

# Exoplanetary Atmospheres: Theory & Simulation



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*Review Talk at University of Kiel Workshop 2014*

**u<sup>b</sup>**

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**EXOPLANETS  
& EXOCLIMES  
GROUP**

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# General Questions

## (Theory)

What are the **processes** governing the **atmospheric dynamics**, **chemistry** and **radiative transfer** of exoplanetary atmospheres?

What are the obstacles and degeneracies associated with **interpreting transmission** (transit) and **emission** (secondary eclipse) **spectra** and **phase curves** of exoplanetary atmospheres?

What lessons can we learn from the **Solar System**?  
(Can the techniques be borrowed without modification?)

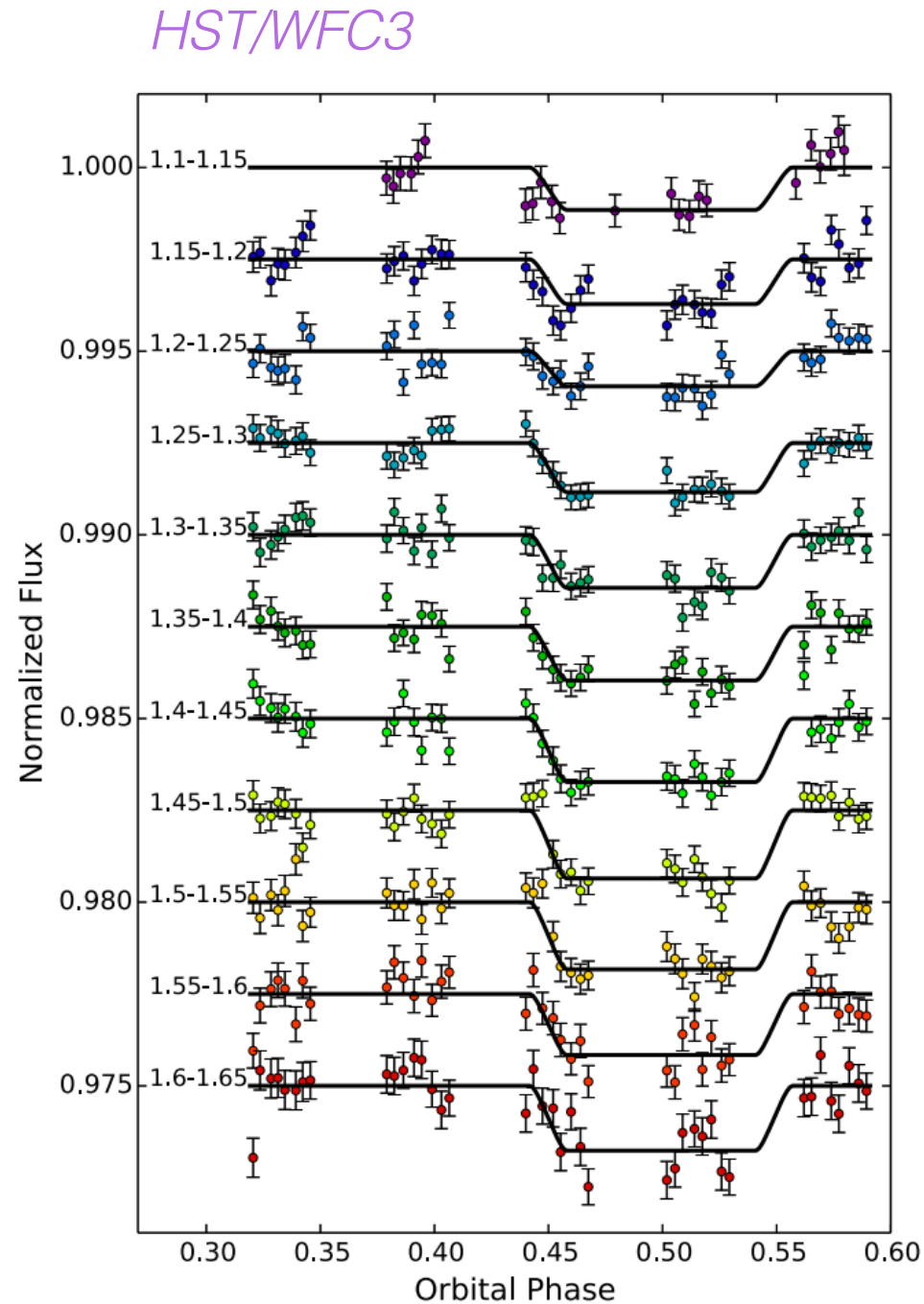
# Agenda

- I. Brief tour of observations
- II. Theory
- III. Simulations

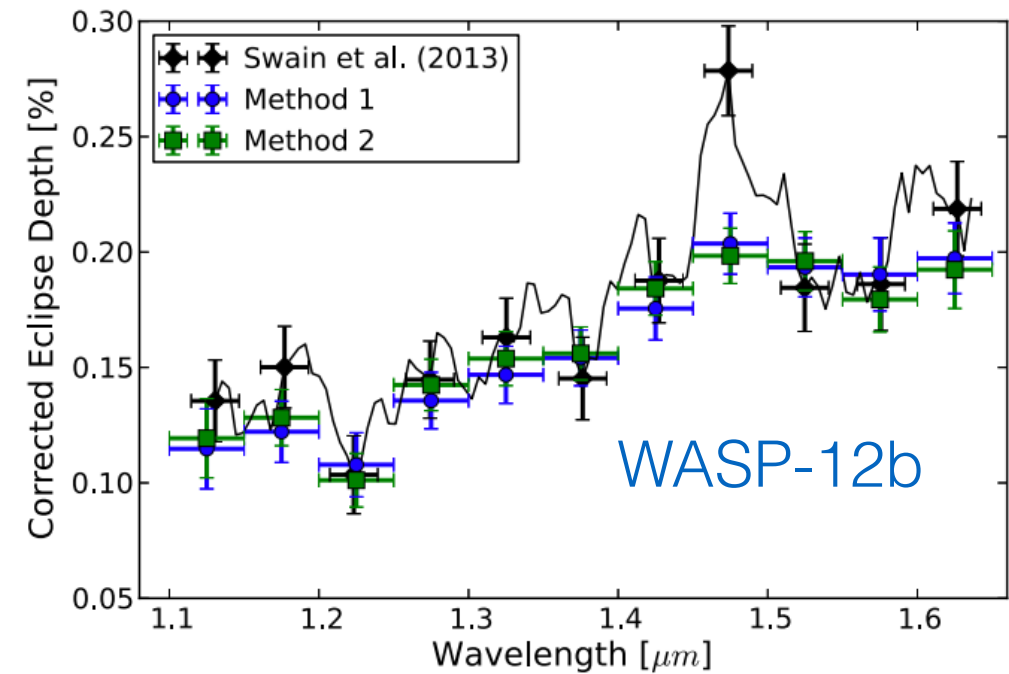
# **I. Brief Tour of Observations**



# Spectro-photometry: emission spectrum



Note: these are secondary eclipses  
(exoplanet's light is obscured by star)

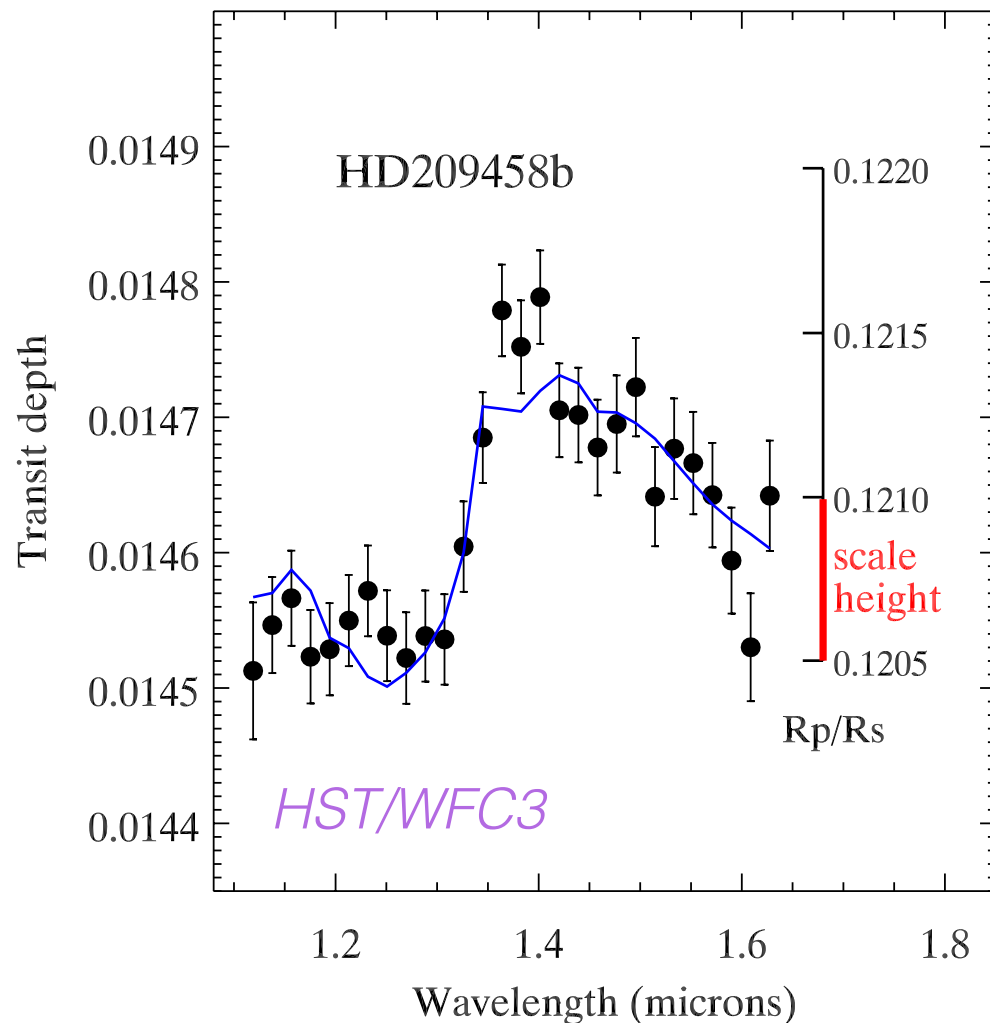


**Figure 5.** WASP-12b corrected emission spectrum using WFC3's G141 grism. Both methods used in our analyses (blue circles and green squares) agree with the results from Swain et al. (2013, black line with diamonds for comparison) in all but one of the spectroscopic channels.

Abundances of major molecules  
(CO, CH<sub>4</sub>, H<sub>2</sub>O, CO<sub>2</sub>) may be inferred  
using inversion techniques, albeit  
currently with some controversy.

