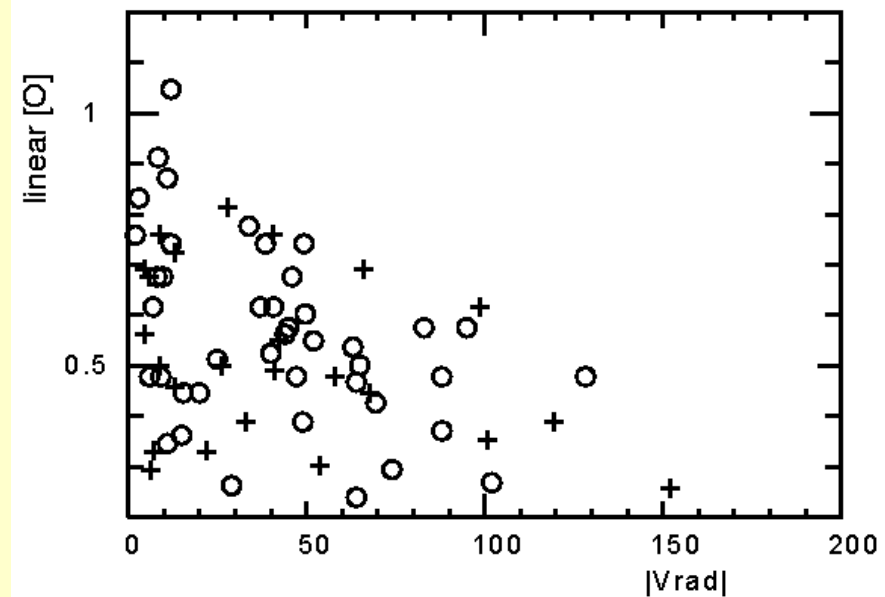


# Vertical 'gradients'

- General idea: old stars have higher vertical velocity dispersions (kinematical heating?) and thus larger mean heights above plane
- Observations with PN show **tendency** for O/H to decrease with height above plane (Cuisinier et al. 1997) in agreement with expectations from 'standard' model of kinematical heating of the disk and radial diffusion of stars



... but also:



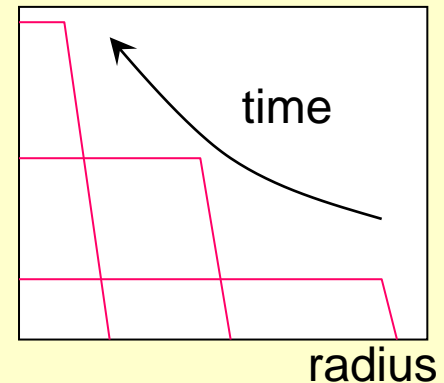
# Gradients in spheroidal systems

Observed: Radial colour (=metallicity) gradients  
Detailed character varies widely

Interest: monolithic collapse (more later)

