

Bridging the gap between the core accretion and gravitational instability planet formation theories

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**University of
Zurich** ^{UZH}



ETH

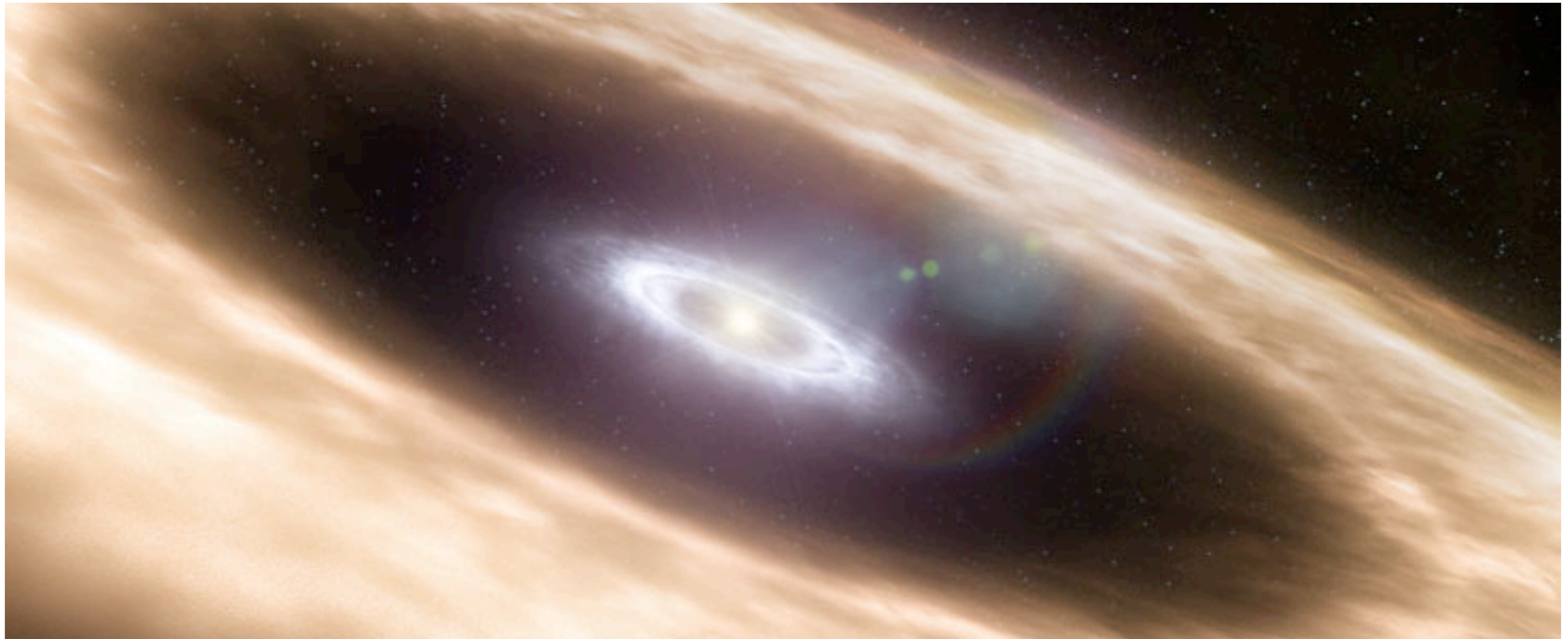
Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology Zurich

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- Introduction
 - Planet formation mechanisms
 - The gap between the formation mechanisms
- Recent developments on planet formation
 - core accretion
 - gravitational instability

Introduction

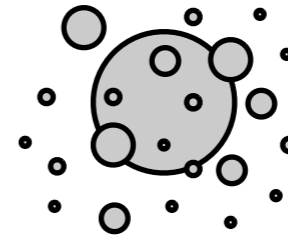
Planets form in circumstellar discs made of gas and dust



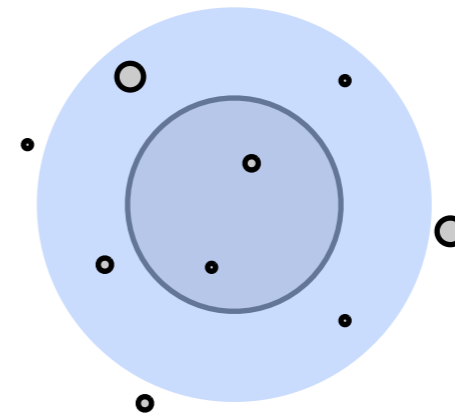
Artist's impression, ESO

Planets may form by dust growth followed by gas accretion

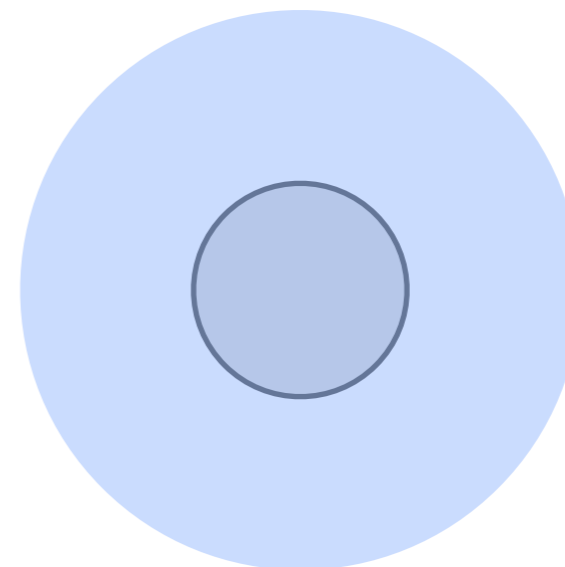
1. Dust coagulates to form a solid core



2. Core starts to accrete gas



3. Runaway gas accretion forms giant planet



Can in principle occur at any time

Posters & talks:
Venturini, Yang,
Picogna, Drazkowska

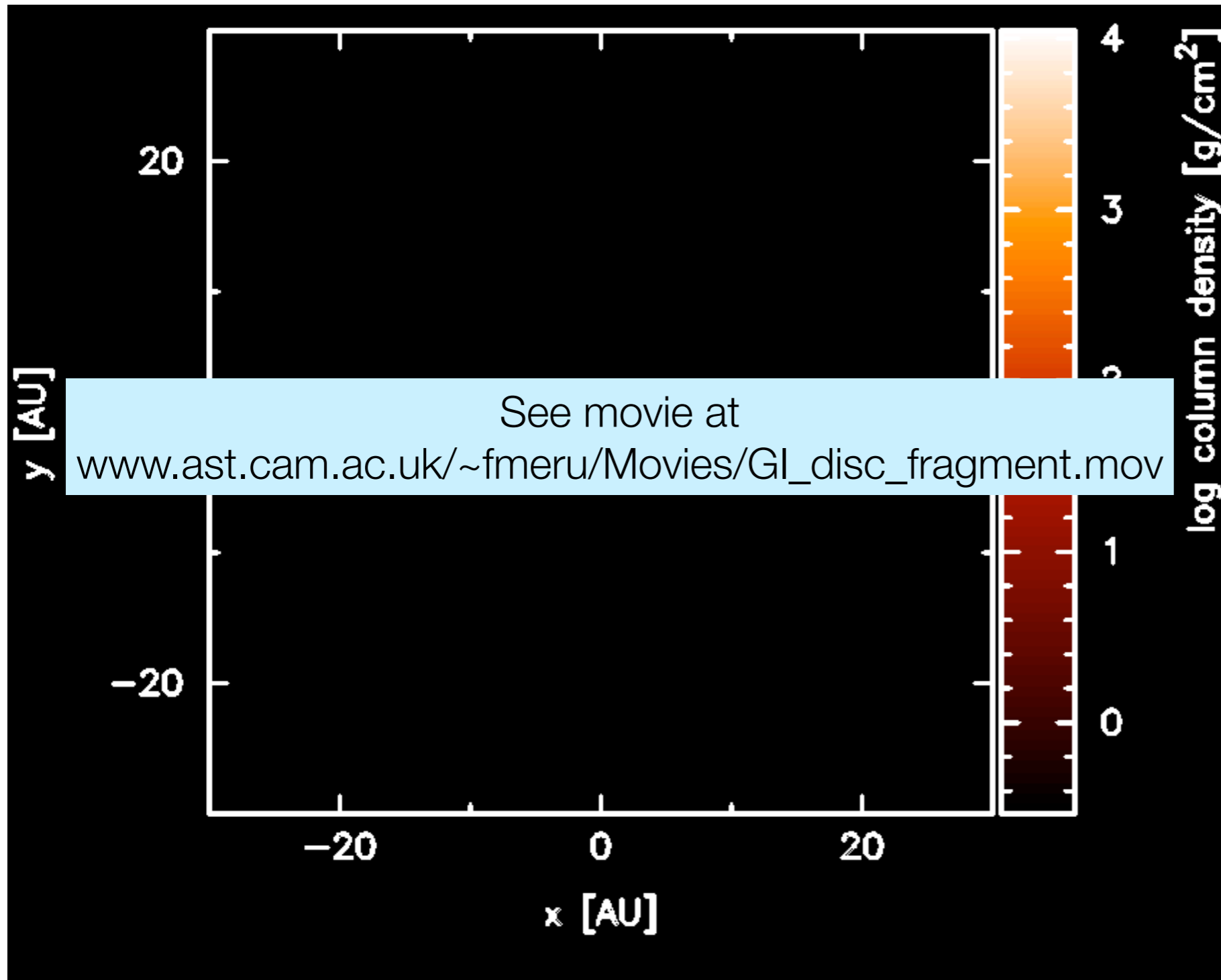
Planets form by core accretion in the inner disc

Formation timescales too long at large radii

$$\frac{dM_p}{dt} \propto \Sigma \Omega$$

Planetesimal accretion
rate too long at large radii

Gravitational Instability involves the fragmentation of massive discs



Self-gravity drives the evolution of massive discs
(spiral structures form)

Spirals collapse and fragment under the “right” conditions

Poster and talk:
Stoyanovska,
Vorobyov

Fragmentation occurs locally if the disc is unstable

Stability determined by:

$$Q = \frac{c_s \kappa}{\pi \Sigma G}$$

For an infinitesimally thin disc:

$$Q > 1 \equiv \text{stable}$$

$$Q < 1 \equiv \text{unstable}$$

A fast cooling is also needed for fragmentation

Cooling needs to be faster than a critical value

Gammie 2001; Rice et al 2005; Meru & Bate 2011b,2012

$$t_{\text{cool}} < \frac{\beta_{\text{crit}}}{\Omega}$$

Fragmentation is more likely at larger radii

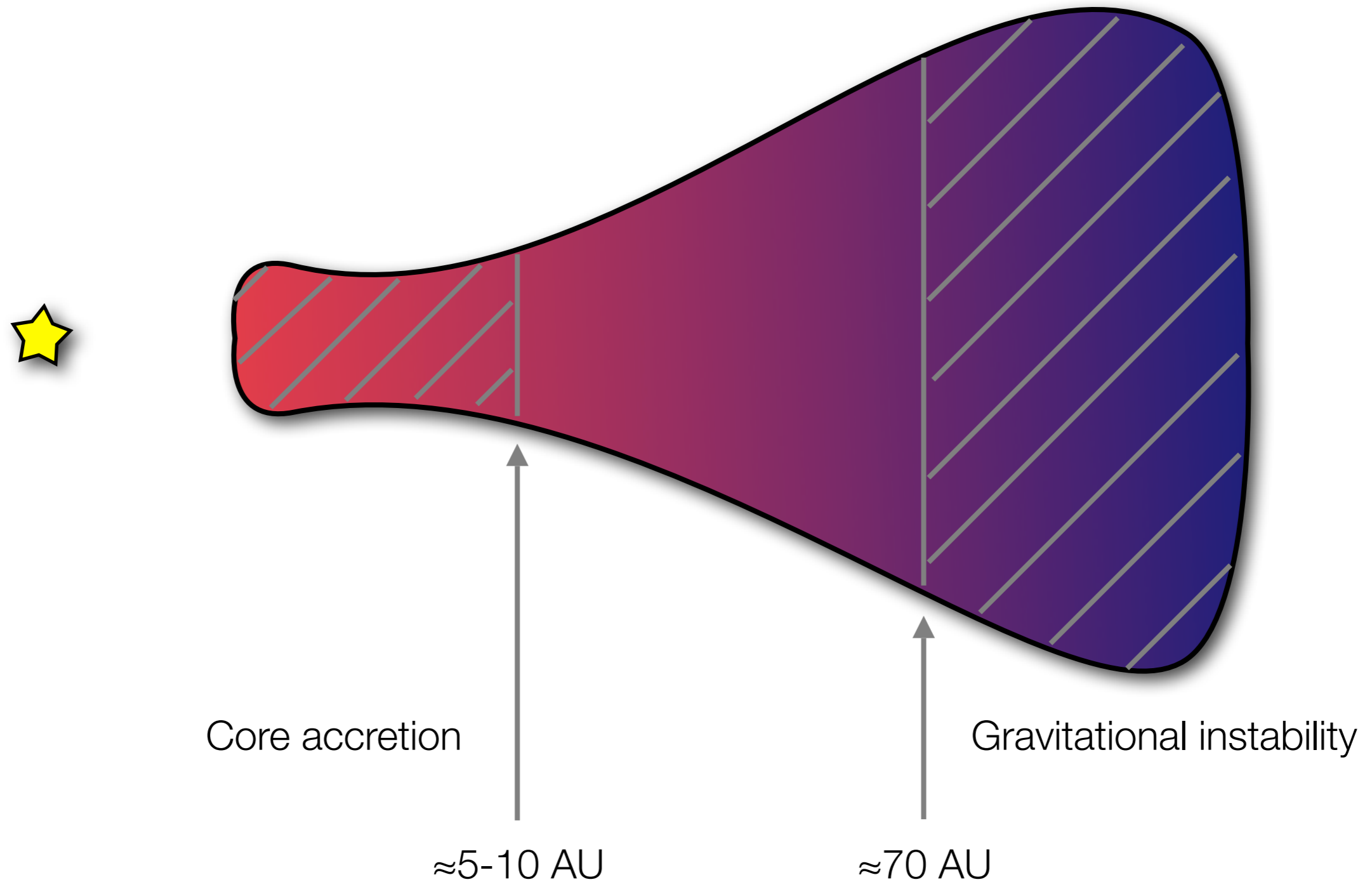
Toomre parameter generally decreases with radius

$$Q = \frac{c_s \kappa}{\pi \Sigma G}$$

Cooling condition more likely to be satisfied at large radii - longer orbital timescale

$$t_{\text{cool}} < \frac{\beta_{\text{crit}}}{\Omega}$$

There appears to be a formation gap in protoplanetary discs

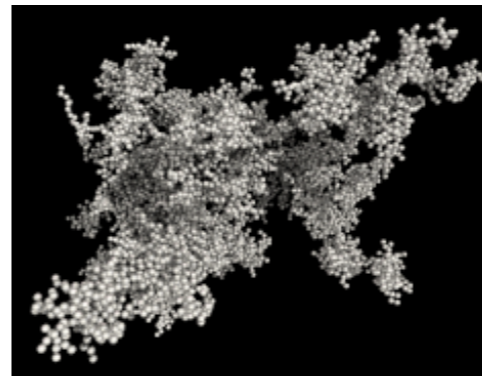


Core accretion

There are different methods used to understand dust growth at small sizes

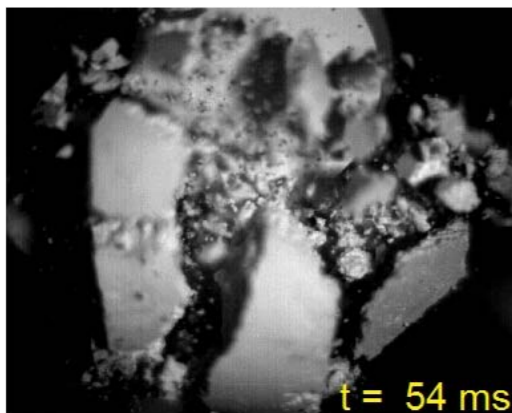
Scale

Molecular dynamics (particles)



A. Seizinger

Laboratory experiments
($\sim 10 \mu\text{m} - 10 \text{cm}$)

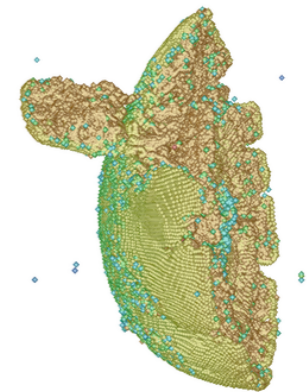


Beitz et al 2011

Posters and talks:

Capelo, De Beule,
Schywek, Kothe, Deckers,
Teiser, Blum, Bukhari,
Kelling, Weidling, Wurm

SPH simulations (cm-dm)



Talk:
Gonzalez

Meru et al 2013

Monte Carlo
(considers background
disc)

Smoluchowski equation
(considers background
disc)

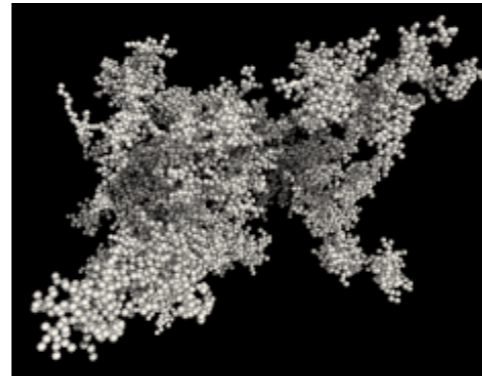
Poster:
Stammler

Gravity-dominated regime

There are different methods used to understand dust growth at small sizes

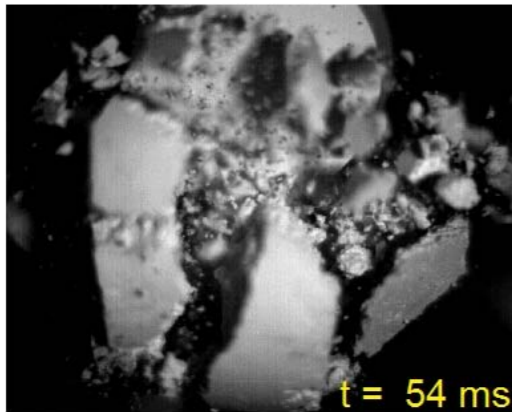
Scale

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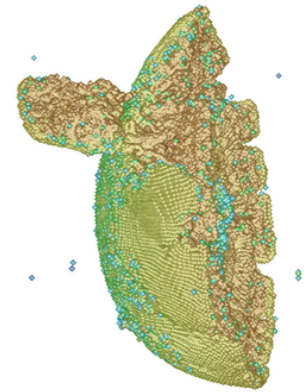


Beitz et al 2011

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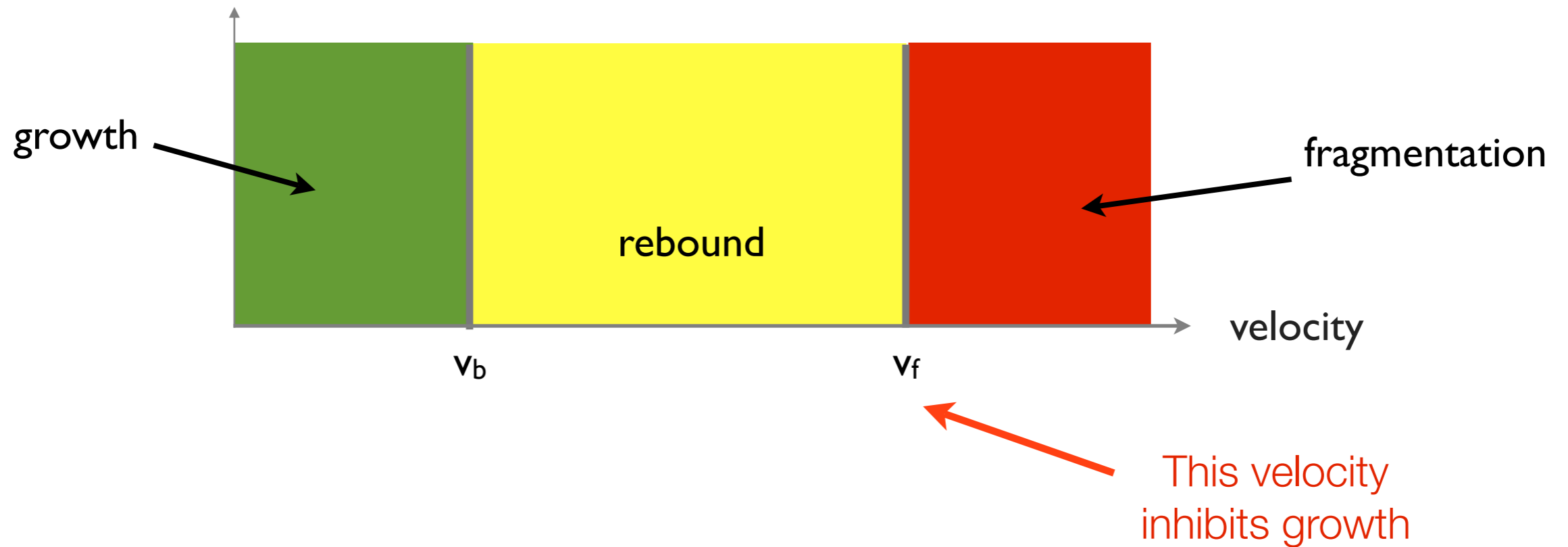
Monte Carlo
(considers background
disc)

Smoluchowski equation
(considers background
disc)

Poster:
Stammler

Gravity-dominated regime

The velocity at which the aggregates collide determines their collisional outcome