# Spectro-photometry: transmission spectra

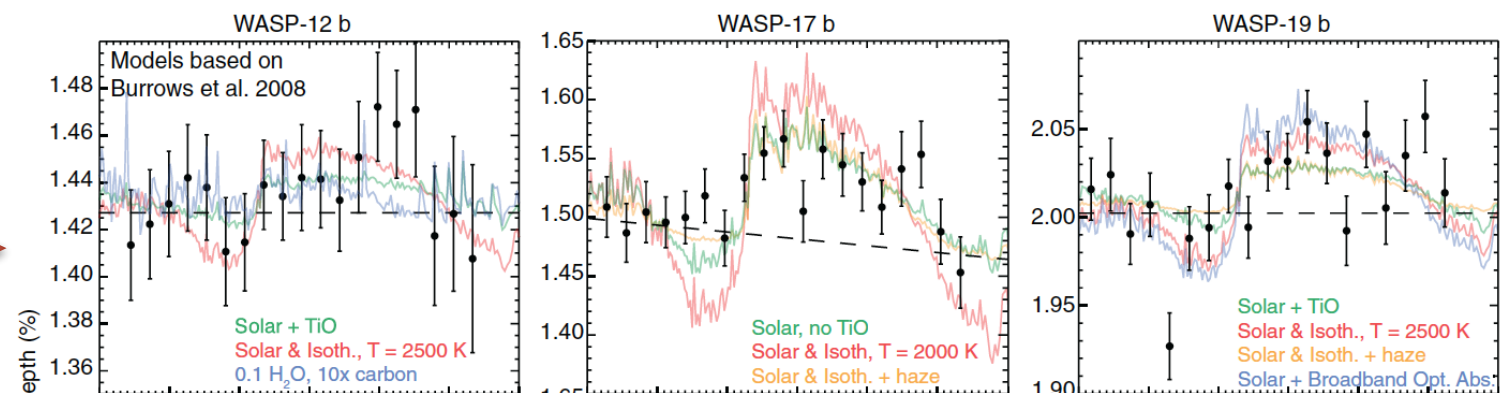
Deming et al. (2013, ApJ, 774, 95)



unambiguous detection  
of water feature

The observations are consistent  
with a degenerate range of models  
(cloud-free, cloudy, different chemistries)

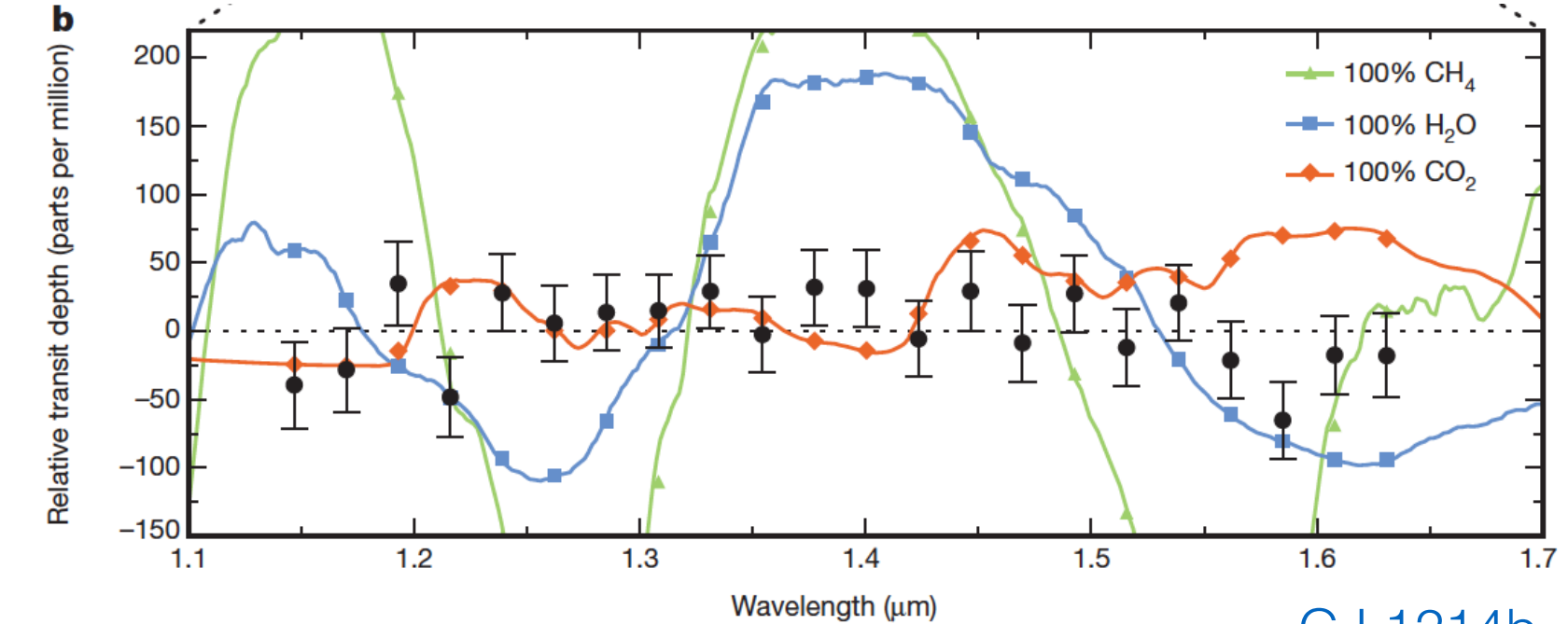
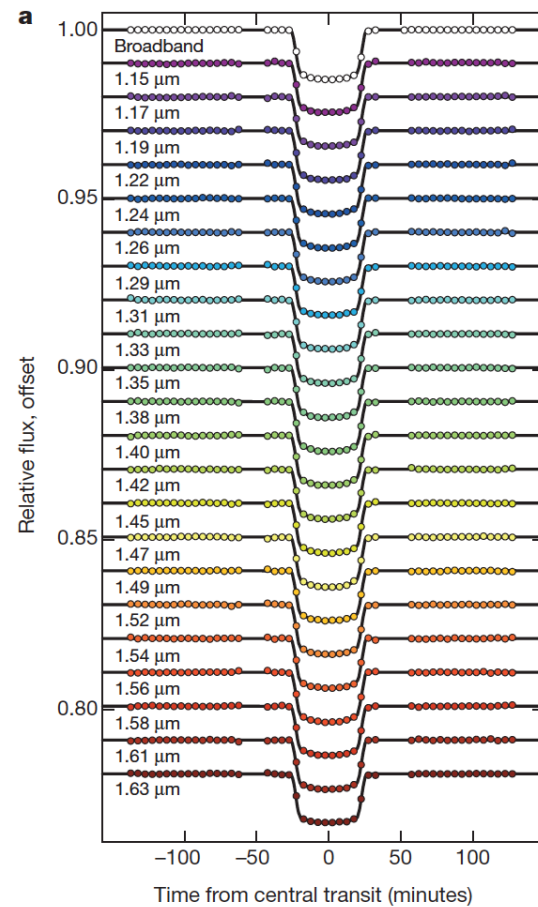
spectra muted  
by clouds?



HST/WFC3

Mandell et al. (2013, ApJ, 779, 128)

# More transmission spectra: flat lines



*HST/WFC3*

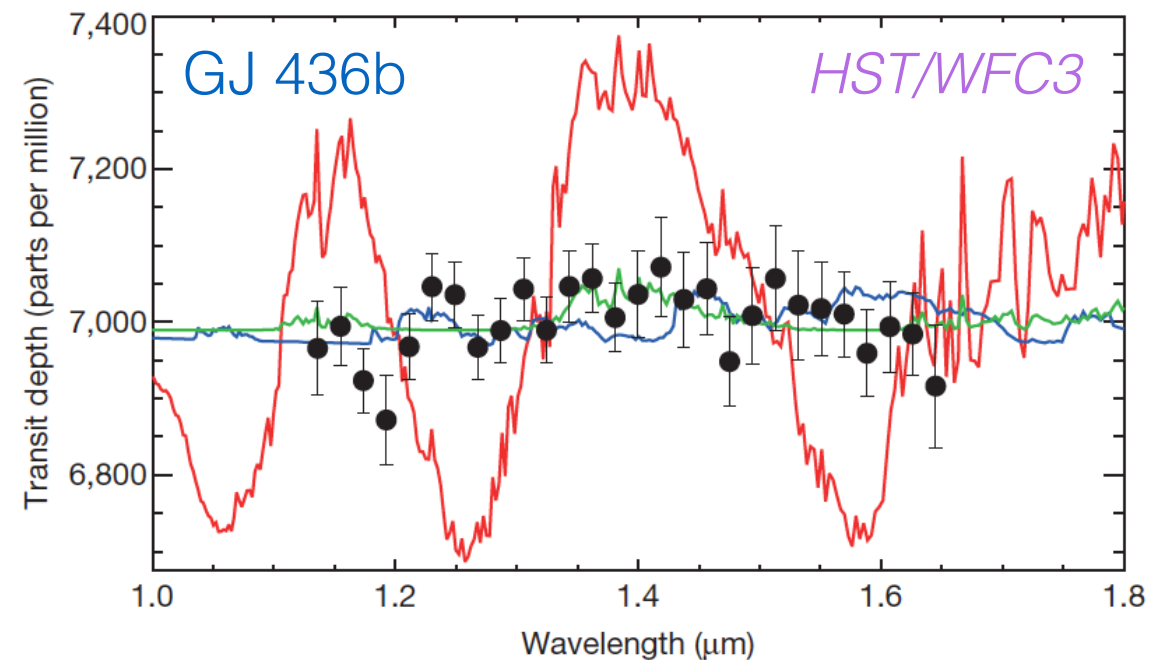
*Kreidberg et al. (2014, Nature, 505, 69)*

GJ 1214b

Cloud-free hydrogen-rich  
atmospheres are ruled out.

Cloudy or metal-rich?

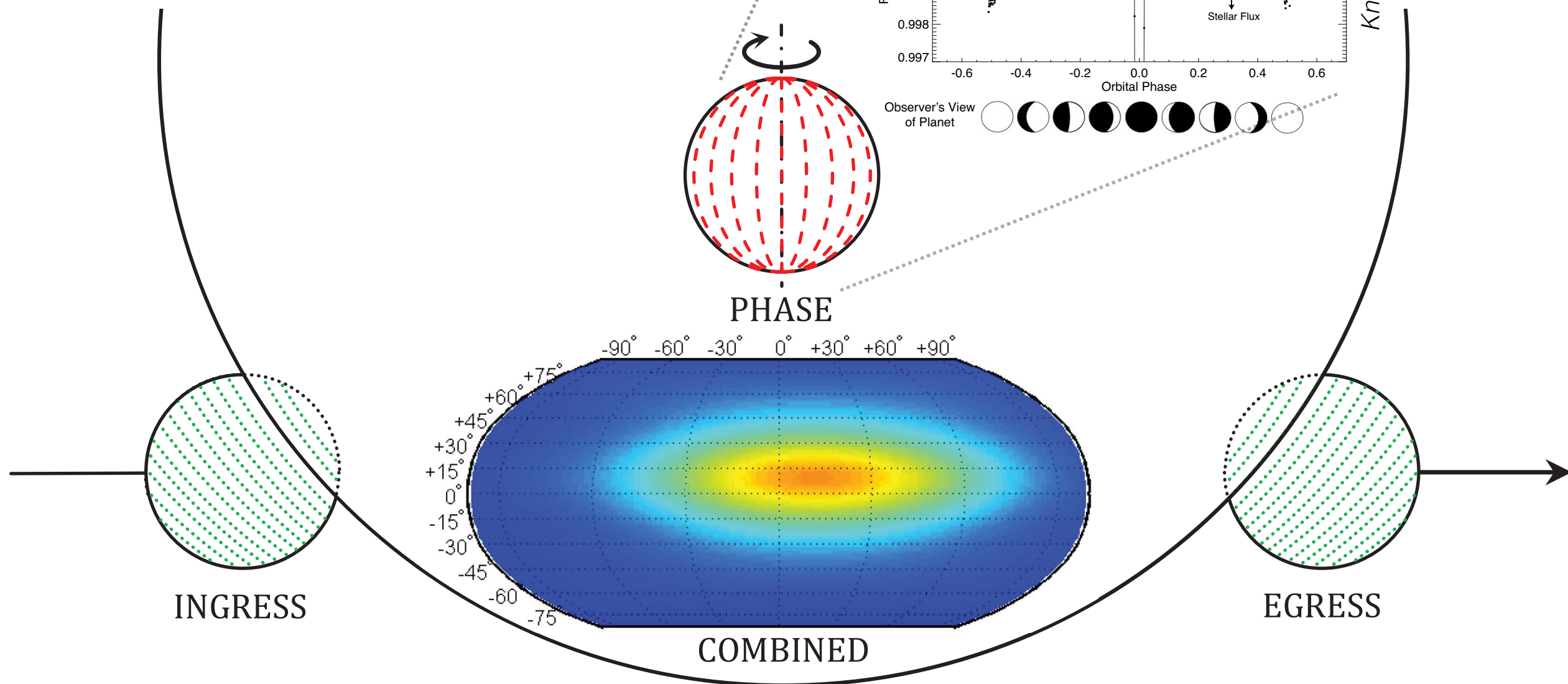
(Or atmosphere-less?)