→ Lynden-Bell's concentration model

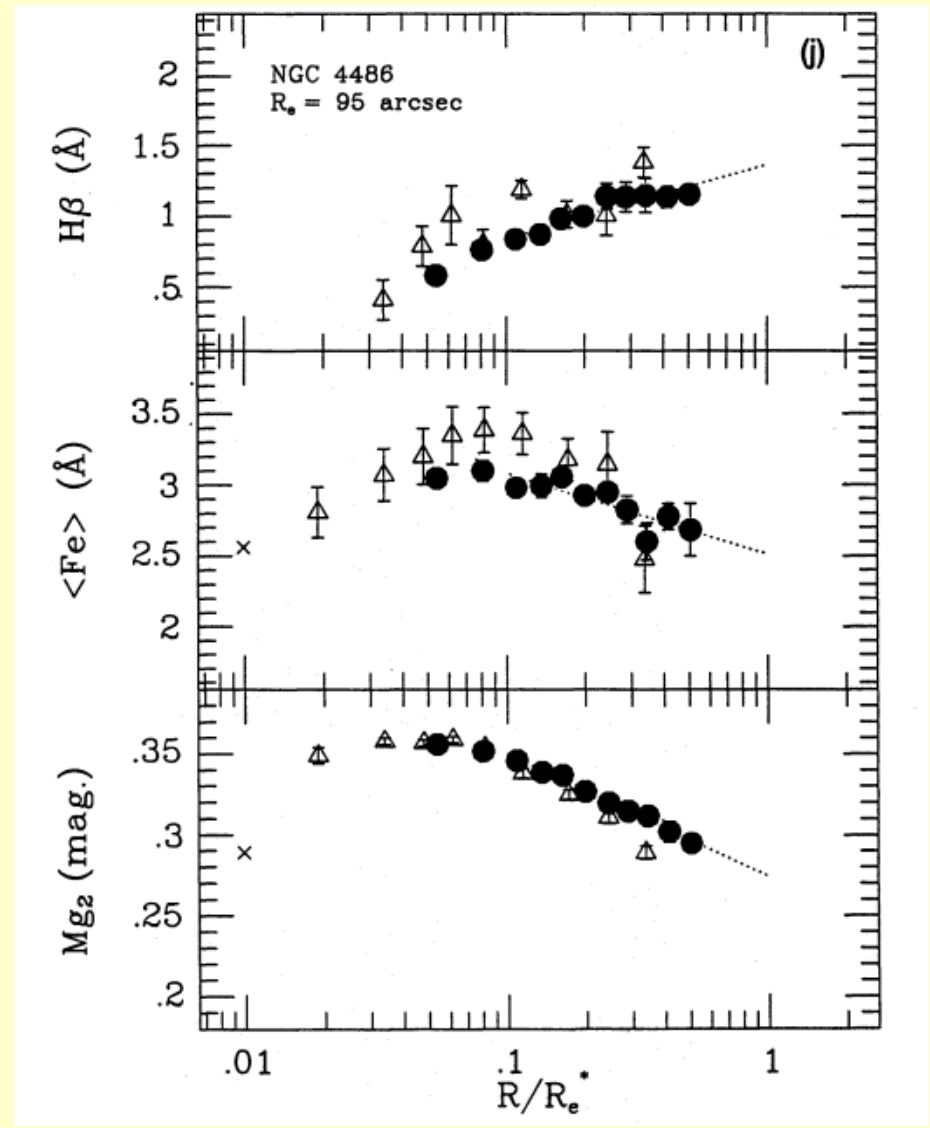
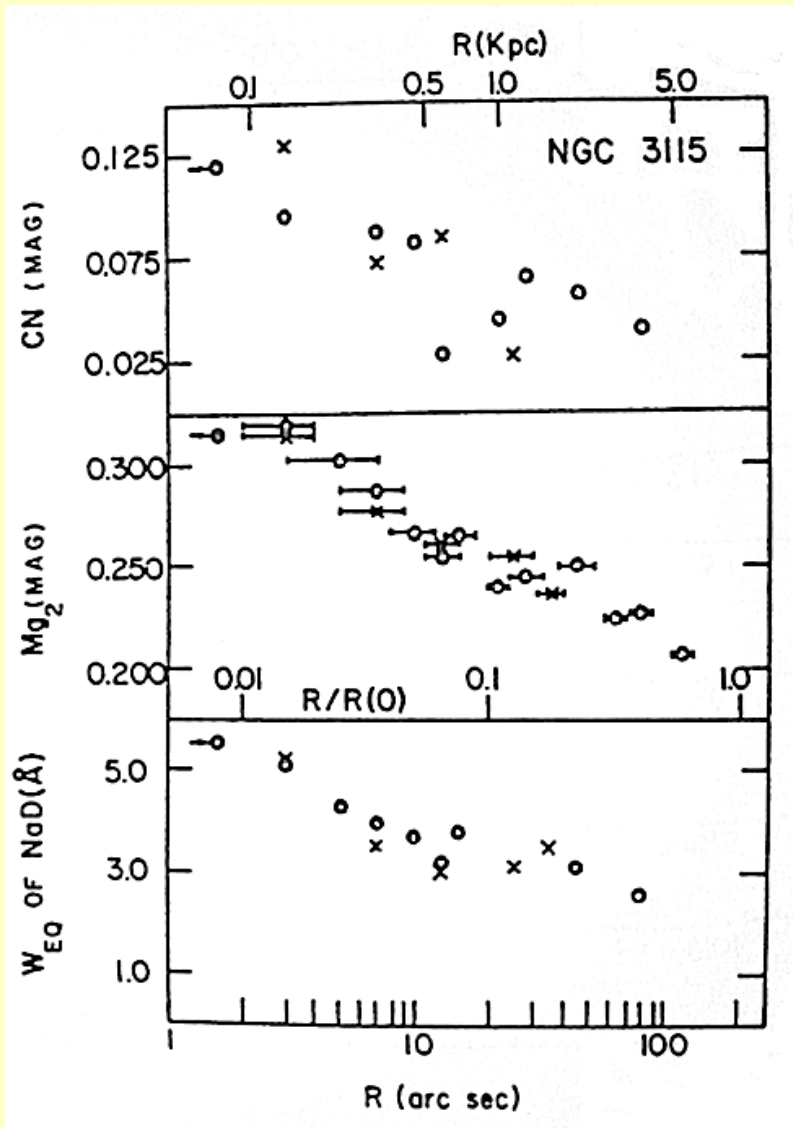
→ does it work?