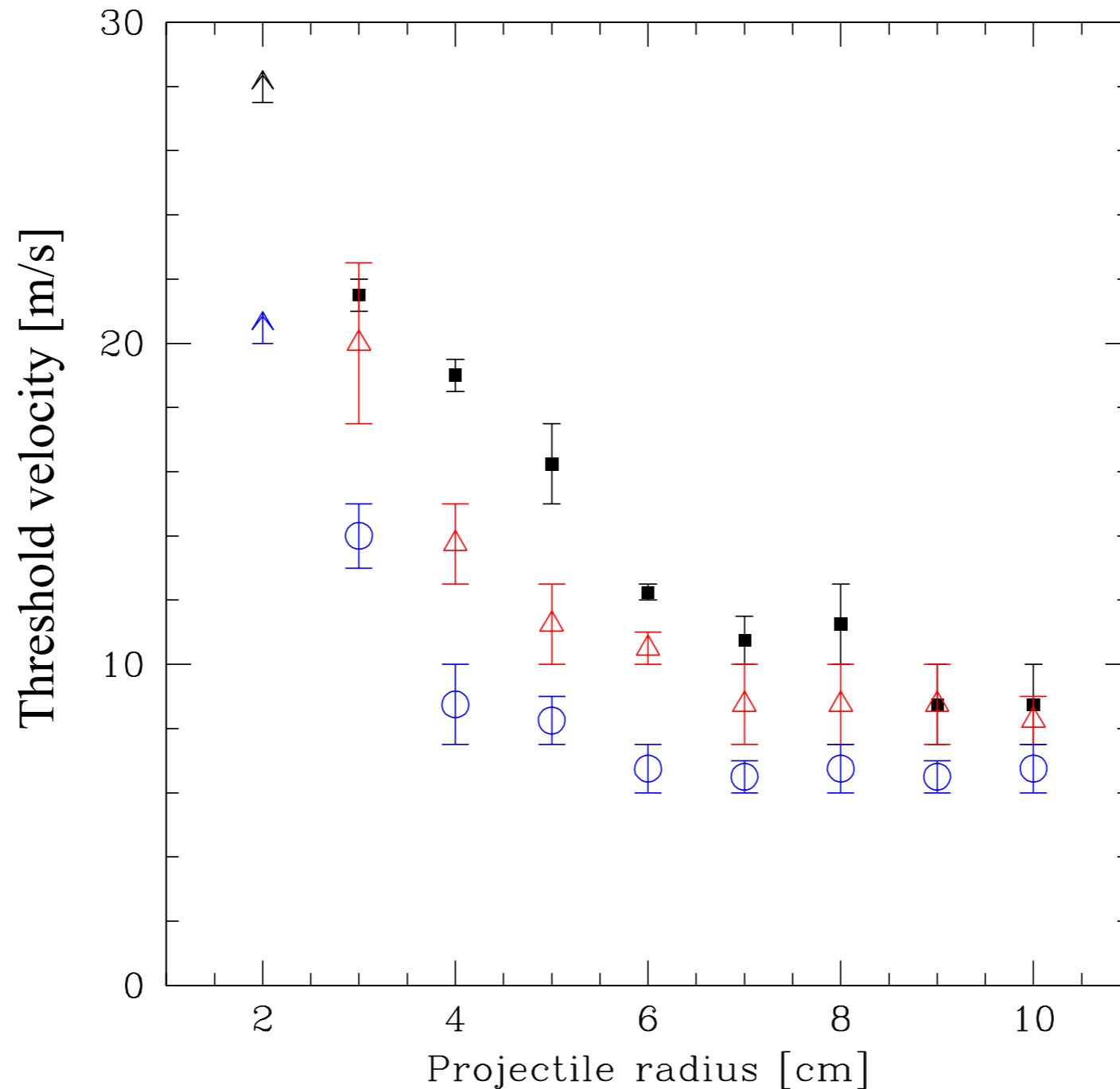


How high can the collision velocities be before aggregates will fragment?

How is the fragmentation velocity affected by aggregate size and porosity ?

Knowing the collisional outcome is essential to model the growth evolution of many dust aggregates

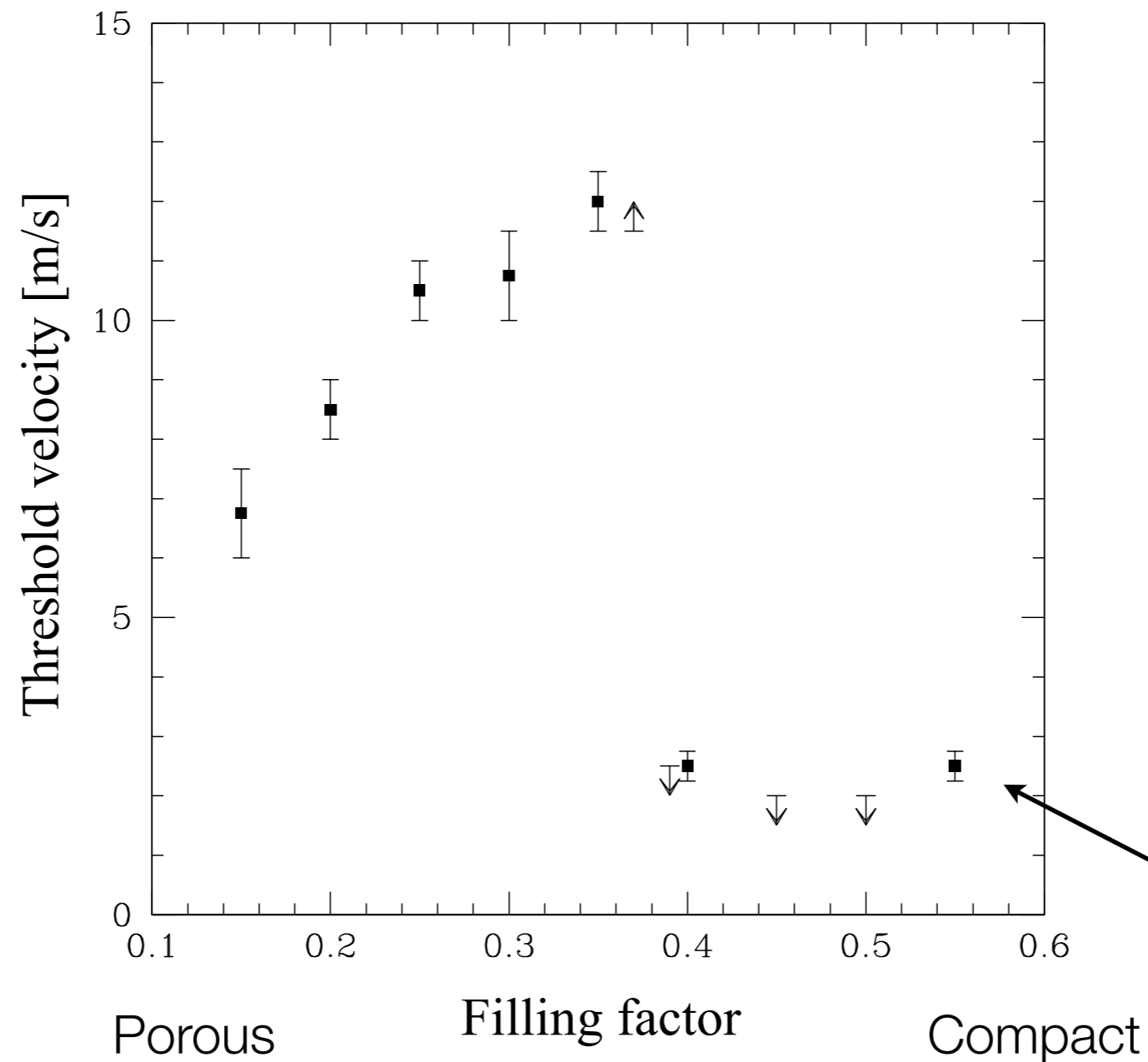
As the mass ratio increases the aggregates are more likely to stick



← Mass ratio

Also seen in laboratory experiments
e.g. Wurm et al 2005, Teiser & Wurm 2009

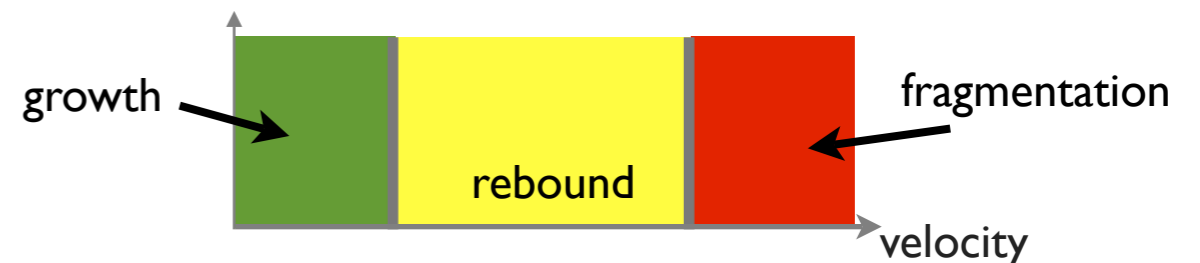
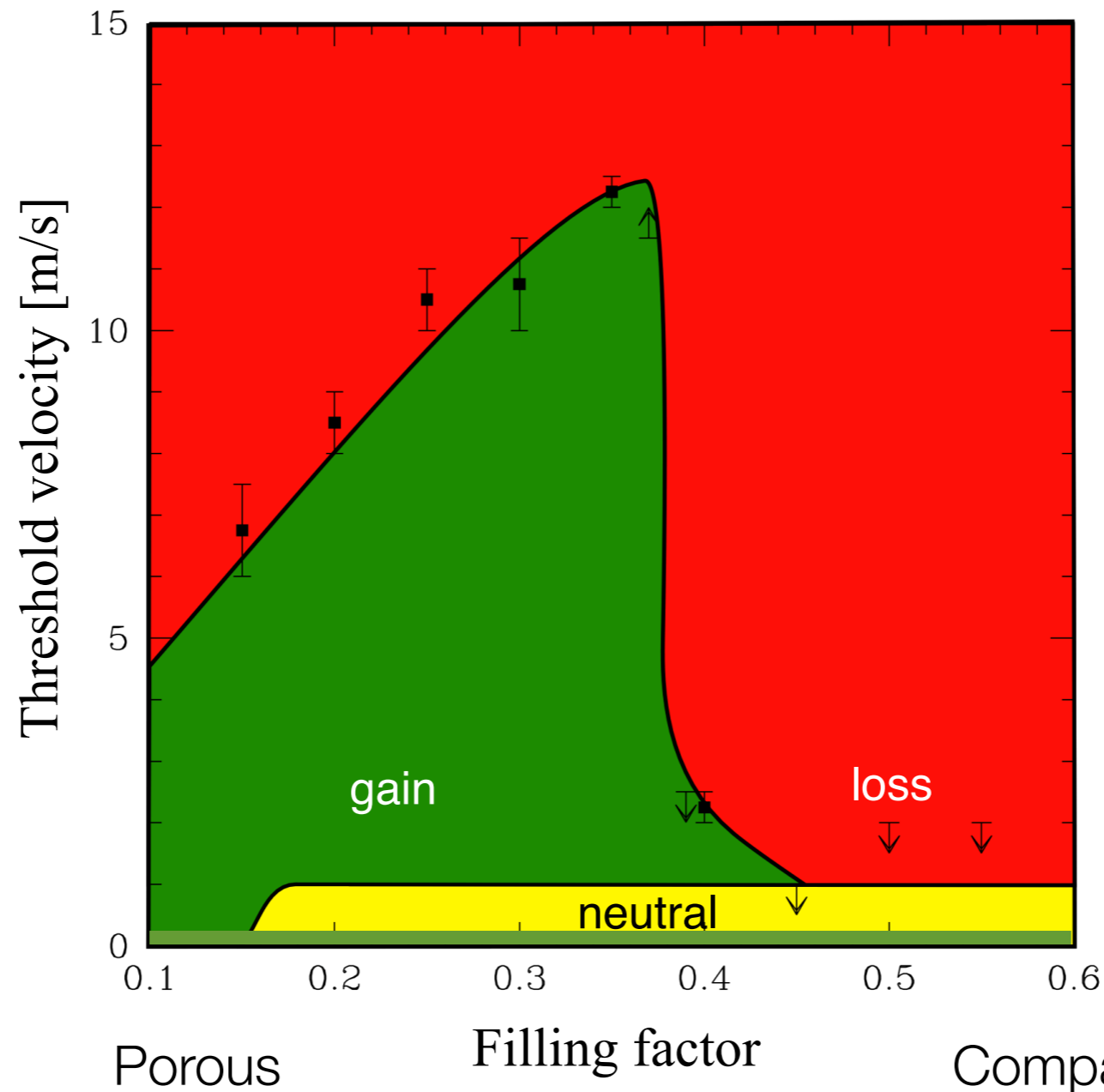
Porous aggregates become stronger with filling factor but compact aggregates break easily