*Knutson et al. (2014, Nature, 505, 66)*

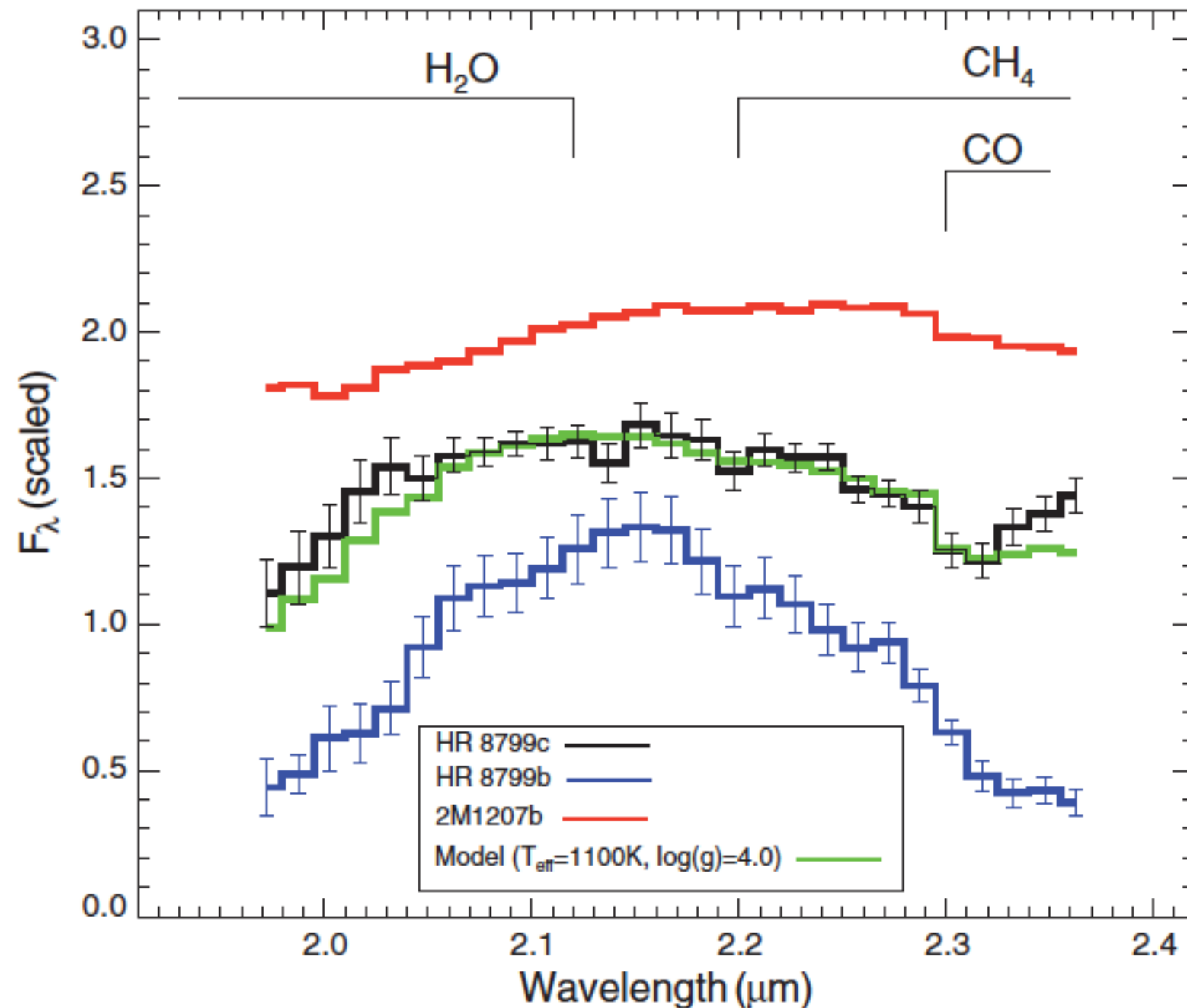
# Eclipse mapping

Multi-dimensional data to validate 2D and 3D models?

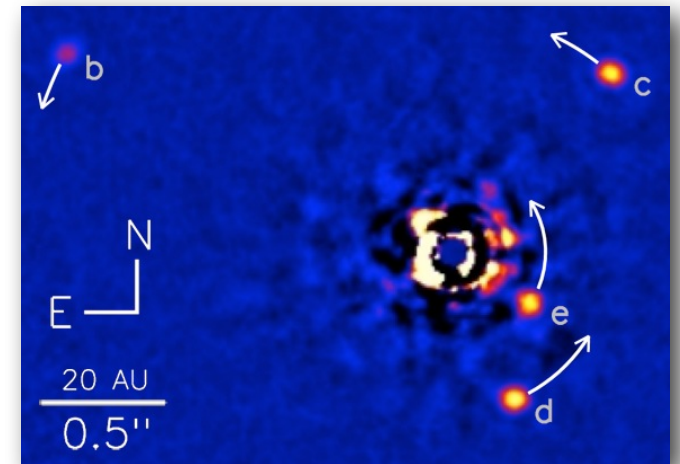




# Directly imaged exoplanets



HR 8799a,b,c,d



R~100-1000 spectra  
exist for a small  
number of objects.

But these objects  
have no radius  
or mass measurements.

## **II. Theory**

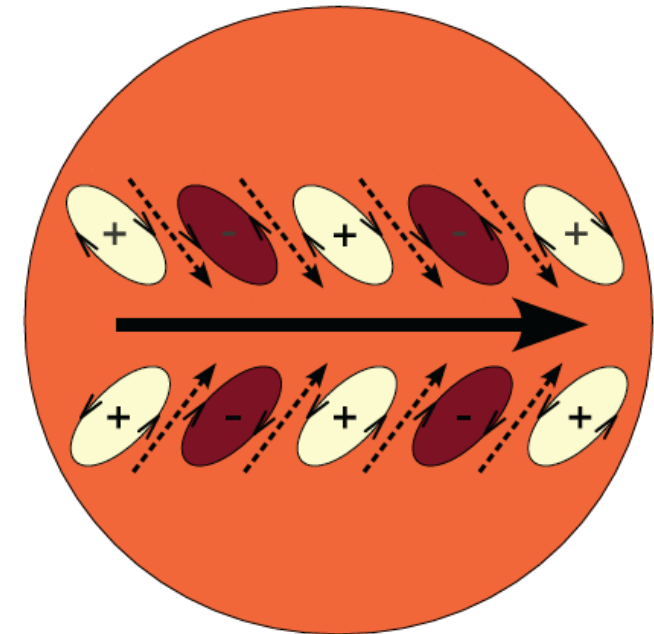
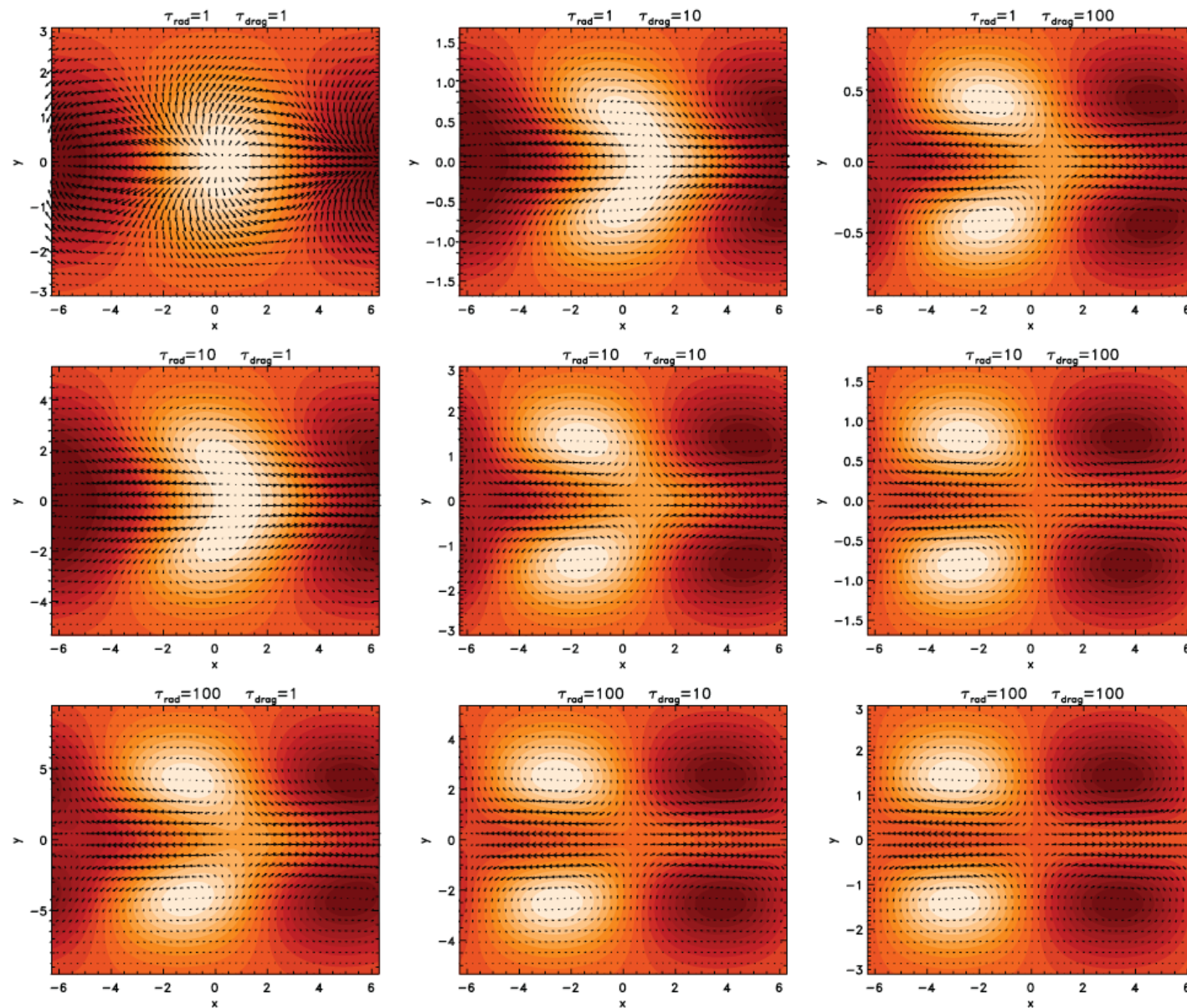
# What may we learn from the Solar System?

All of the current characterisable exoplanets are hot ( $\sim 800\text{-}3000\text{ K}$ ).

Solar System	Hot Exoplanets	Implications
stellar and interior flux comparable	stellar flux dominates (by factor $\sim 10,000$ )	thermal and dynamical structures
fast rotators	slow rotators (indirect arguments)	dynamical structure
small Rossby scale	large Rossby scale	size of vortices
small Rhines scale	large Rhines scale	width of zonal jets
in-situ measurements (some ground truth)	remote sensing (rely on physics)	consider chemical, radiative and dynamical equilibrium carefully

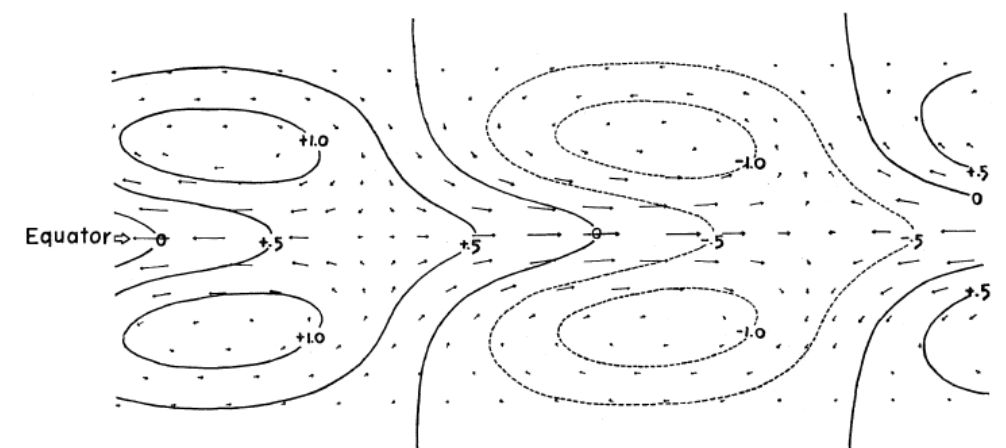
Bottom line: it does not mean we cannot benefit from SS knowledge.  
It just means we have to tread carefully...