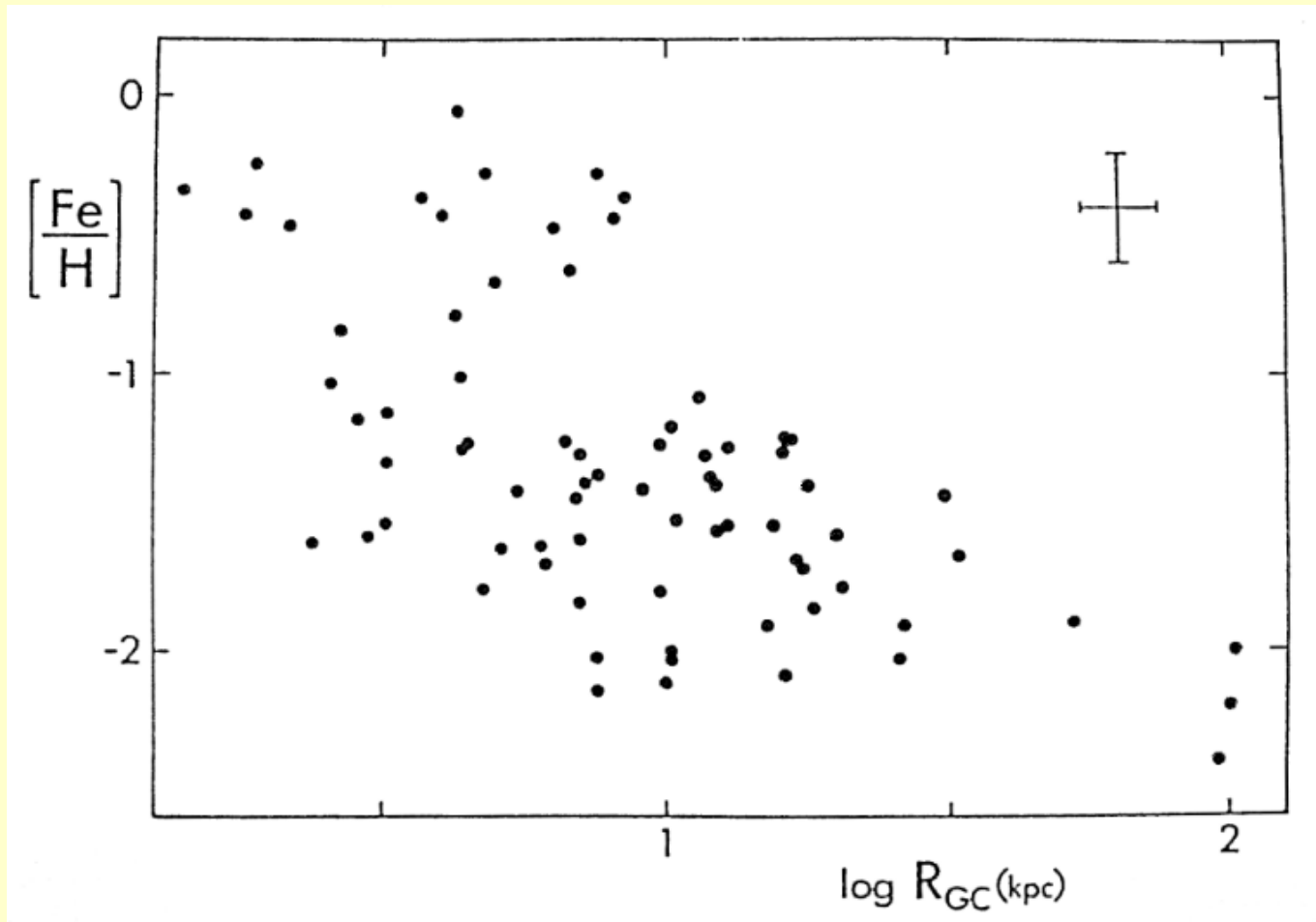
## Difficulties

- deprojection
  - assume geometry
  - not possible for individual objects → large data sets
- stars: mixture of ages

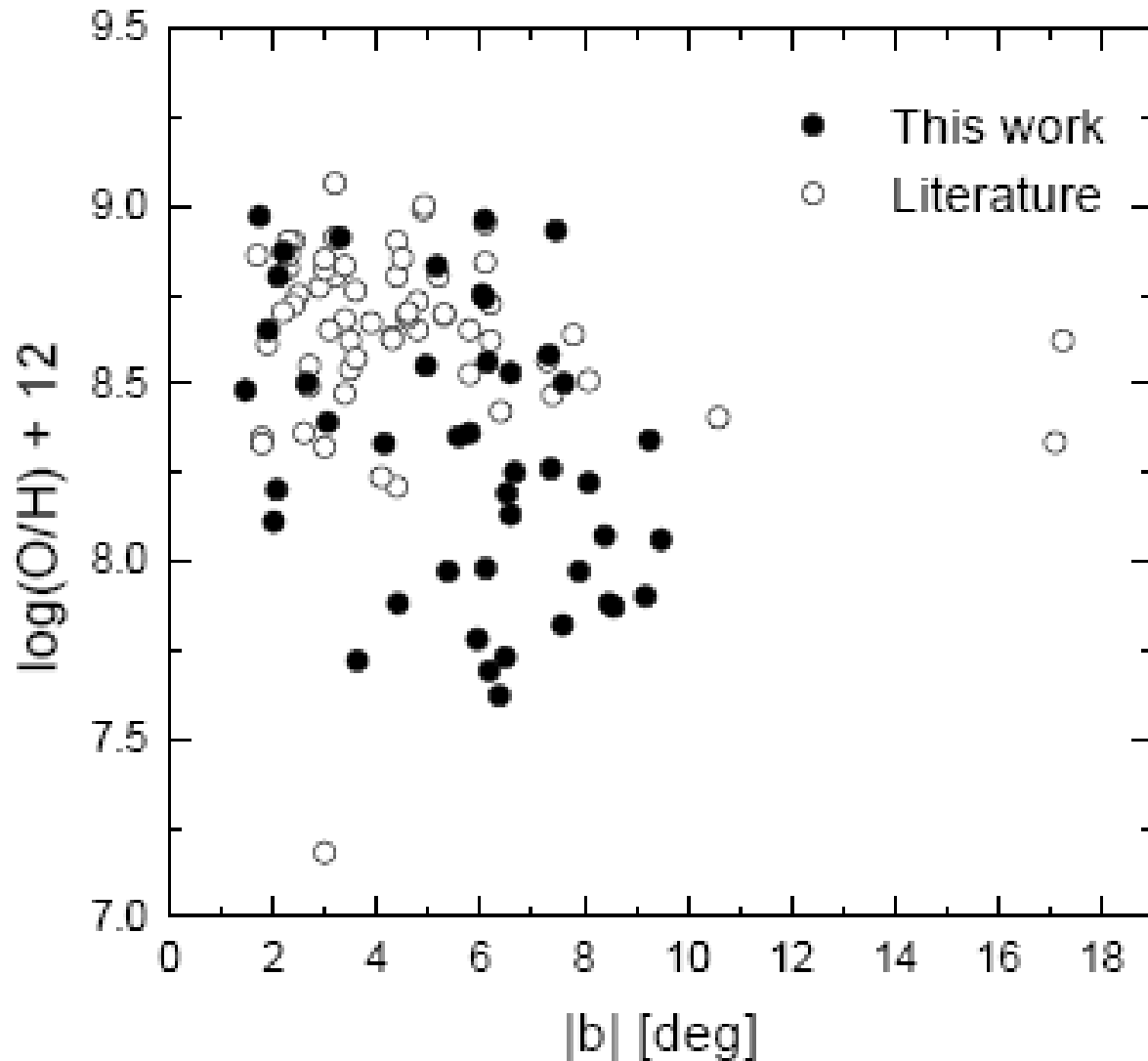
# Gradients of photometric indices in Ellipticals