Compact aggregates may not survive easily

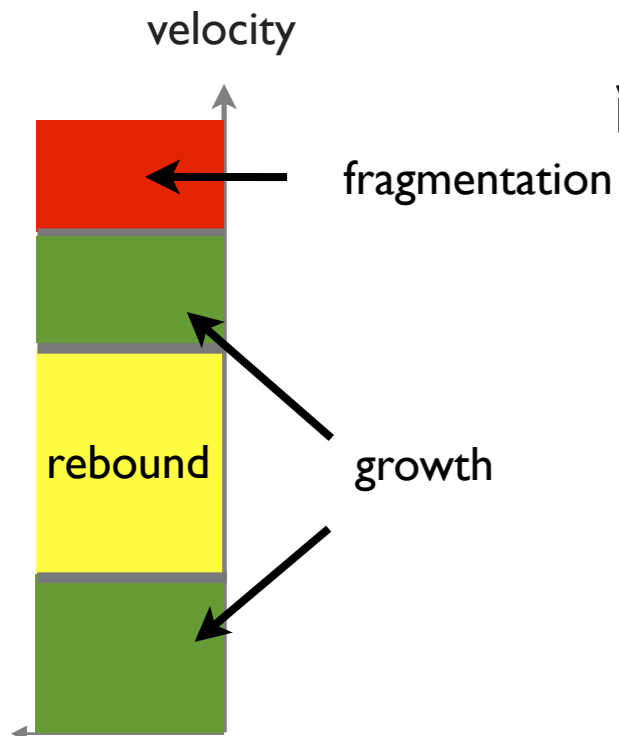
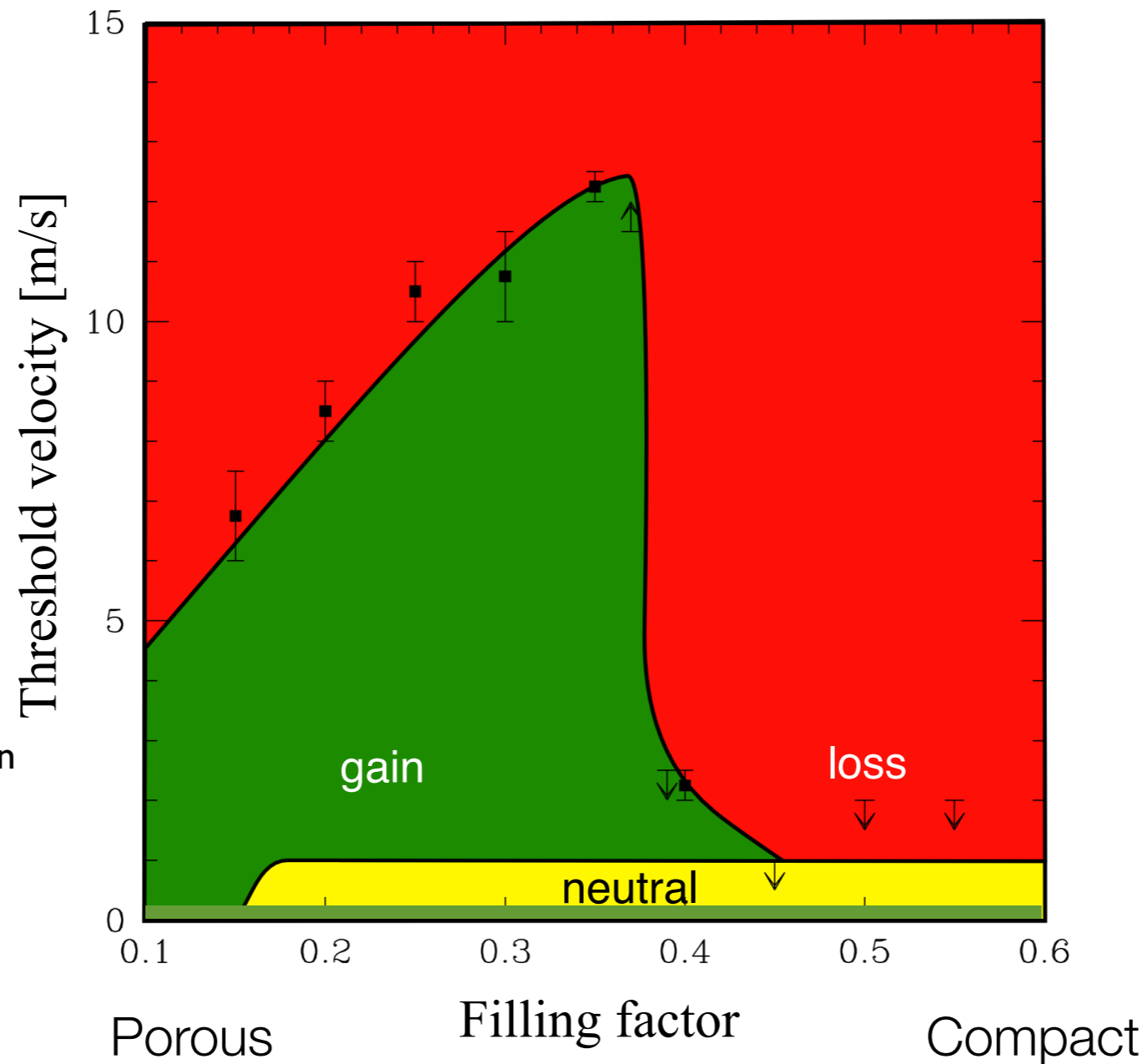
Porous aggregates become stronger with filling factor but compact aggregates break easily

Also combines results of
Beitz et al 2011,
Geretshauser, Meru et al
2011, Geretshauser et al
2012

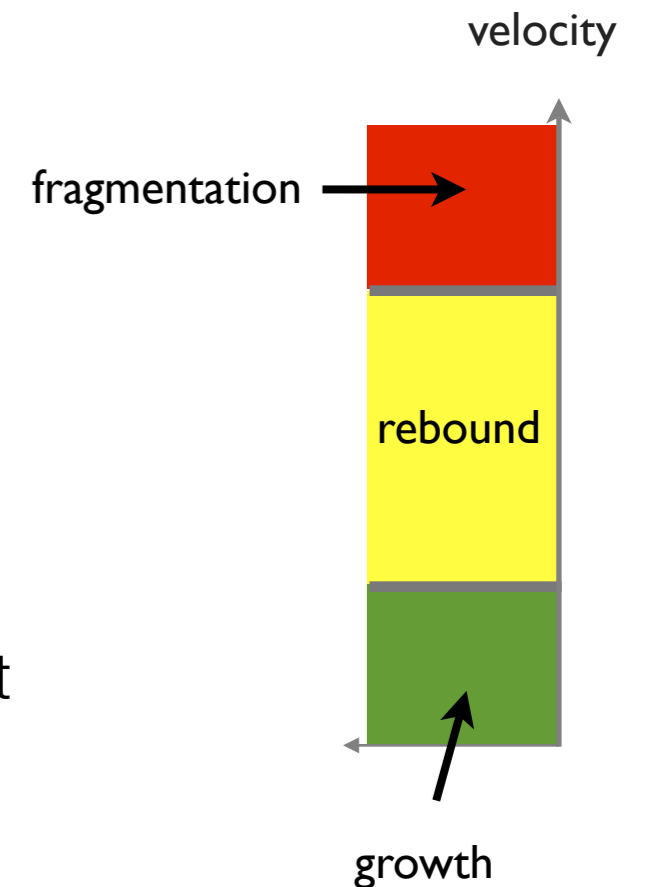


Porous aggregates become stronger with filling factor but compact aggregates break easily

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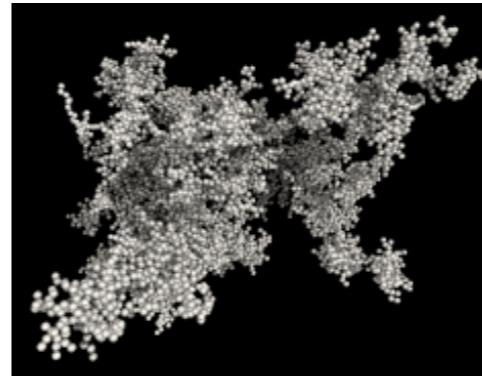
Meru et al 2013



There are different methods used to understand dust growth at small sizes

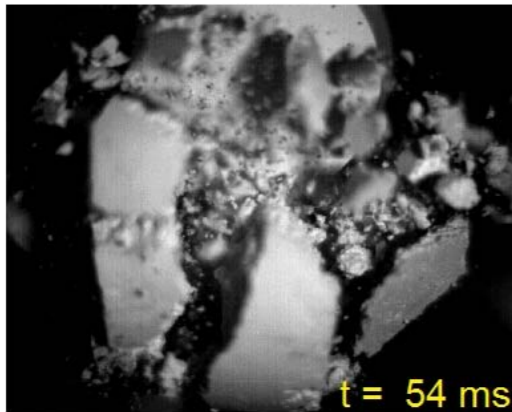
Scale

Molecular dynamics (particles)



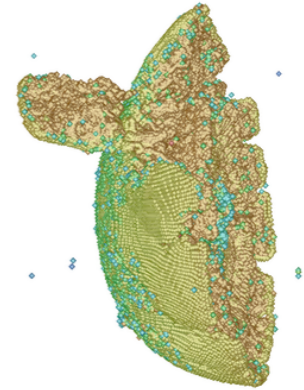
A. Seizinger

Laboratory experiments
($\sim 10 \mu\text{m} - 10 \text{cm}$)



Beitz et al 2011

SPH simulations (cm-dm)



Meru et al 2013

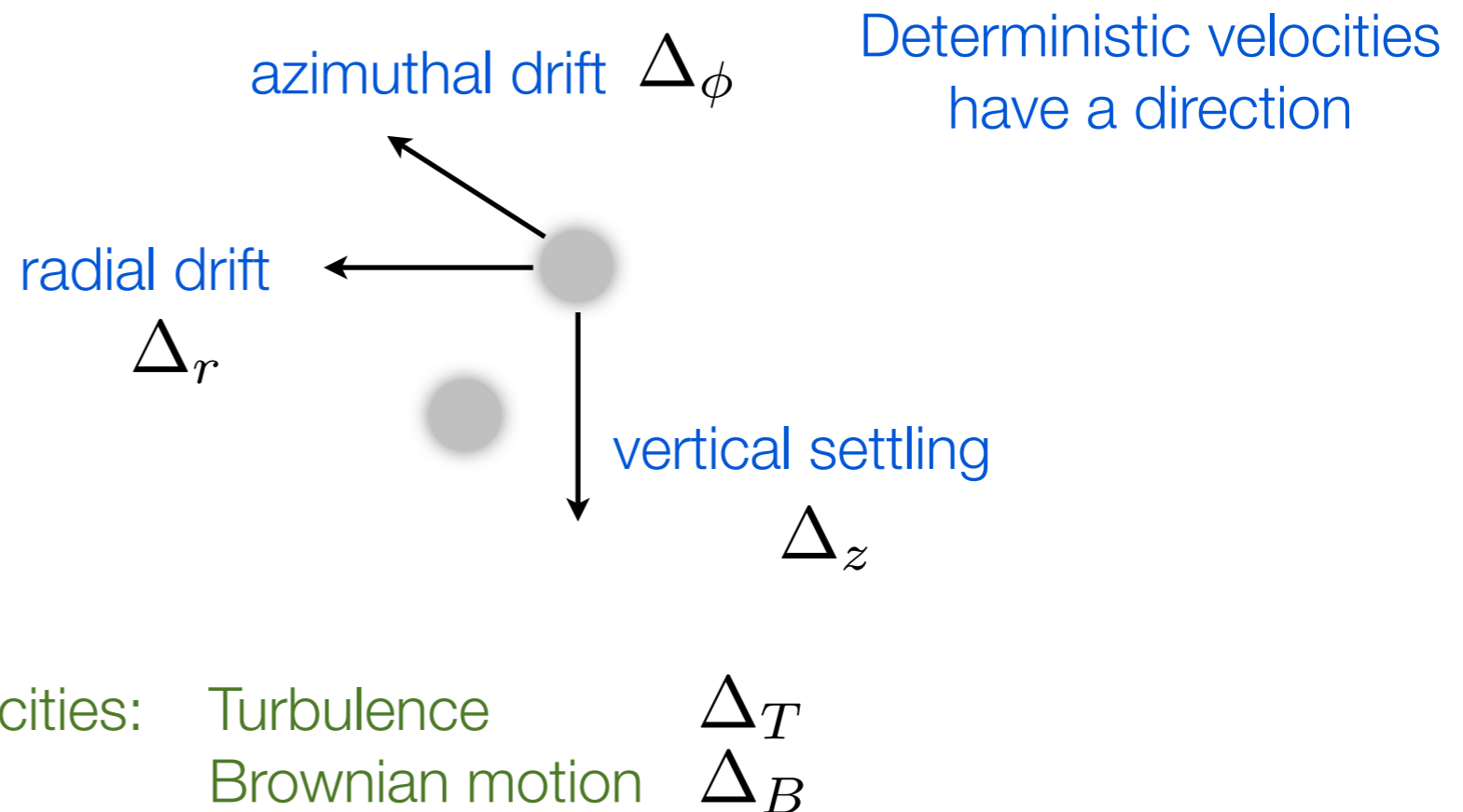
Monte Carlo
(considers background
disc)