# Atmospheric dynamics: an example where the Earth sciences taught us some physics



Super-rotation:  
angular momentum transport  
by standing Rossby and Kelvin waves

super-rotation appears to be robust  
to different applications of friction/drag



*inspired by Matsuno (1966)*  
*See also: Gill (1980)*



# And where we could give something back (MHD shallow water waves)

**The key governing equation for MHD systems and the quantum harmonic oscillator are identical, even when forcing, sources of friction and magnetic fields are considered.**

## **Challenges:**

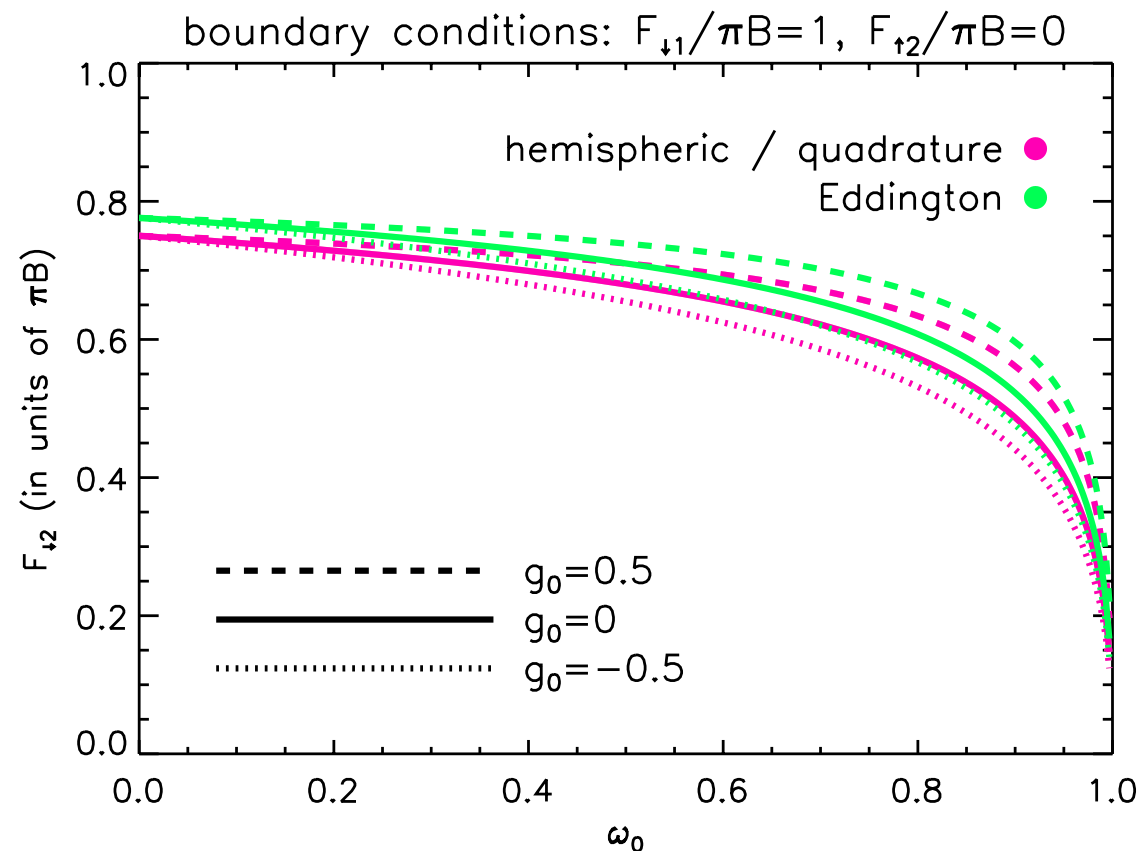
ODEs with complex coefficients raised to fractional powers (double-valued), have to use De Moivre's formula

non-oscillator behaviour (poloidal magnetic field, non-uniform drag)

*Heng & Workman (2014, ApJS, 213, 27)*

# Two-stream radiative transfer: when standard approaches are not so standard

emergent flux



Easier to solve moments of the radiative transfer equation, but there is always one more unknown than number of equations.

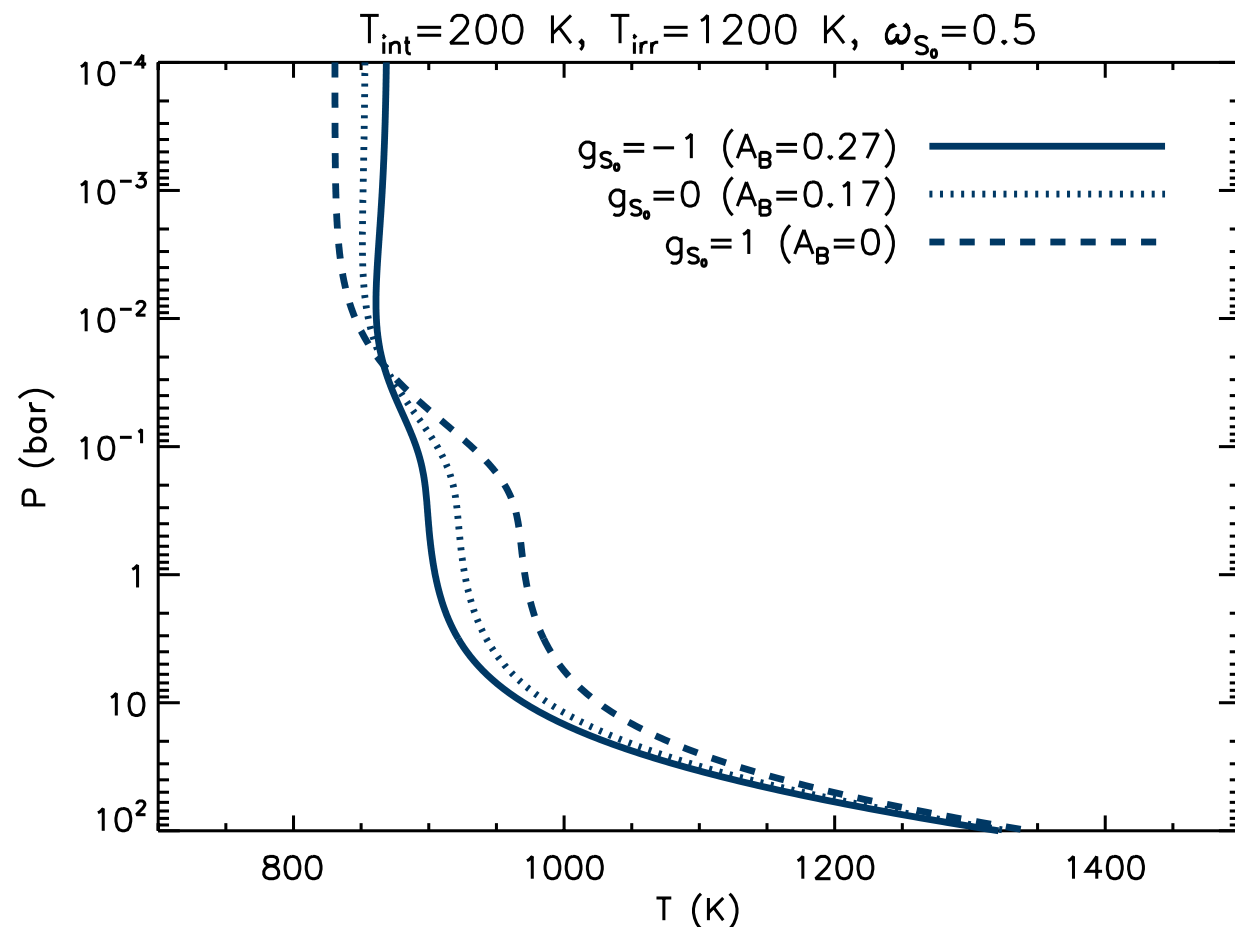
Need to “close” the set of equations (Eddington coefficients).

Choice of closure is intimately related to general energy conservation.

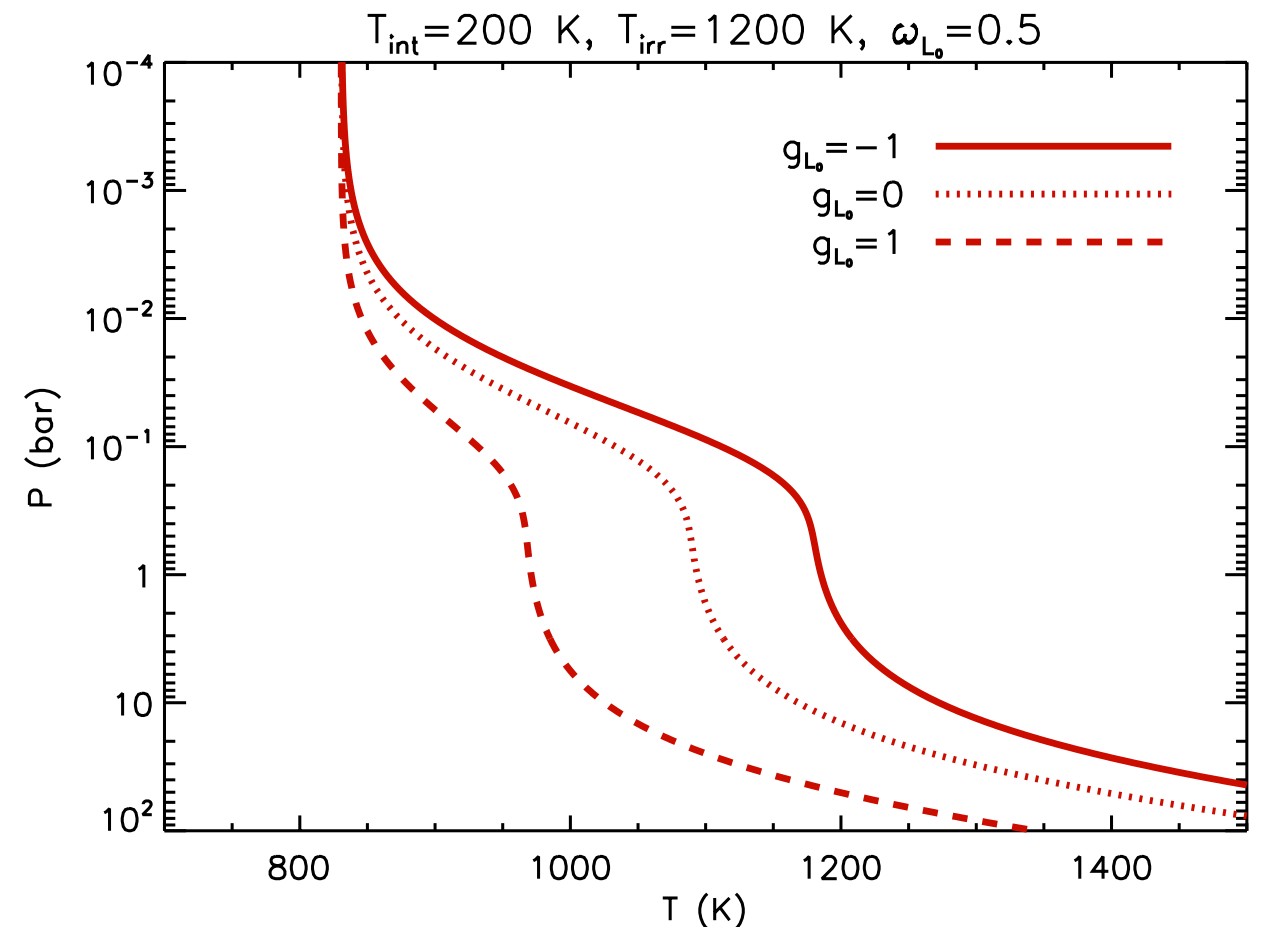
single scattering albedo

- The commonly used **Eddington closure** introduces two types of errors:
1. spurious enhancement of blackbody emission
  2. spurious production of reflected flux

# Building on the work of Chandrasekhar, Mihalas: analytical T-P profiles with irradiation



scattering of starlight generally  
warms the upper atmosphere  
and cools the lower atmosphere  
**(anti-greenhouse effect)**