# Galactic Globular Cluster System



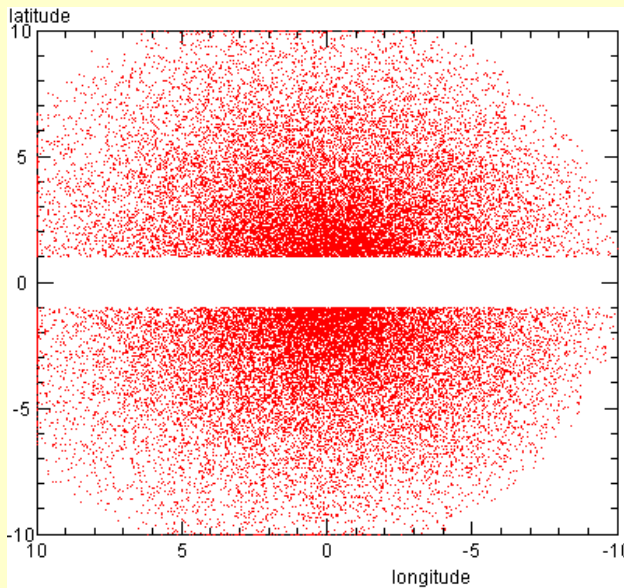
# Galactic Bulge with PN



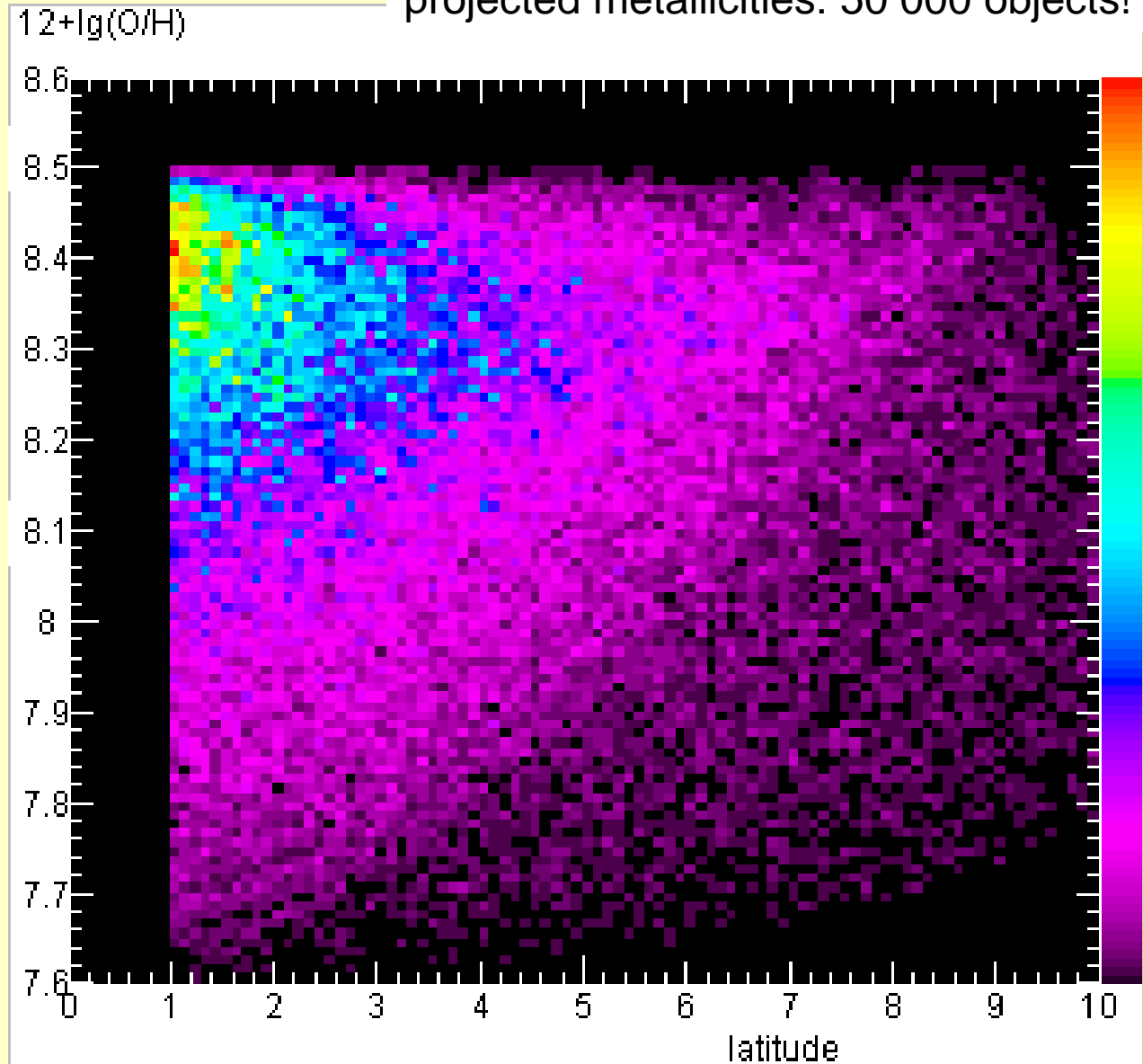
Gradient?