**Smoluchowski equation
(considers background
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Gravity-dominated regime

The collision velocity was previously single-valued, determined by aggregate sizes and disc properties

Contributions to collision velocity:



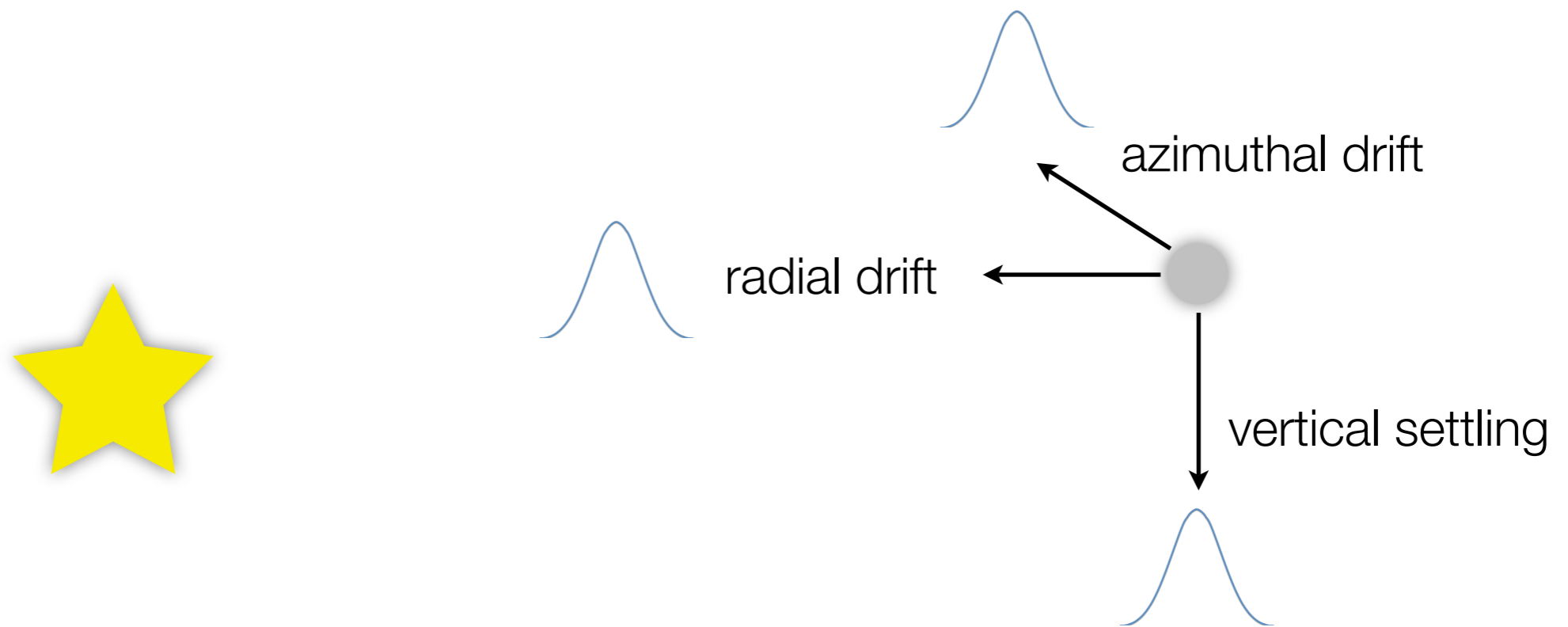
$$\text{Collision velocity} = \sqrt{\Delta_r^2 + \Delta_\phi^2 + \Delta_z^2 + \Delta_T^2 + \Delta_B^2}$$

Tanaka, Dullemond, Brauer et al 2007, 2008;
Birnstiel et al 2010; Zsom et al 2010

Two aggregates of particular sizes at a particular disc location will always collide at the same velocity. Realistic?

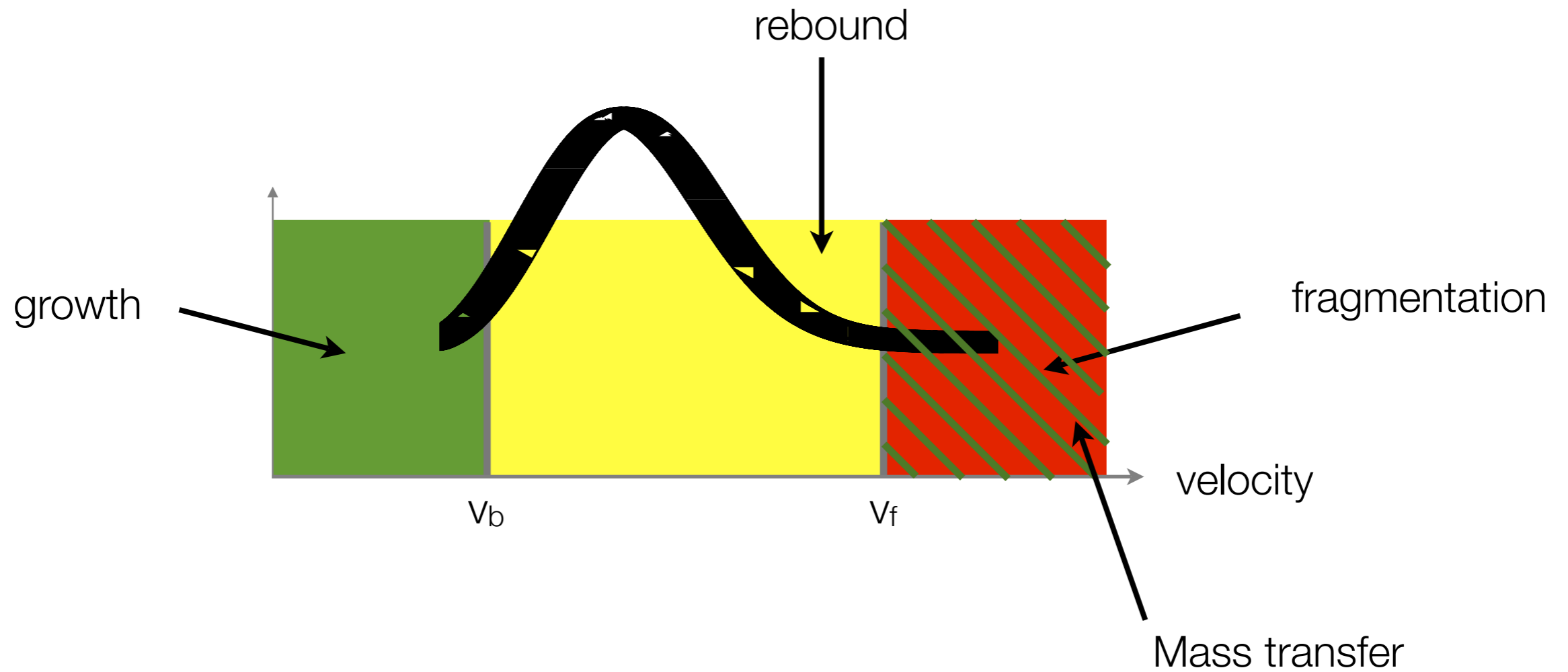
The new approach assumes each particle has a distribution of velocities

Peak given by deterministic velocity in each direction



Spread in each direction given by stochastic velocities
(turbulence & brownian motion)

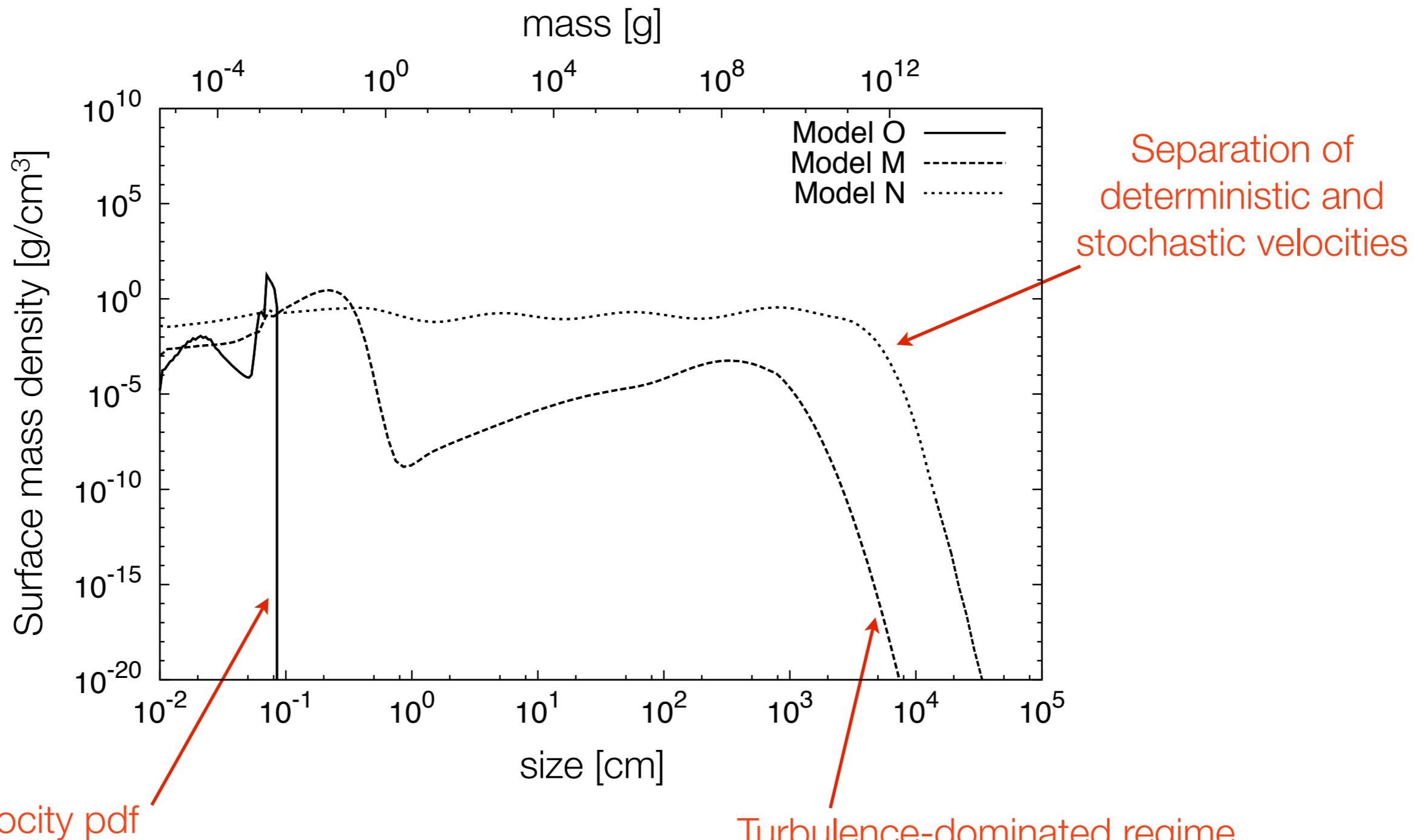
The end result is a distribution with non-zero sticking probability