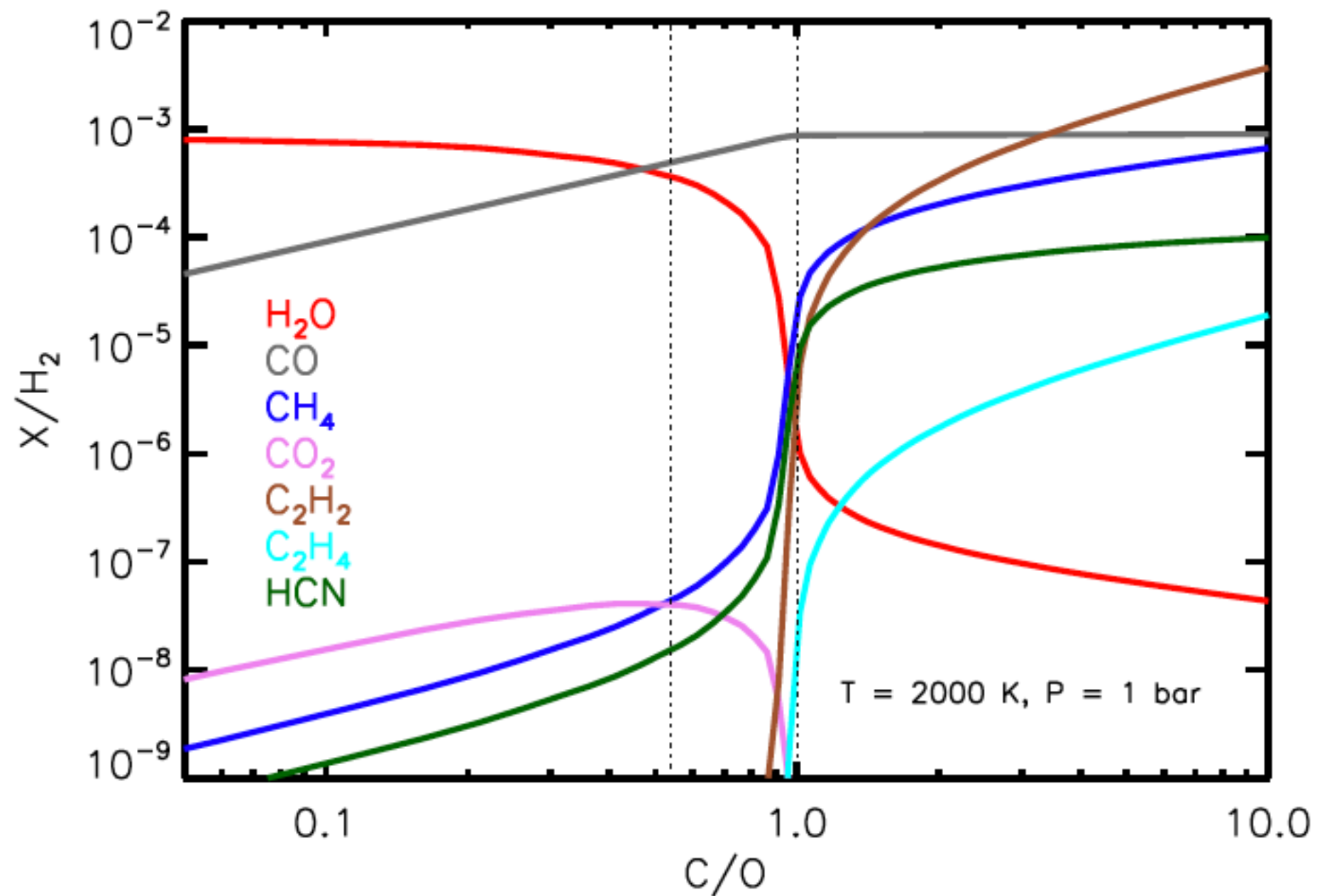


scattering of thermal emission  
generally warms the atmosphere,  
unless it is purely forward scattering  
**(scattering greenhouse effect)**

*Heng, Mendonca & Lee (2014, ApJS, in press)*

*See also: Hubeny et al. (2003), Hansen (2008), Guillot (2010), Heng et al. (2012), Parmentier & Guillot (2014)*

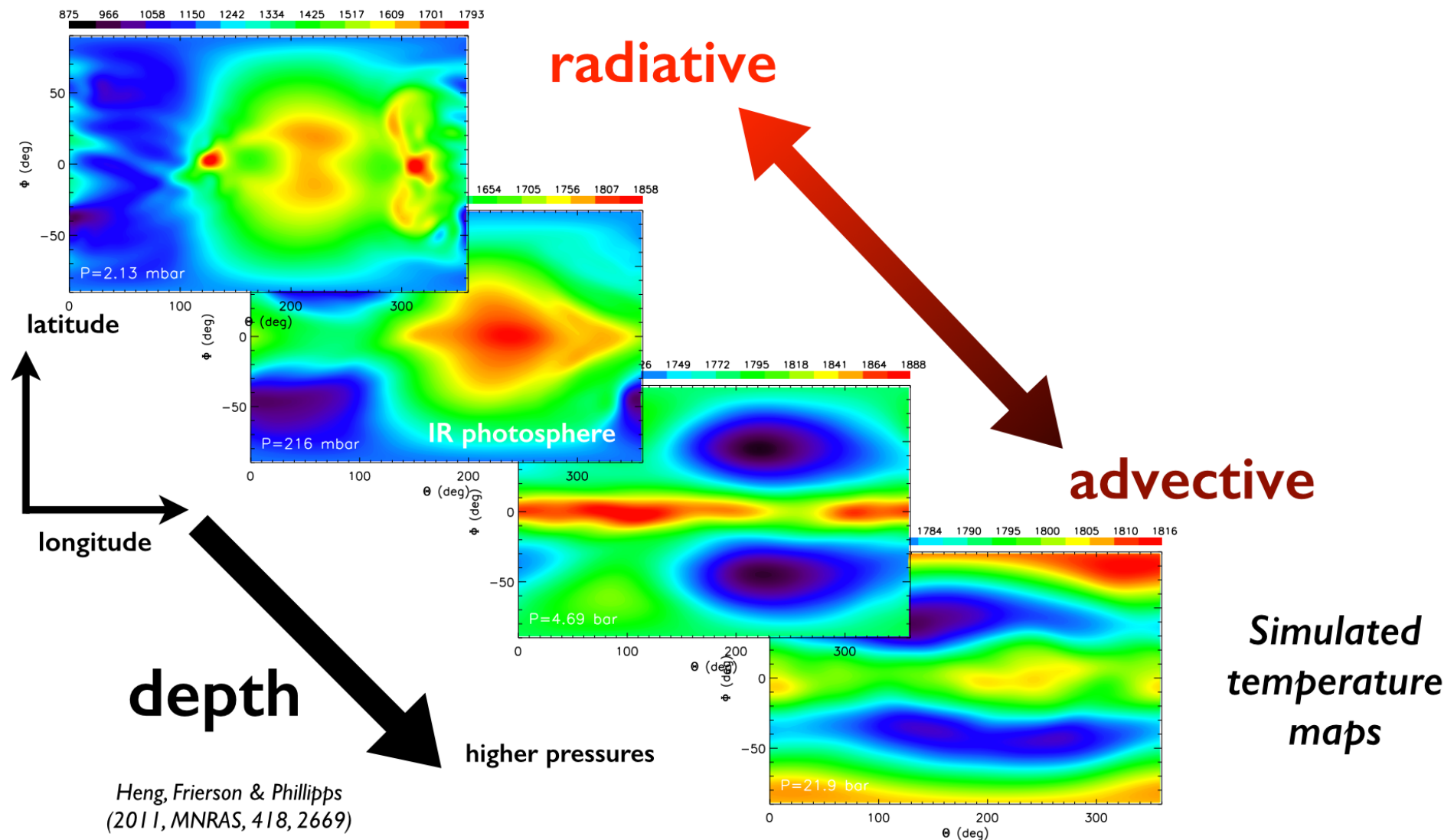
# Do hot exoplanets display chemical diversity?



As C/O ratio varies, abundances of molecules generally vary by orders of magnitude (except for CO).  
VO and TiO formation are inhibited in carbon-rich environments.

# **III. Simulations**

# Why do we even need 3D simulations in the first place?

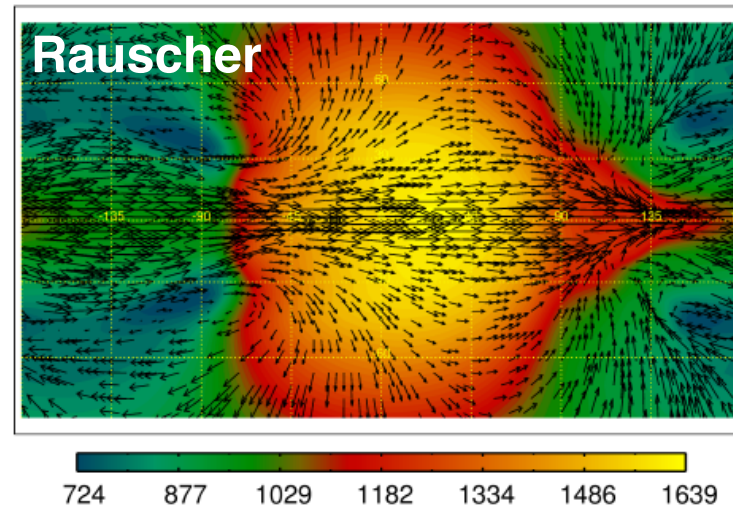
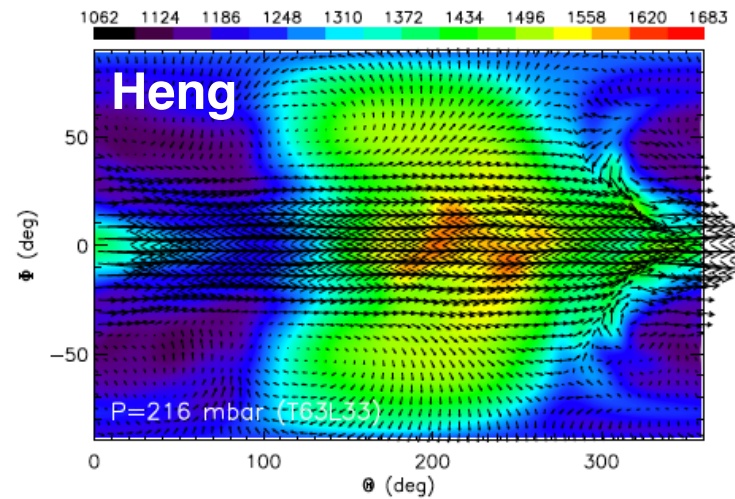


We are interested in the infrared photosphere, but to simulate it properly we need to simulate the different interacting atmospheric layers.

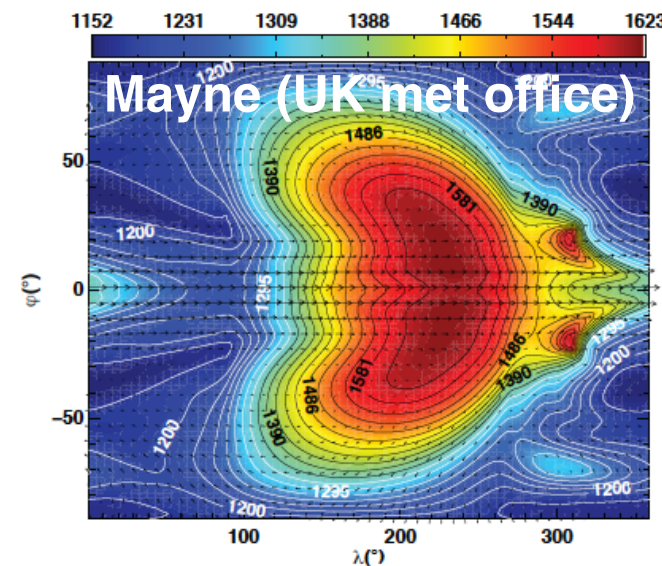
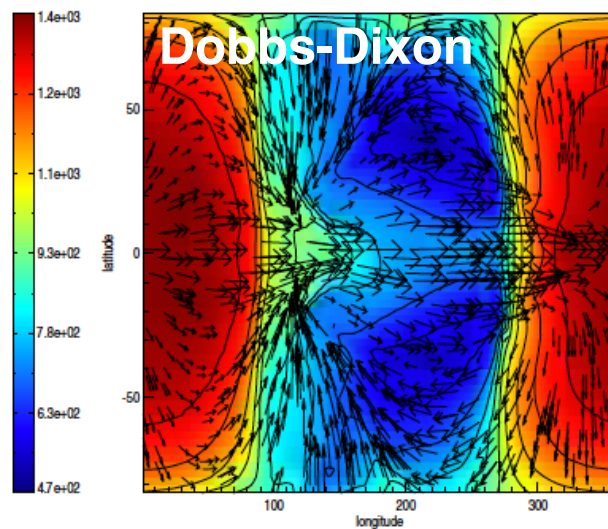
GCMs (general circulation models) have had some success explaining basic trends and observed spectra (Showman et al. 2009).