# ... but it's tough!

Simulation: assume  
spheroidal bulge  
radial abundance gradient



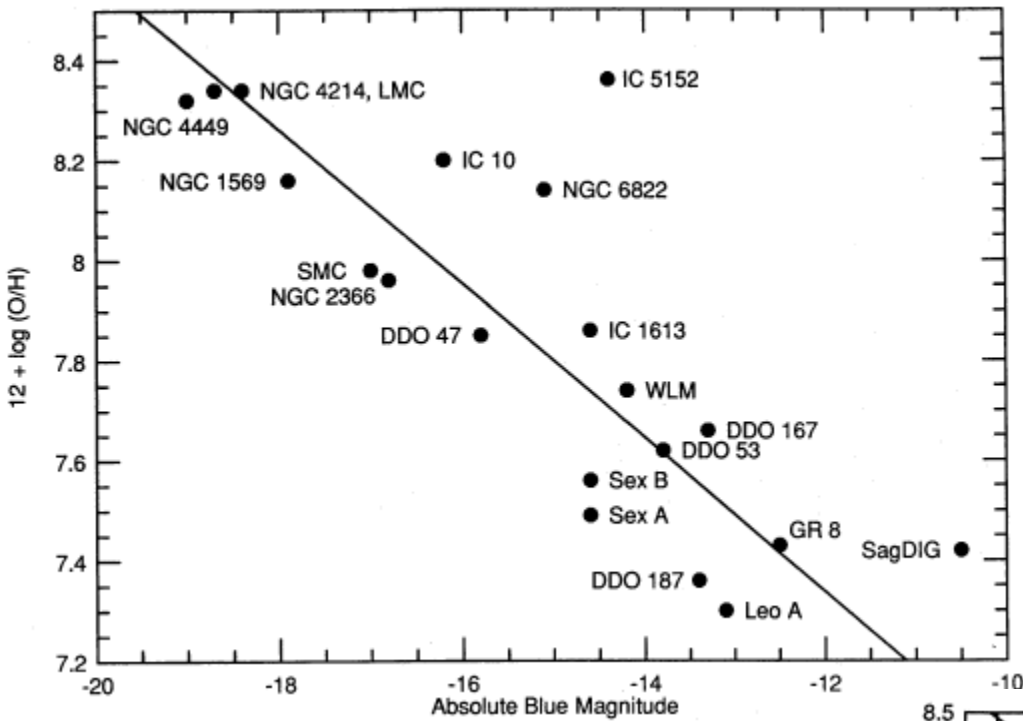
projected metallicities: 50 000 objects!