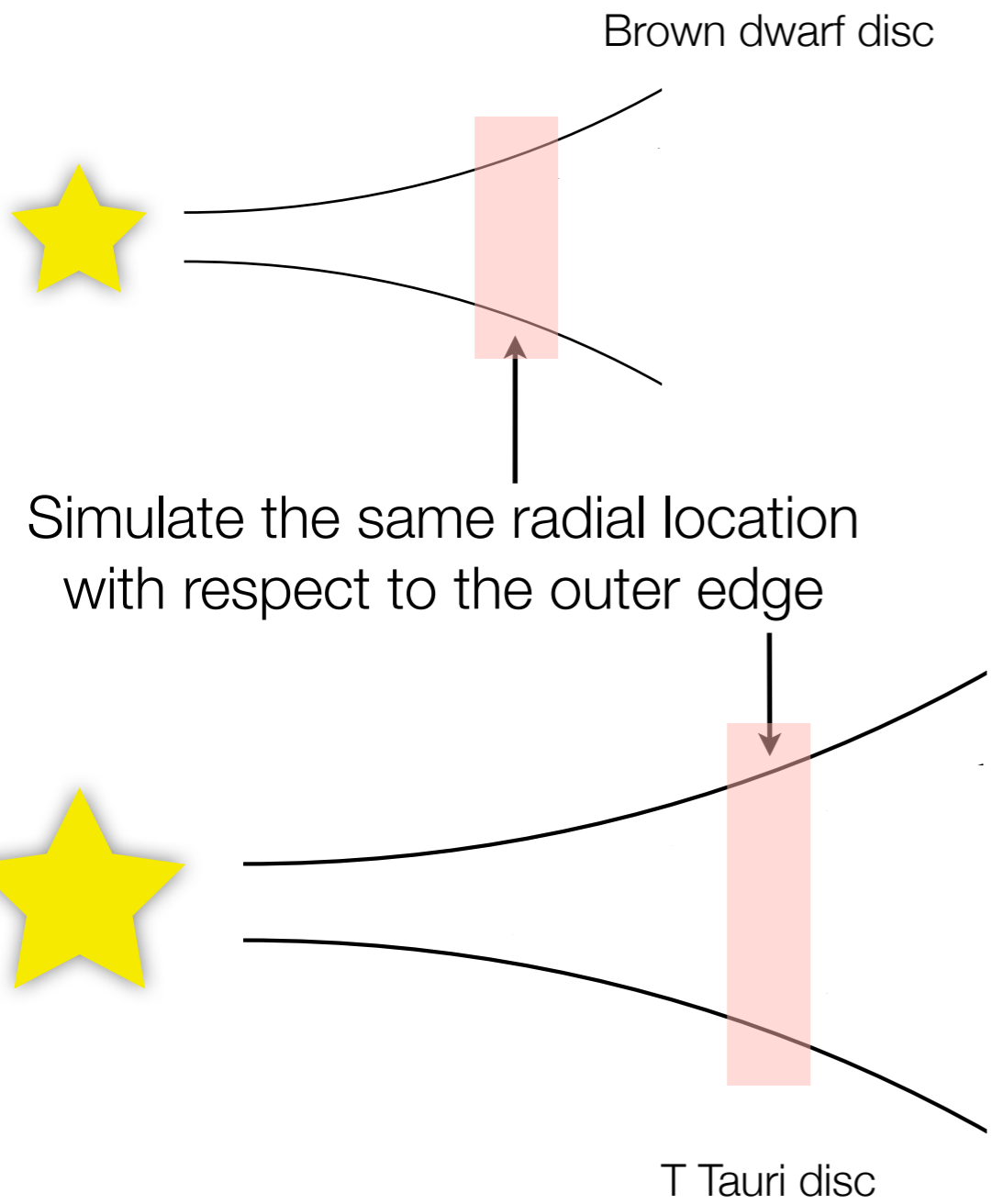
Teiser & Wurm 2009, Meru et al 2013

Growth achieved to larger sizes than before

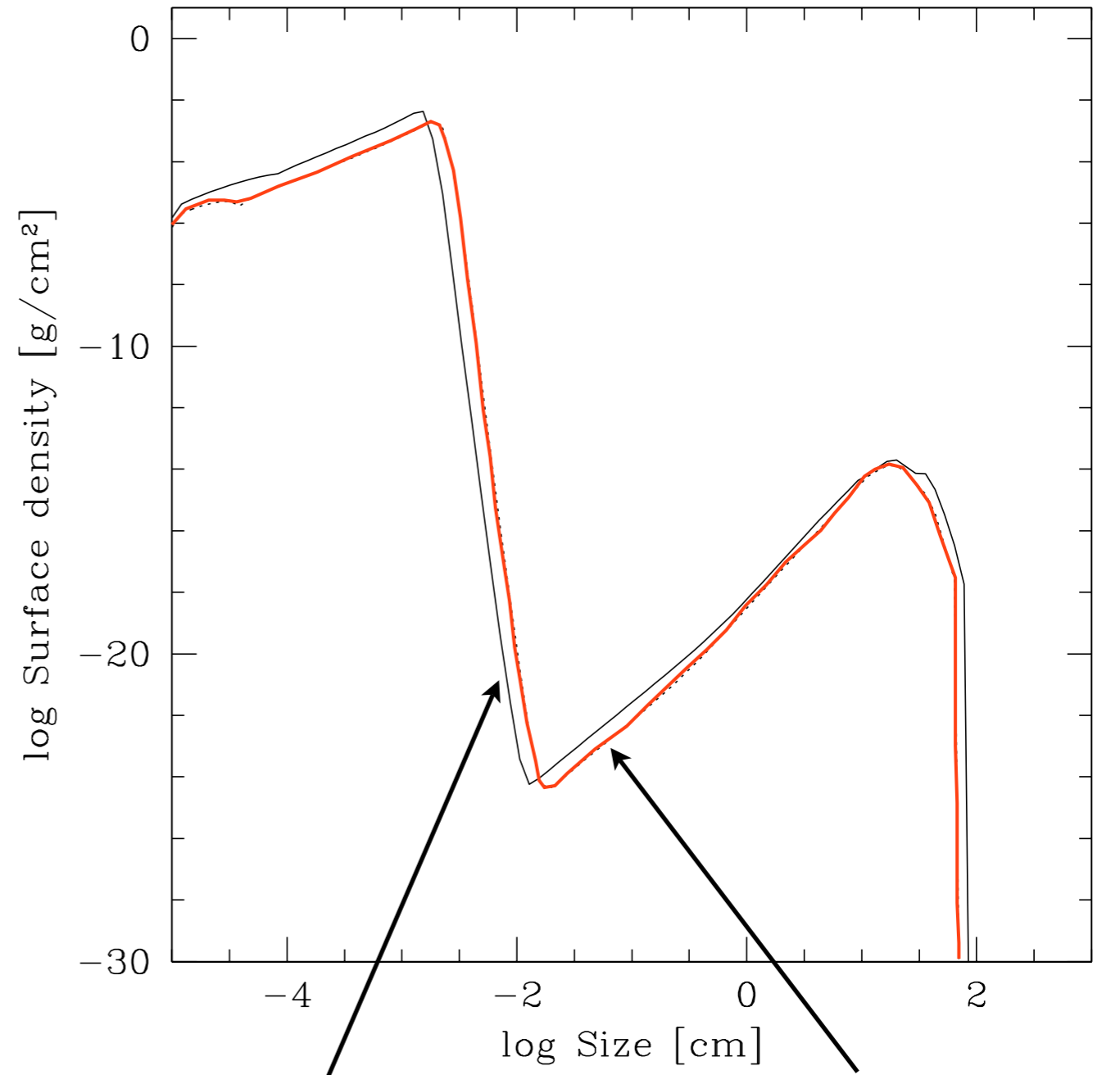
1 AU



Growth in brown dwarf and T Tauri discs occurs to the same maximum size



T Tauri disc is scaled-up
(disc mass, radius and stellar mass)



Gravitational instability

A fast cooling is also needed for fragmentation

Cooling needs to be faster than a critical value

Gammie 2001; Rice et al 2005; Meru & Bate 2011b,2012

$$t_{\text{cool}} < \frac{\beta_{\text{crit}}}{\Omega}$$

Fast cooling implies high turbulent stresses

Gammie 2001; Rice et al 2005

$$\alpha_{\text{GI}} = \frac{4}{9} \frac{1}{\gamma(\gamma - 1)} \frac{1}{\beta}$$

Turbulent stresses vary with radius

Clarke 2009

$$\alpha_{\text{GI}} = 0.4 \left(\frac{R}{100\text{AU}} \right)^{2/9}$$

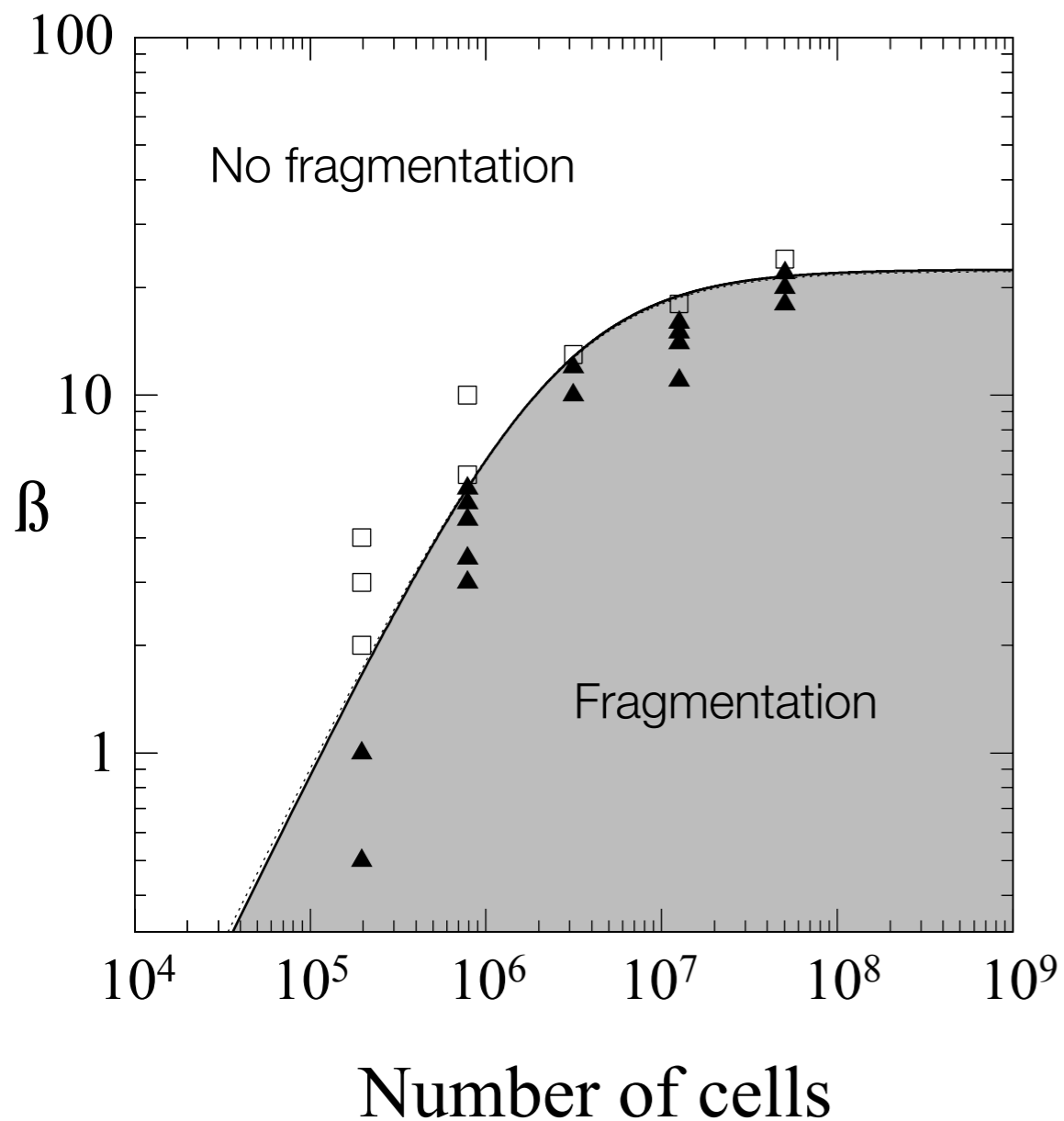
There is a critical radius outside of which fragmentation occurs