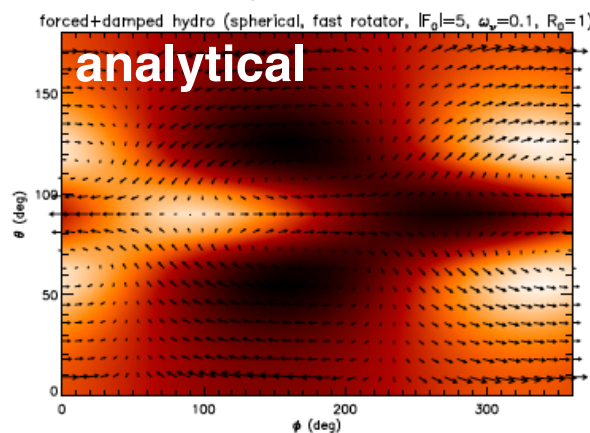
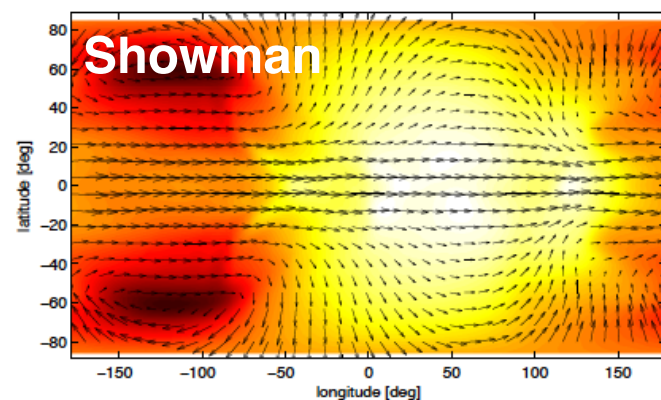
# Published simulations show consensus on global structure of hot Jupiters



Quantitative differences exist between results from different groups, but the qualitative trends agree.



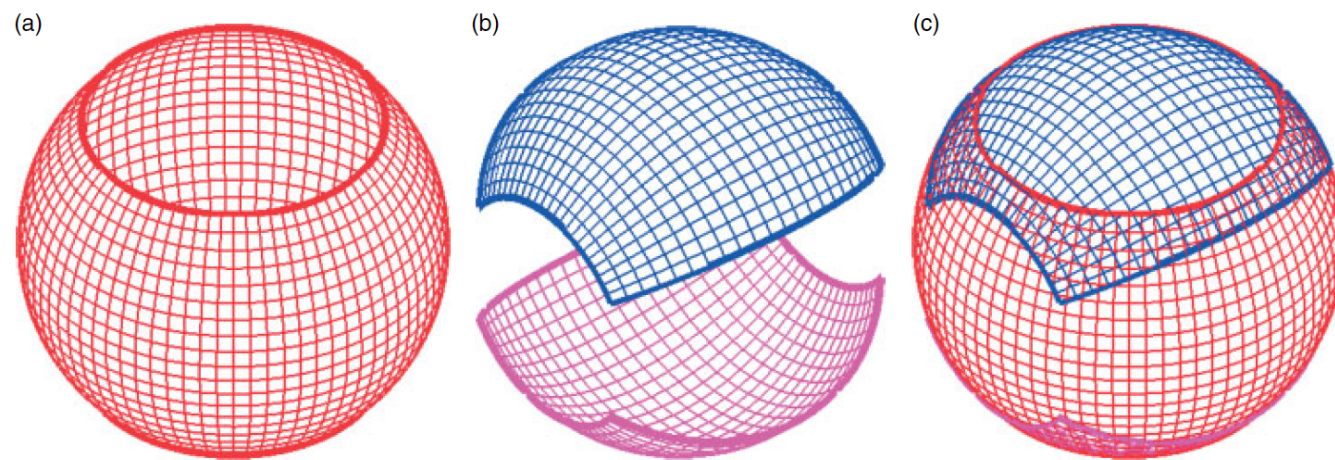
Nevertheless, several formidable technical challenges remain (see upcoming slides).



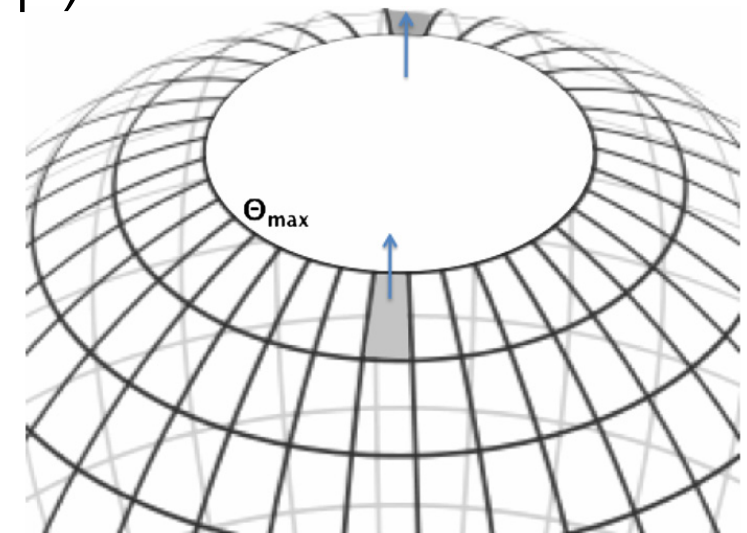


# Challenge #1: the pole problem

regular spherical grids have singularities  
at the poles (zero time step)

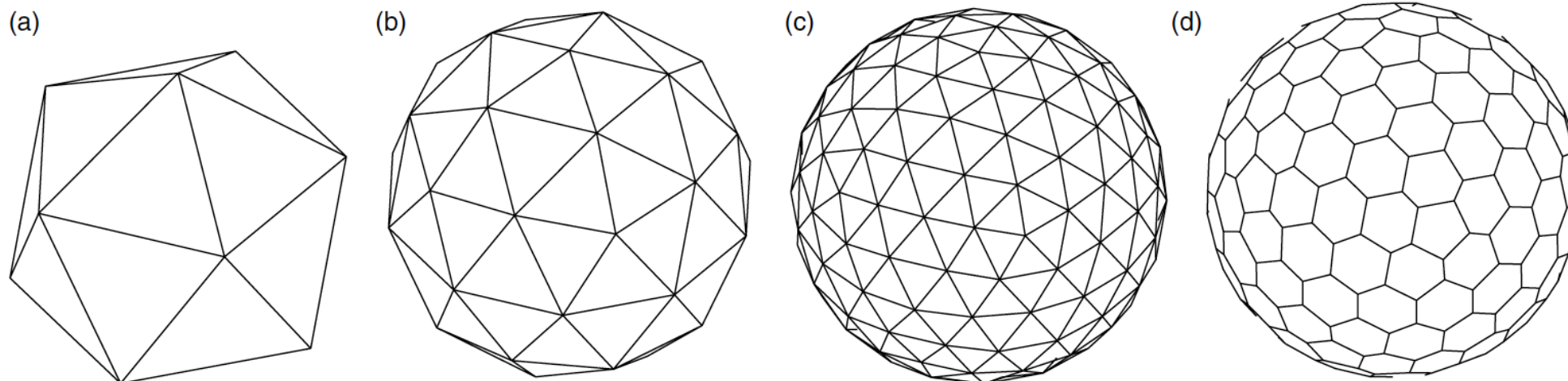


multiple spherical grids



**Figure 1.** Illustration of the staggered grid setup near the north pole. Scalars are defined at grid centers while velocities and fluxes are defined along appropriate grid edges. Cells along the polar circle  $((\phi, \theta) = (\phi, \theta_{max}))$  utilize the cell at  $(\phi + \pi, \theta_{max})$  as a neighboring cell. For instance, the two shaded cells communicate directly and the velocities (blue arrows) across the cell edges are identical.

truncation (ignore the problem)  
cf. Dobbs-Dixon



icosahedral grid



## Challenge #2: atmospheres are nearly hydrostatic

### **Common belief:**

hydrostatic balance (pressure vs. gravity)  
implies zero vertical/radial flow

True only in 1D!

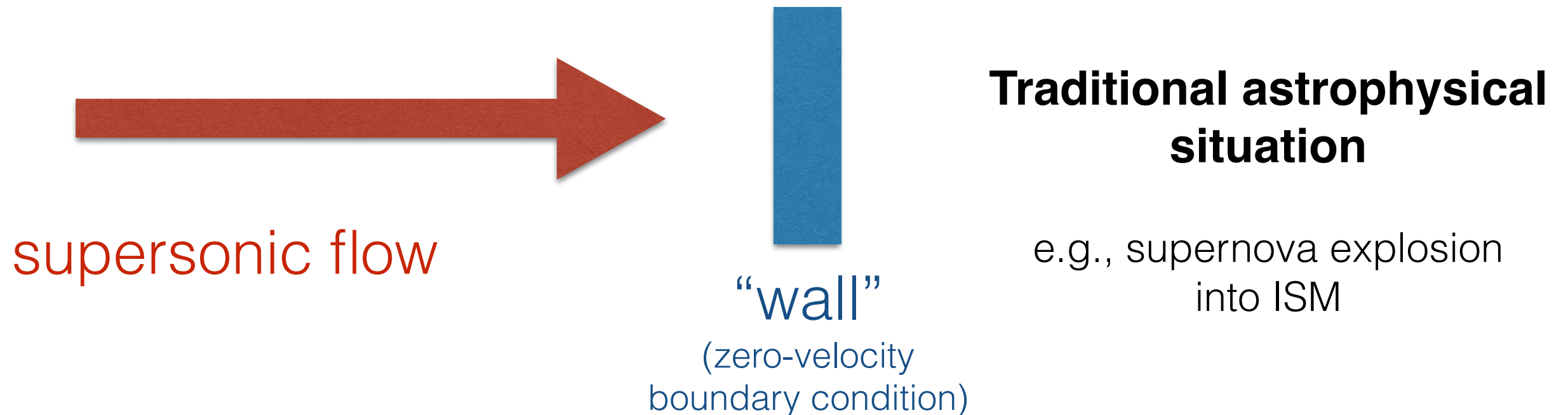
It really means that adjustment back to  
hydrostatic equilibrium is very fast.

### **Computational challenge:**

bottlenecks time step in the  
vertical/radial direction

Possible solutions include using  
hybrid explicit-implicit schemes (e.g., HEVI).