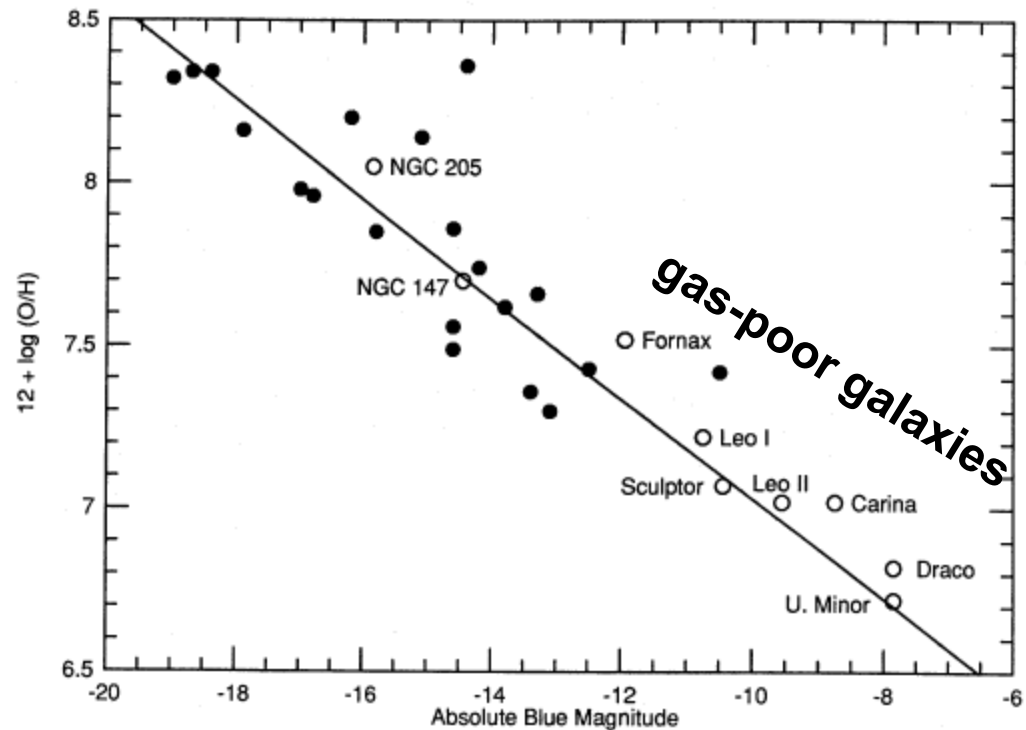




# Mass-Metallicity Relation in galaxies

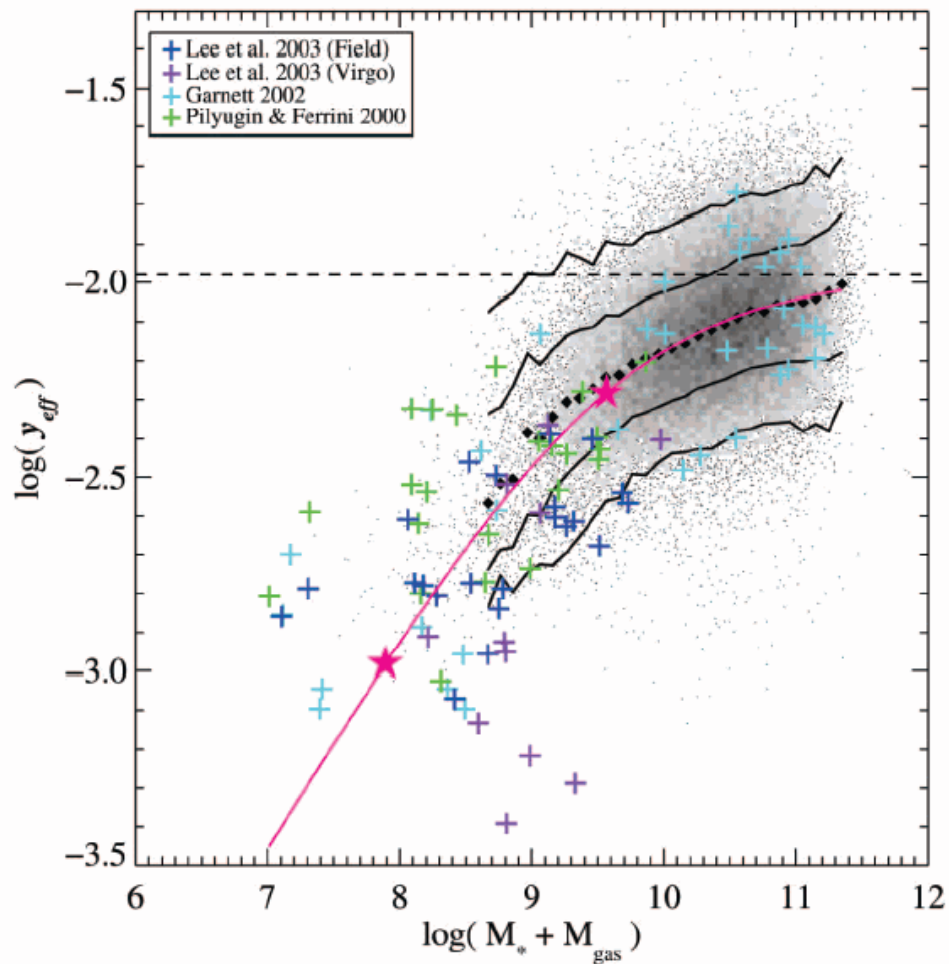
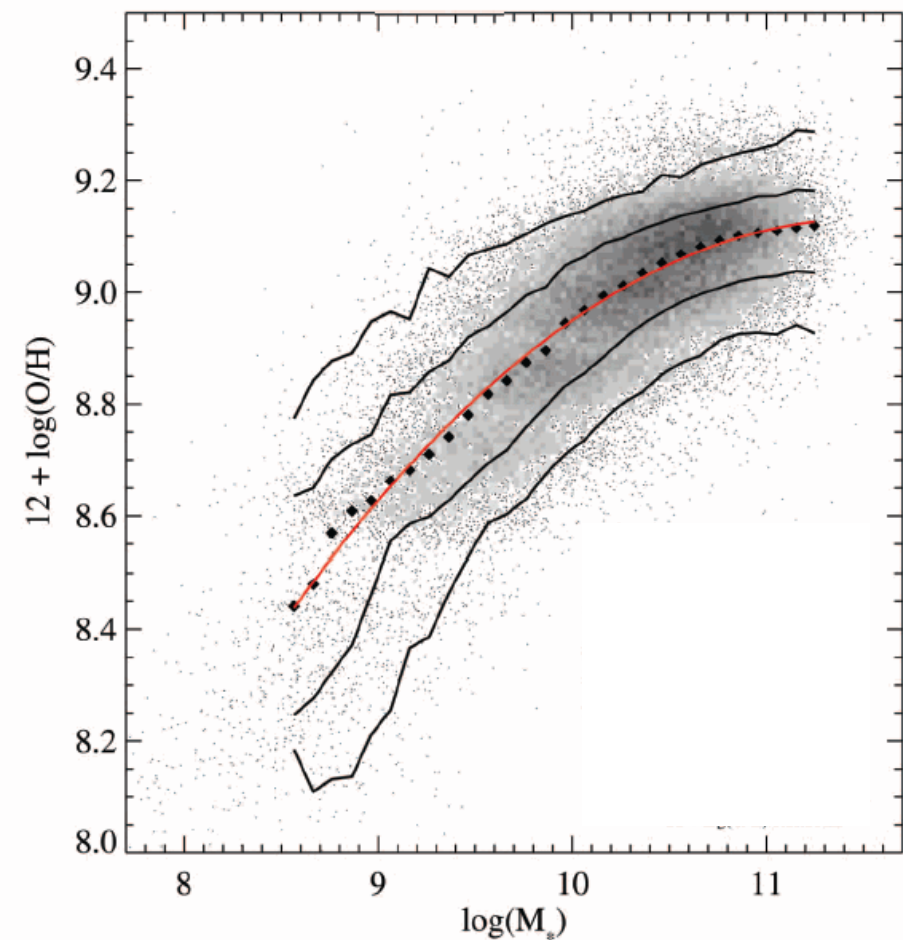