New results show fragmentation is easier than previously thought

Previous results:

$$\beta_{\text{crit}} \approx 6 - 7 \quad \text{for} \quad \gamma = \frac{5}{3}$$

Rice et al 2005



Meru & Bate 2012

β_{crit}	R_{crit} ($M_{\star} = 1M_{\odot}$)
6.5	66 au

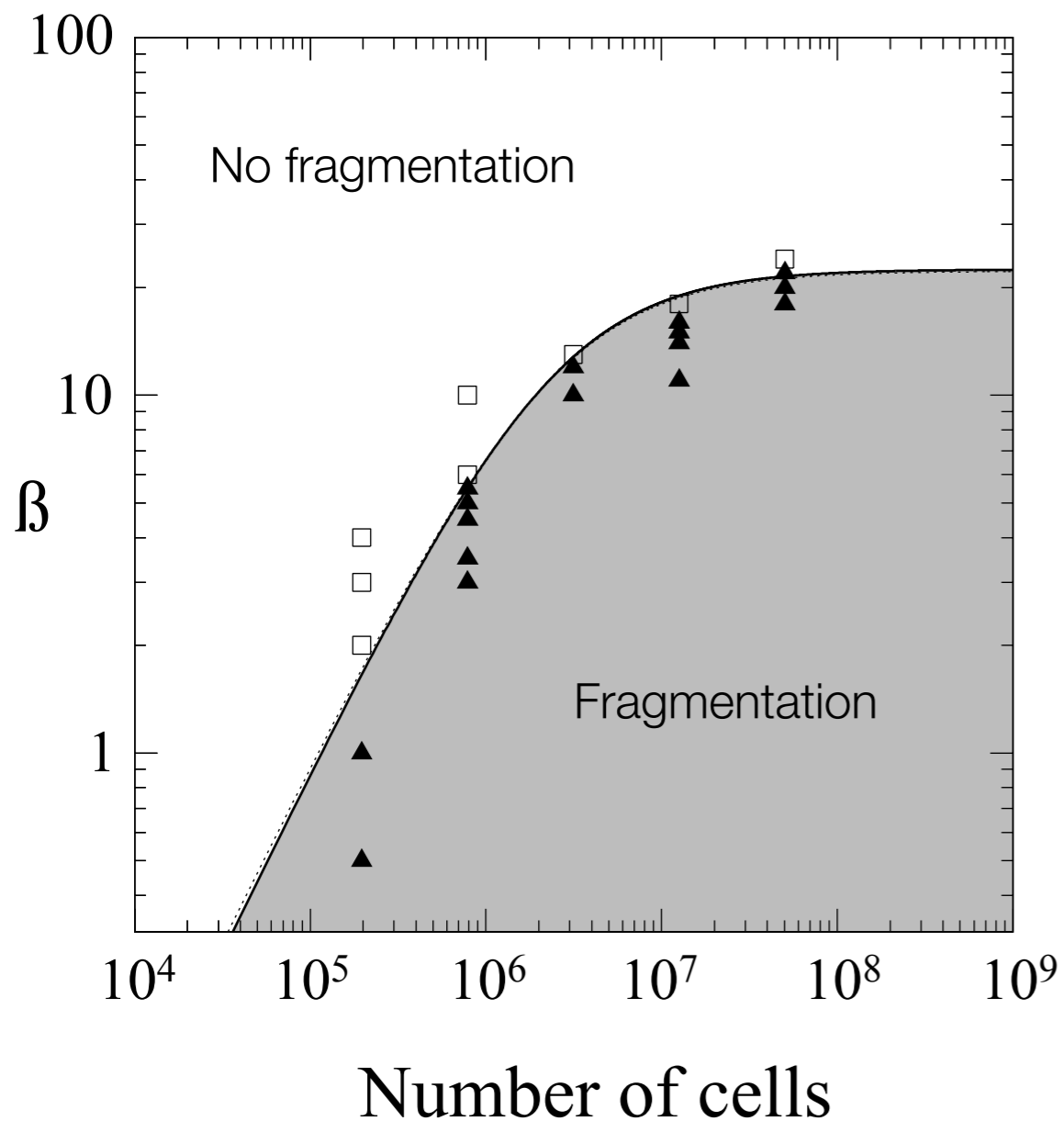


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Rice et al 2005



Meru & Bate 2012

β_{crit}	R_{crit} ($M_{\star} = 1M_{\odot}$)
6.5	66 au
20.0	51 au
30.0	47 au

Updated simulation results suggest $\beta_{\text{crit}} > 20$

Paardekooper 2012,
Meru & Bate 2012

The story isn't quite over yet

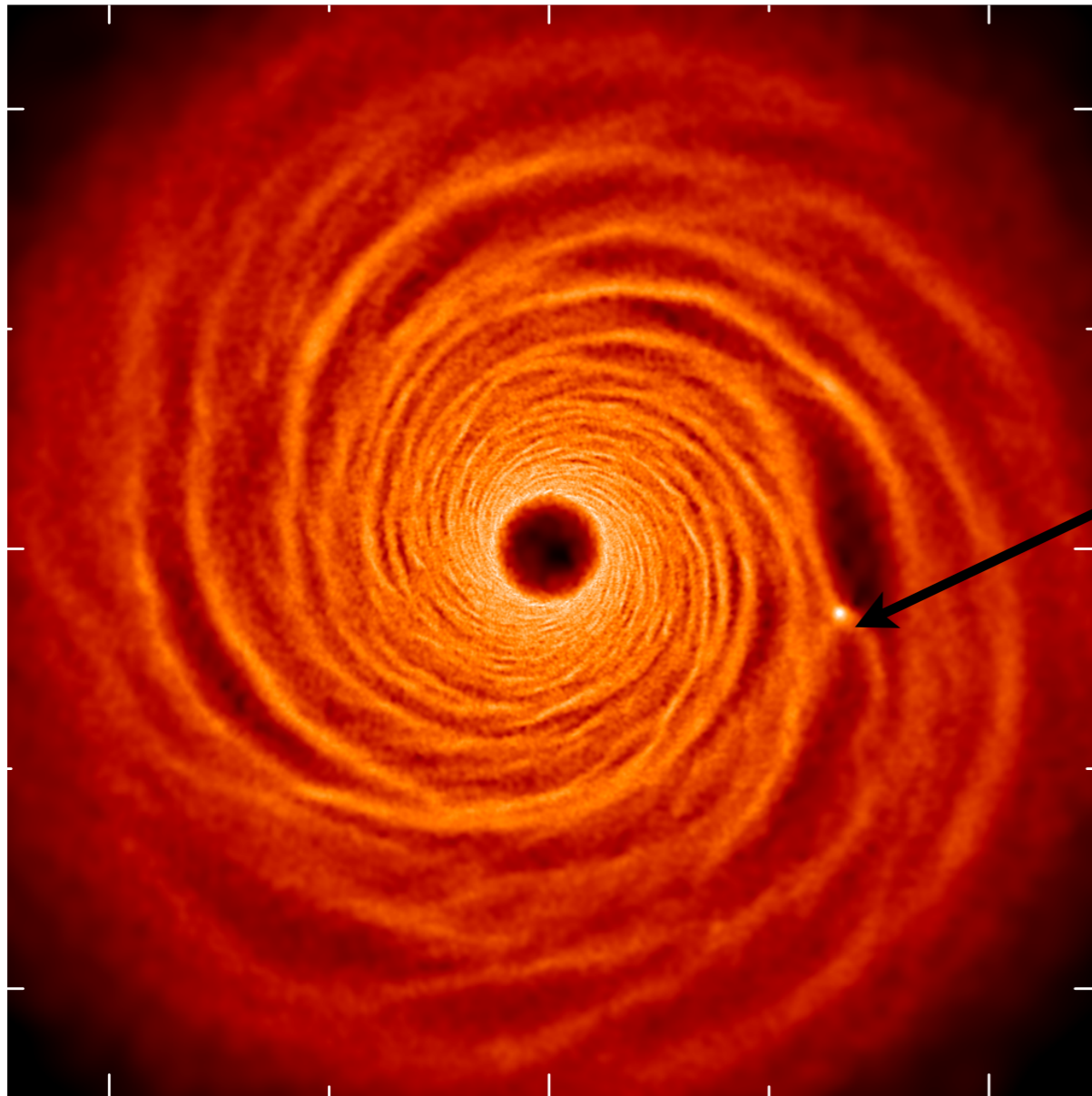
Stochastic fragmentation makes assessing when fragmentation occurs harder

Paardekooper 2012; Hopkins & Christiansen 2013

Different ways of modelling cooling can affect the results

Rice et al 2014

What happens in a gravitationally unstable disc after the first fragment forms?