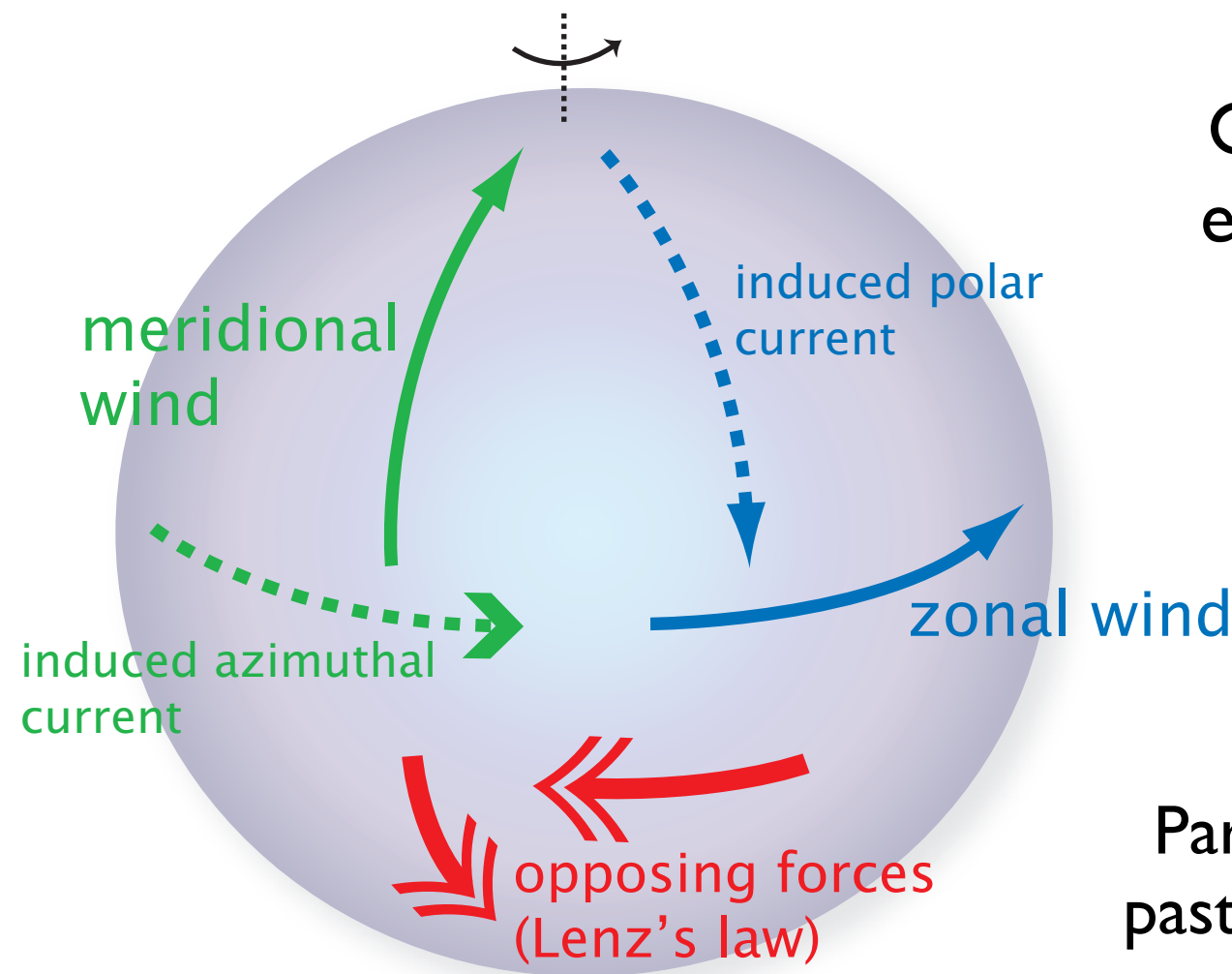
# Challenge #3: ~1000 K flows form shocks



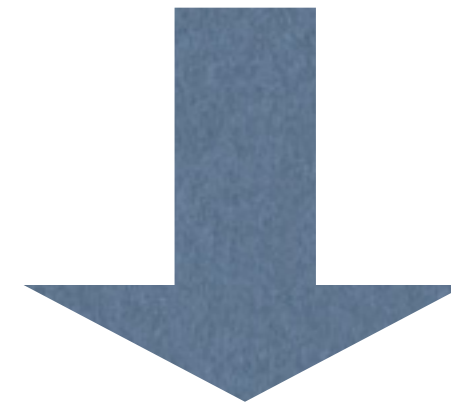
**In an exoplanetary atmosphere, the “wall” is created naturally by the night-to-day transition of the flow (re-compression). Shocks convert ~25% of kinetic energy into heat.**

The situation is similar to a **wind tunnel**. The Mach number needs to exceed unity and decrease locally for a shock to form.

# Challenge #4: ~1000 K flows are partially ionised



Collisional ionization liberates electrons from Group I metals (Na, K)



Partially ionized atmosphere advected past magnetic field induces currents and opposing forces

## An exoplanet-scale manifestation of Lenz's law

*Perna, Menou & Rauscher (2010a,b); Batygin & Stevenson (2010); Batygin et al. (2011); Menou (2012); Heng (2012b); Rauscher & Menou (2013); Rogers & Showman (2014); Batygin & Stanley (2014)*

Study (Alphabetical)	Approx. Used	Global Grid?	Irradiated <sup>†</sup> Atmosphere?	Radiative <sup>†</sup> Transfer?	Treats Shocks?	Magnetic Fields?	Passes Earth <sup>‡</sup> Benchmark?	Ref.
Batygin et al. (2013) <sup>♣</sup>	BQ (3D)	Y	Y	N	N	Y	N	[6]
Bending et al. (2012)	PE (3D)	Y	Y	N	N	N	Y	[7]
Burkert et al. (2005) <sup>♣◊</sup>	EE (2D)	N	Y	Y	N	N	N	[15]
Burrows et al. (2010)	PE (3D)	Y	Y	N	N	N	Y	[18]
Cho et al. (2003)	EB (2D)	Y	N	N	N	N	N	[23]
Cho et al. (2008)	EB (2D)	Y	N	N	N	N	N	[24]
Cooper & Showman (2005)	PE (3D)	Y	Y	N	N	N	Y	[25]
Cooper & Showman (2006)	PE (3D)	Y	Y	N	N	N	Y	[26]
Dobbs-Dixon & Lin (2008) <sup>♣</sup>	EE (3D)	N	Y	Y	N	N	N	[41]
Dobbs-Dixon et al. (2010) <sup>♣</sup>	NS (3D)	N	Y	Y	Y	N	N	[42]
Dobbs-Dixon et al. (2012) <sup>♣</sup>	NS (3D)	N	Y	Y	Y	N	N	[43]
Dobbs-Dixon & Agol (2013)	NS (3D)	N	Y	Y	Y	N	N	[44]
Heng et al. (2011a)	PE (3D)	Y	Y	N	N	N	Y	[57]
Heng et al. (2011b)	PE (3D)	Y	Y	Y	N	N	Y	[58]
Kataria et al. (2013)	PE (3D)	Y	Y	Y	N	N	Y	[68]
Langton & Laughlin (2008)	EE (2D)	Y	Y	Y	N	N	N	[82]
Lewis et al. (2010)	PE (3D)	Y	Y	Y	N	N	Y	[85]
Li & Goodman (2010)	NS (2D)	N	Y	N	Y	N	N	[87]
Liu & Showman (2013)	PE (3D)	Y	Y	N	N	N	Y	[88]
Mayne et al. (2013)	EE (3D)	Y	Y	N	N	N	Y	[96]
Mayne et al. (2014) <sup>♡</sup>	EE (3D)	Y	Y	N	N	N	Y	[97]
Menou & Rauscher (2009)	PE (3D)	Y	Y	N	N	N	Y	[99]
Menou (2012)	PE (3D)	Y	Y	Y	N	N	Y	[101]
Merlis & Schneider (2010) <sup>♣</sup>	PE (3D)	Y	Y	Y	N	N	Y	[103]
Parmentier et al. (2013)	PE (3D)	Y	Y	Y	N	N	Y	[107]
Perna et al. (2010a)	PE (3D)	Y	Y	N	N	N	Y	[111]
Perna et al. (2010b)	PE (3D)	Y	Y	N	N	N	Y	[112]
Perna et al. (2012)	PE (3D)	Y	Y	Y	N	N	Y	[113]
Polichtchouk & Cho (2012)	PE (3D)	Y	N	N	N	N	Y	[117]
Rauscher & Menou (2010)	PE (3D)	Y	Y	N	N	N	Y	[119]
Rauscher & Menou (2012a)	PE (3D)	Y	Y	N	N	N	Y	[120]
Rauscher & Menou (2012b)	PE (3D)	Y	Y	Y	N	N	Y	[121]
Rauscher & Menou (2013)	PE (3D)	Y	Y	Y	N	N	Y	[122]
Rogers & Showman (2014)	AN (3D)	Y	Y	N	N	Y	N	[127]
Showman & Guillot (2002)	PE (3D)	Y	Y	N	N	N	Y	[132]
Showman et al. (2008)	PE (3D)	Y	Y	N	N	N	Y	[134]
Showman et al. (2009)	PE (3D)	Y	Y	Y	N	N	Y	[135]
Thrustarson & Cho (2010)	PE (3D)	Y	Y	N	N	N	Y	[151]
Thrustarson & Cho (2011)	PE (3D)	Y	Y	N	N	N	Y	[152]

<sup>†</sup>: "Irradiated" refers specifically to whether the model atmosphere is being forced by stellar irradiation, i.e., whether the irradiation is doing work on the atmosphere. Simulations that are unforced by irradiation are sometimes termed "adiabatic". It is possible for the effects of radiation in irradiated atmospheres to be mimicked without explicitly performing radiative transfer, by adopting a Newtonian relaxation or cooling term in the thermodynamic equation.

<sup>‡</sup>: only marked "Y" if there is either an explicit demonstration in the publication or a clear citation to previous publications describing that the simulation code used is able to reproduce the Held-Suarez benchmark test for Earth [56]. Since it is a 3D test, 2D simulations, by definition, are unable to reproduce it.

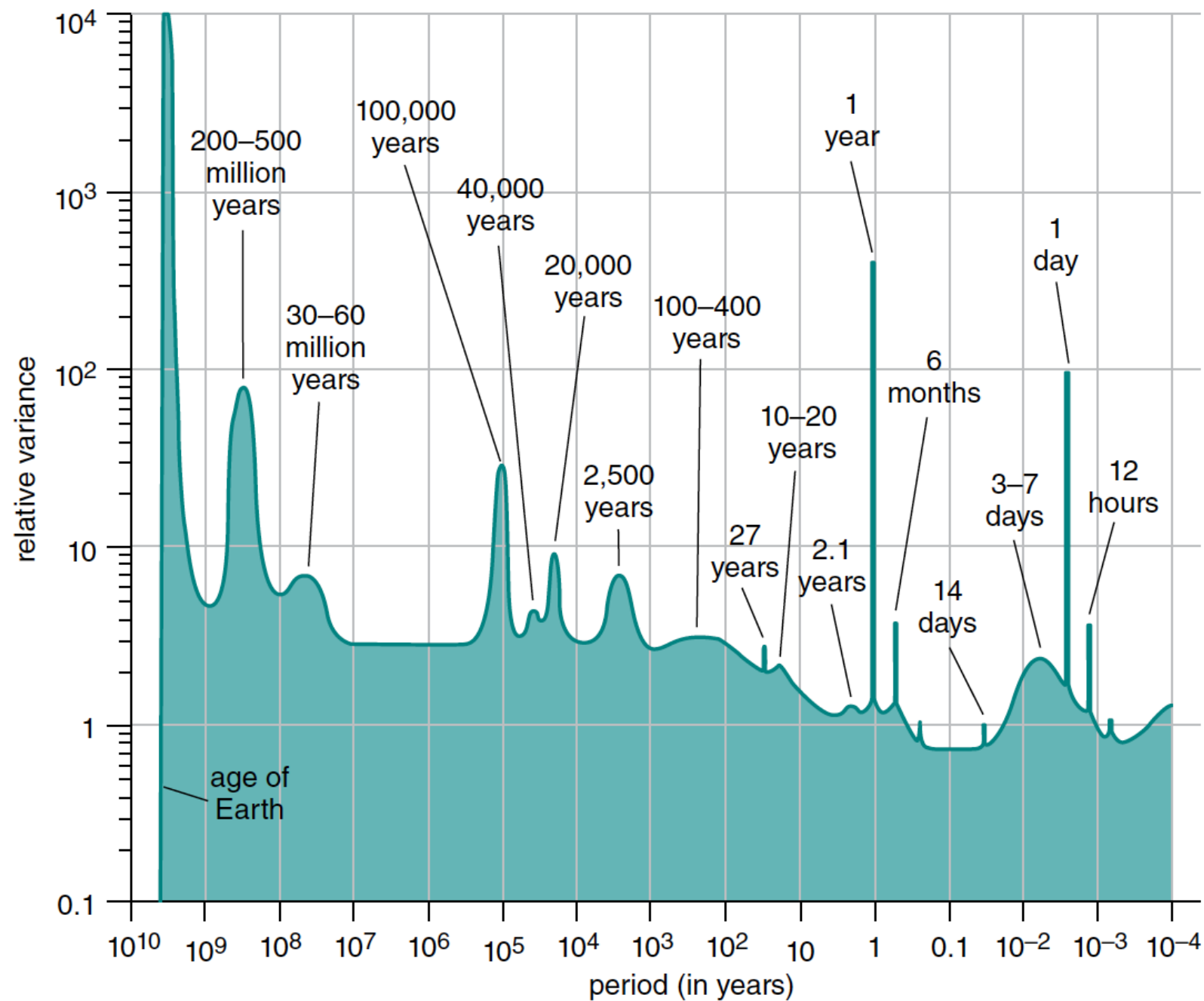
♣: Employs flux-limited diffusion in the region encompassing the photosphere, an approximation that is strictly valid only in optically thin or thick situations.