gas-rich galaxies



# SDSS data

53 000 galaxies



# Origins of Mass-Metallicity Relation

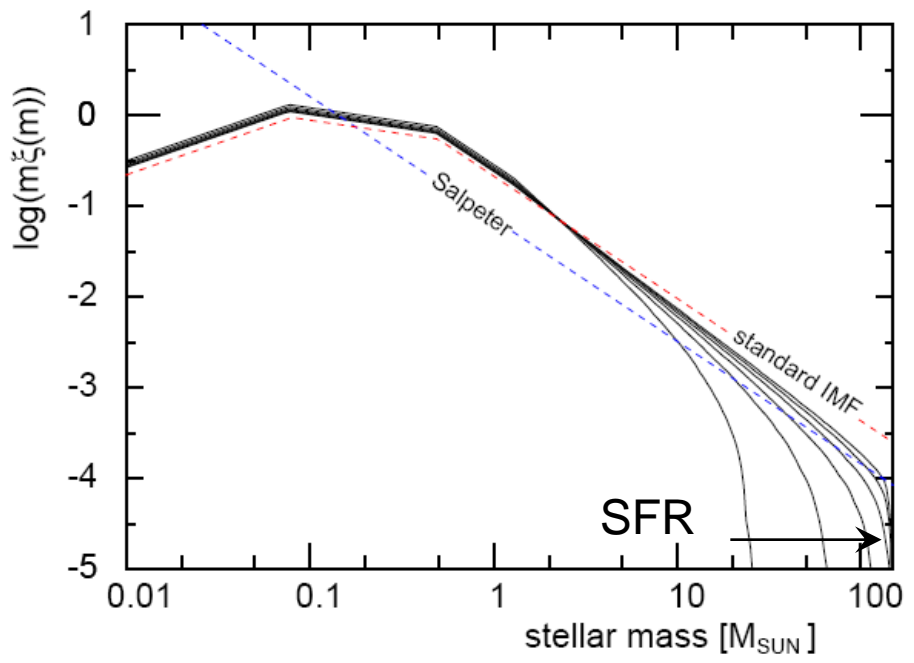
## Less massive galaxies

- are chemically less evolved (i.e. higher gas fractions)
  - have lower SFR
  - have shorter lifetime (or time of essential SF)
- have lower (effective) yields
  - cannot keep all their metals in gravitational well:

$$y_{\text{eff}} = \frac{y_0}{1 + (M_0/M_{\text{baryon}})^{0.57}}$$

Tremonti et al. 2004

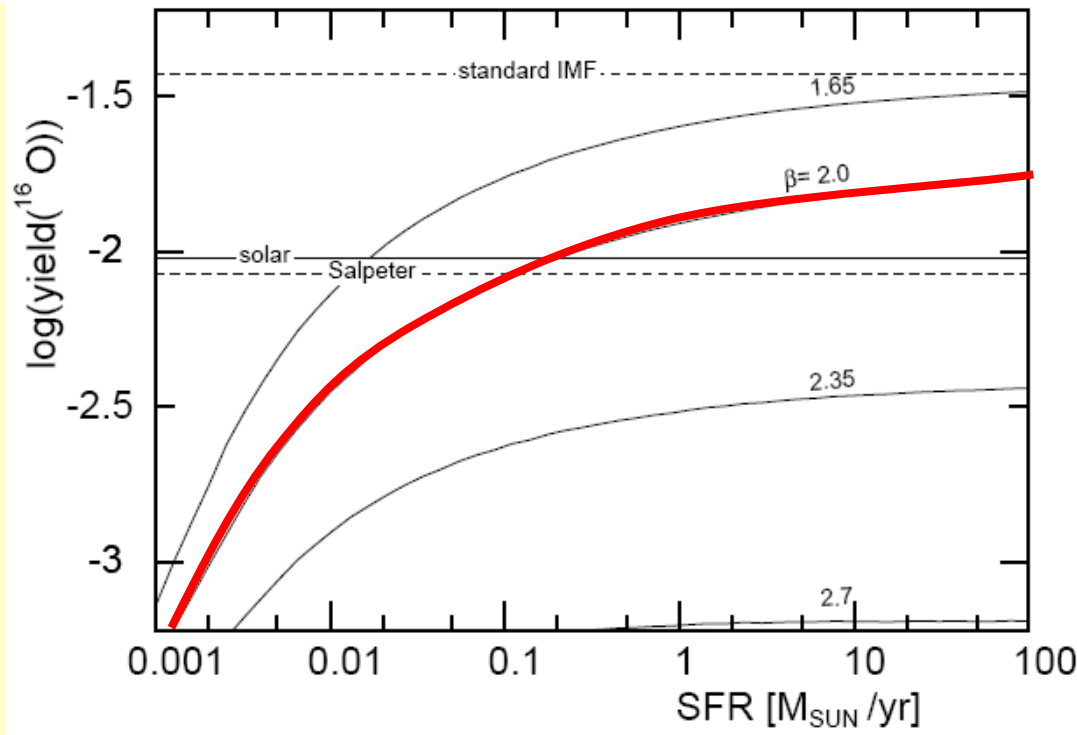
- IMF has fewer massive stars in low-SFR environments



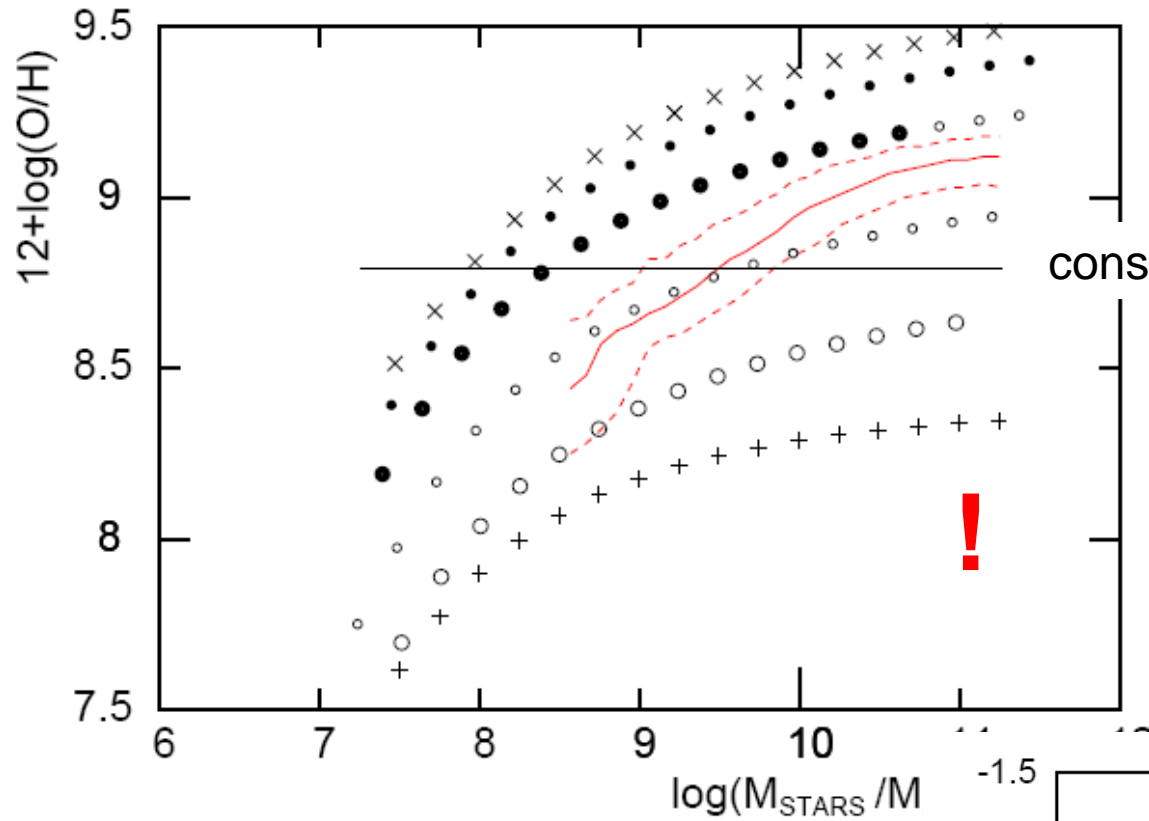
## Variable IMF:

In a high-SFR environment, the newly formed star cluster contains a larger fraction of massive stars

Weidner & Kroupa 2004ff



Köppen, Weidner, Kroupa 2007



Just a  
closed  
box model