◊: Rotation of the exoplanet is not included. ♣: Effects of hydrological cycle included. ♡: Non-hydrostatic.

Acronyms: Boussinesq (BQ), anelastic (AN), equivalent barotropic (EB), primitive equations (PE), Euler equation (EE), Navier-Stokes equation (NS).

Table 1: Summary table of atmospheric circulation studies of exoplanets using GCMs

# A futuristic thought: power spectrum of an exoplanet?



*Mitchell (1976, Quaternary Research, 6, 481)*

# If Earth was an exoplanet.....

# Summary

- The theory and simulation of exoplanetary atmospheres is a **nascent, interdisciplinary** field that builds upon the work of astronomy/astrophysics, atmospheric/climate science, high-performance computing and computer science, etc.
- It is ultimately aimed at developing a deeper understanding of the **processes governing atmospheric dynamics, radiative transfer and chemistry**, so as to aid in the interpretation of observations.
- Expect **order-of-magnitude leaps** in both observational and simulational techniques in the **coming decade**.



[www.exoclimes.org](http://www.exoclimes.org)

*Heng & Showman (2015, Annual Review of Earth & Planetary Science)*

*Prof. Dr. Kevin Heng at the University of Kiel (2014)*



# The Landscape of Things

(biased towards transits)

Also: transition from 1D radiative transfer models to hierarchy of models including 3D GCMs

Spitzer/Hubble era:  
“spectro-photometry”

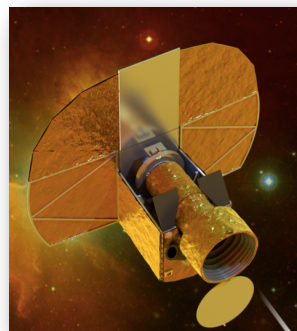
JWST spectroscopy  
(and E-ELT, GMT, TMT)



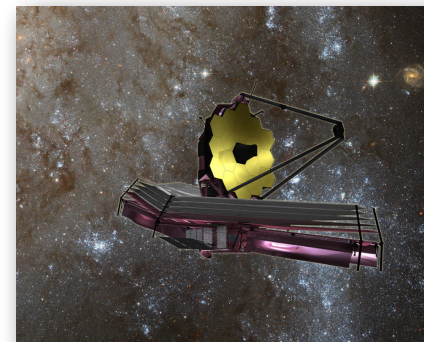
Kepler (2009):  
discovery, statistics



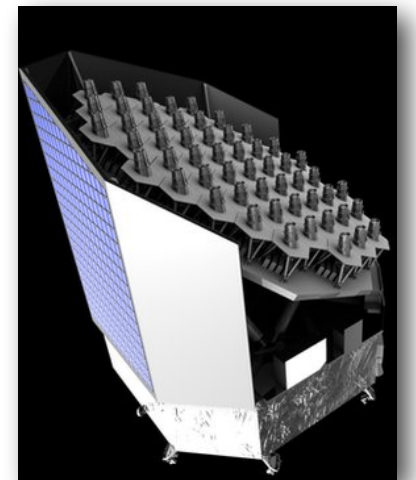
TESS (2017):  
discovery



CHEOPS (2017):  
follow-up

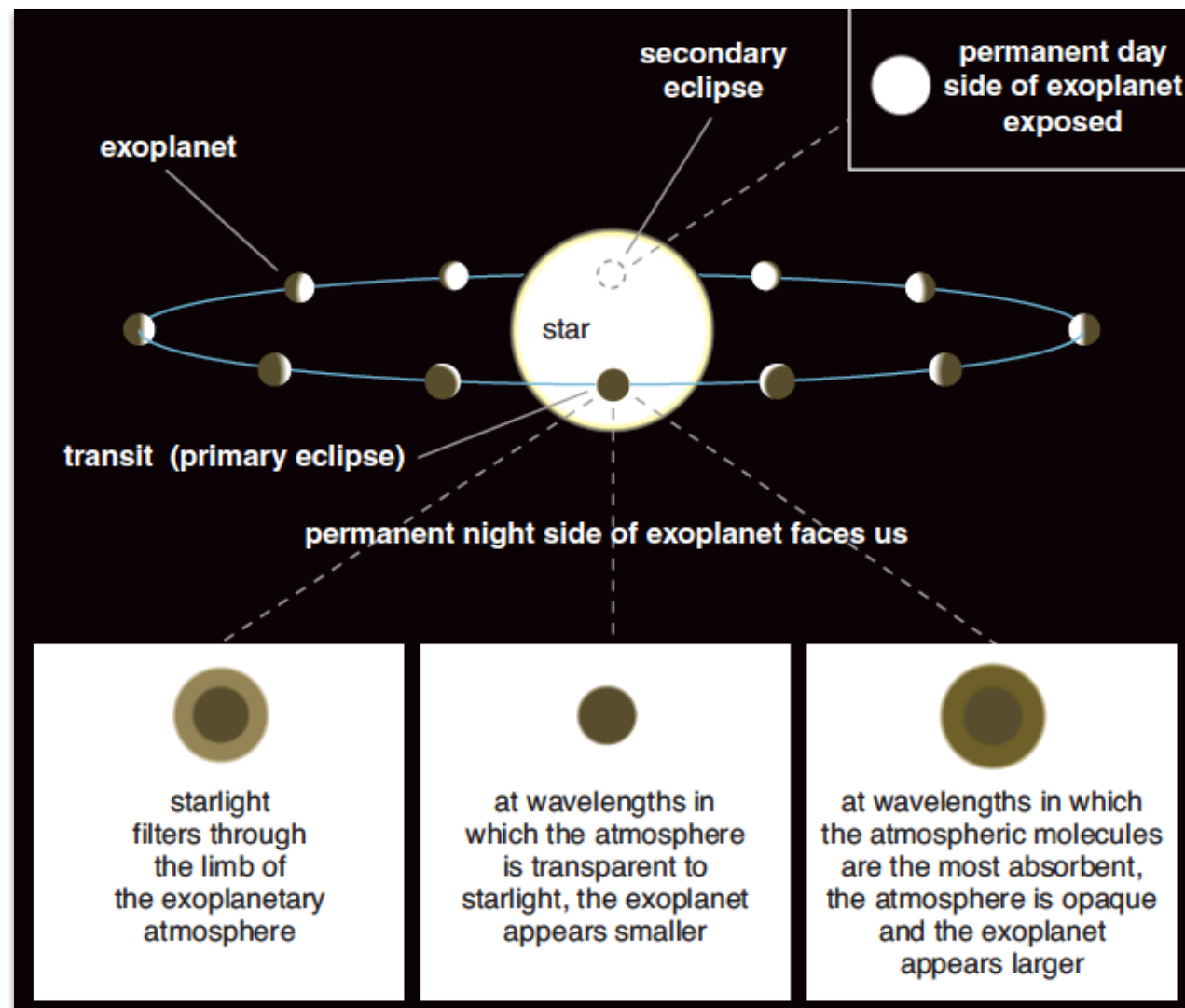


JWST (2018):  
spectroscopy



PLATO (2024):  
discovery, statistics

# Why do we even need 3D simulations in the first place?



To understand the connection between transmission (limb) and emission (dayside) spectra.

To simulate phase curves, eclipse maps, day-night flux contrasts.

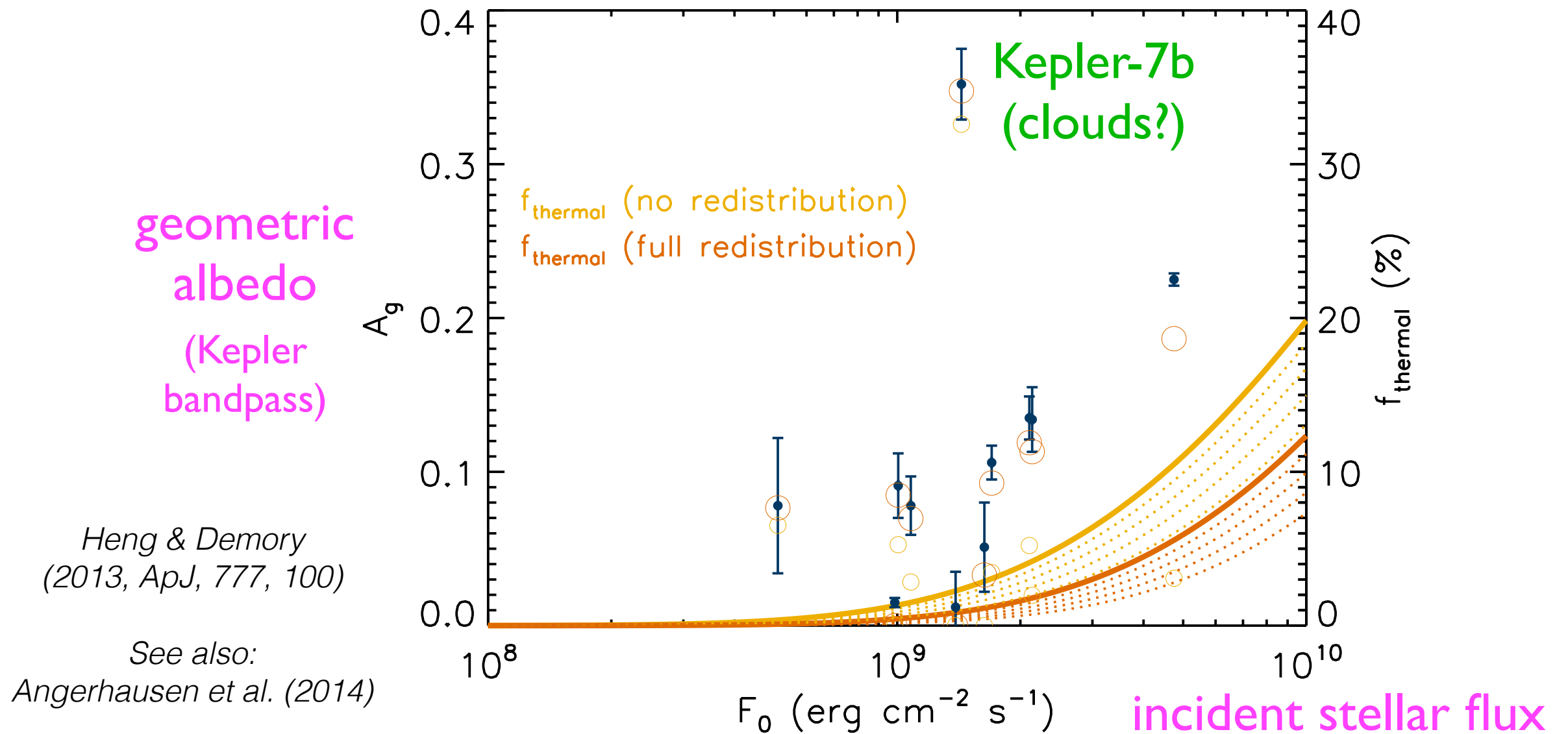
Future: to predict temporal variability

**The cutting-edge data (and an anticipated flood with the next-generation instruments) will provide 2D and even 3D information.**

*Heng & Showman (2015, Annual Review of Earth & Planetary Science)*



# Optical secondary eclipses yield the geometric albedo of the atmosphere



No obvious trend with stellar irradiation

Corrected for contamination by thermal emission (for the hottest objects).