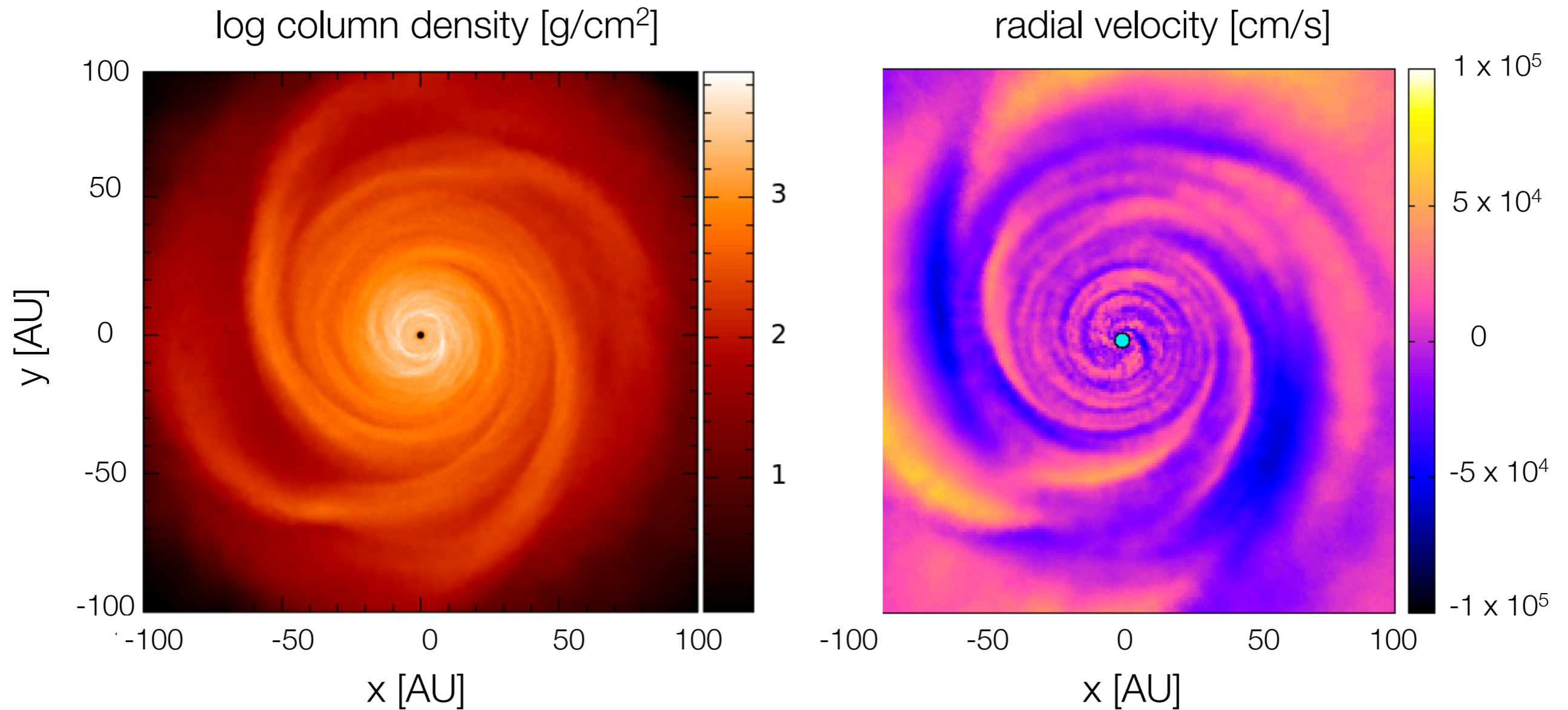


The fragment will have an effect on the surrounding disc material

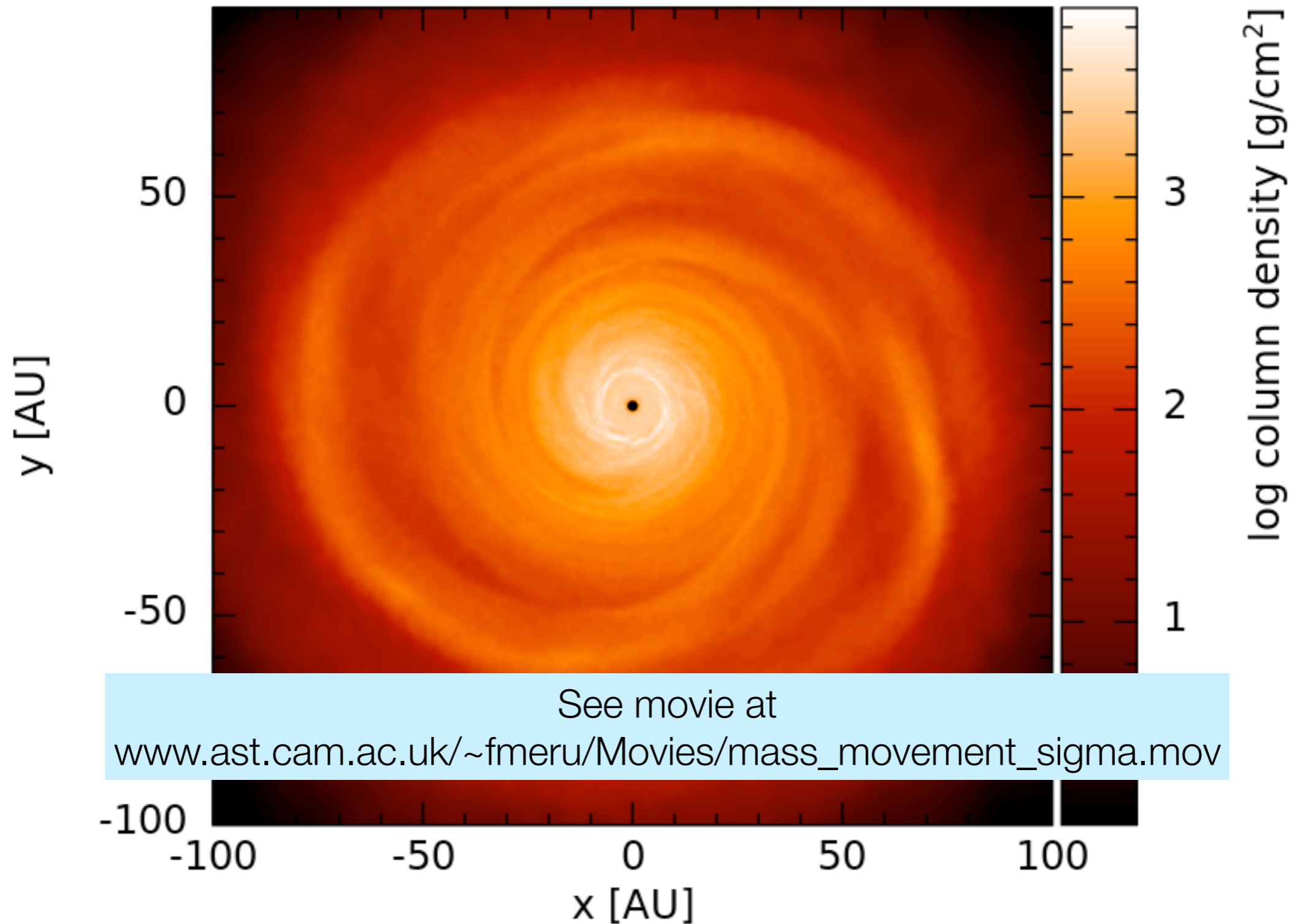
3D SPH simulations with radiative transfer

Self-consistent formation and evolution

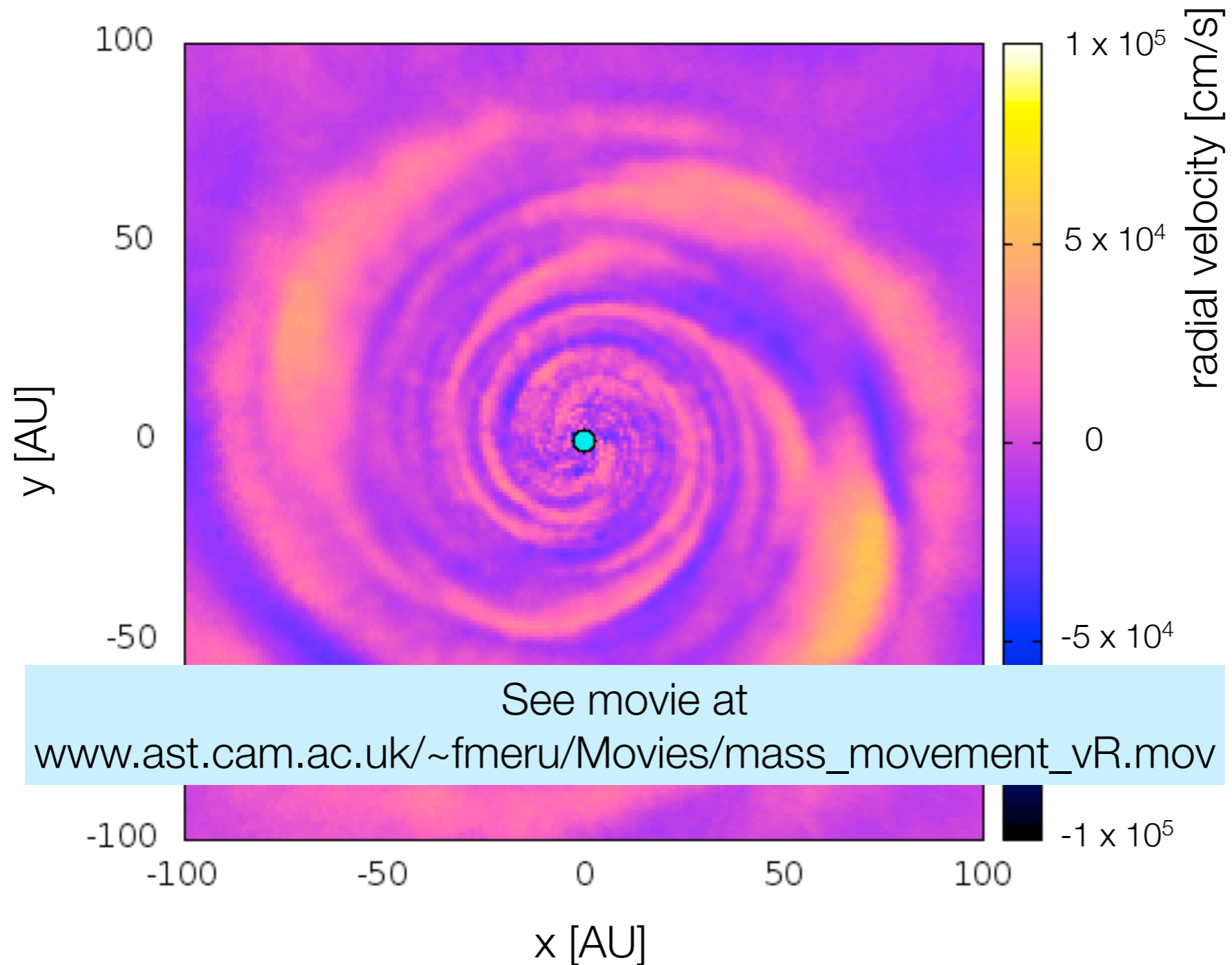
Before it fragments the disc is relatively calm



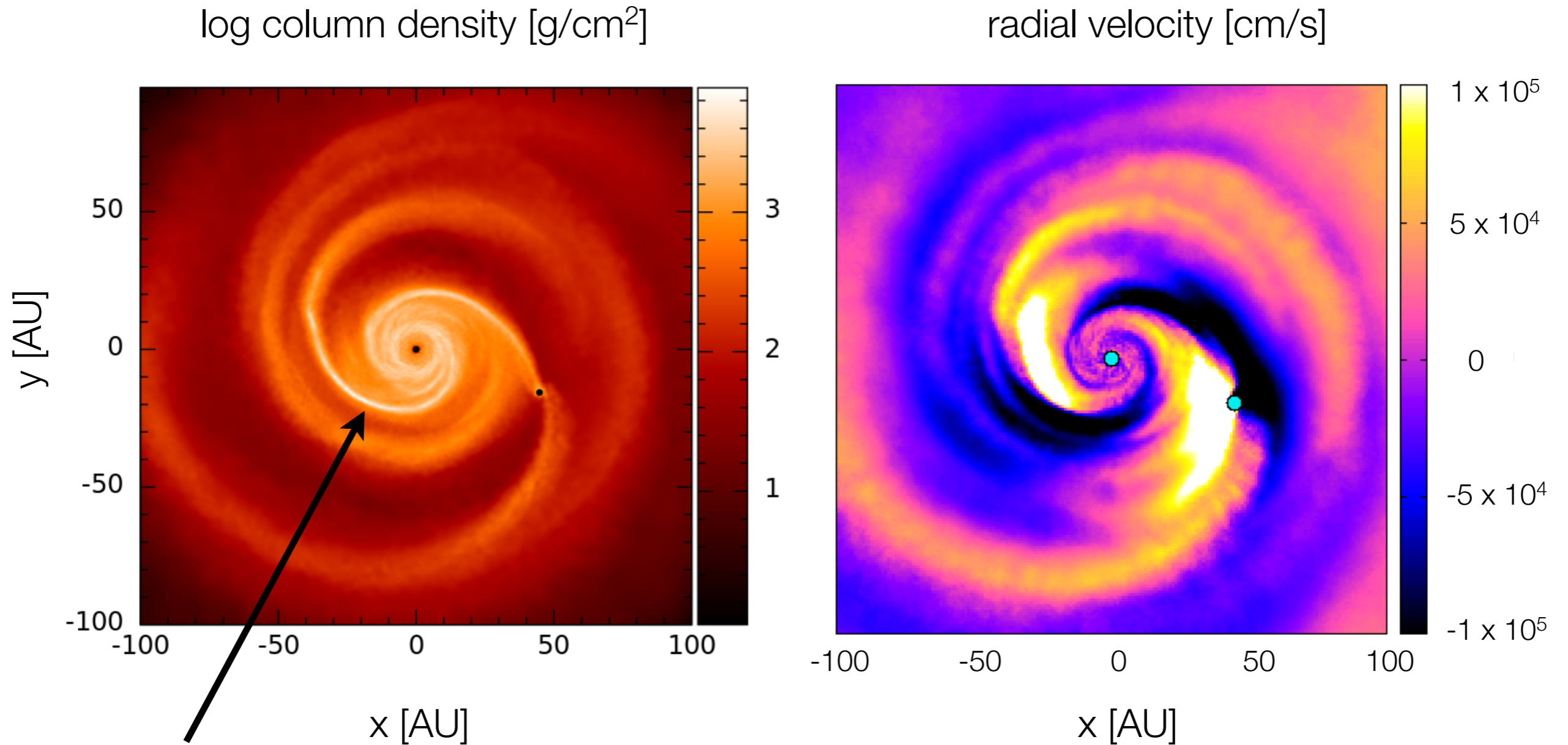
The disc fragments in the outer part
and then the inner parts



The inwards movement of gas triggers further fragmentation



The gas movement in the disc is more dynamic after fragmentation

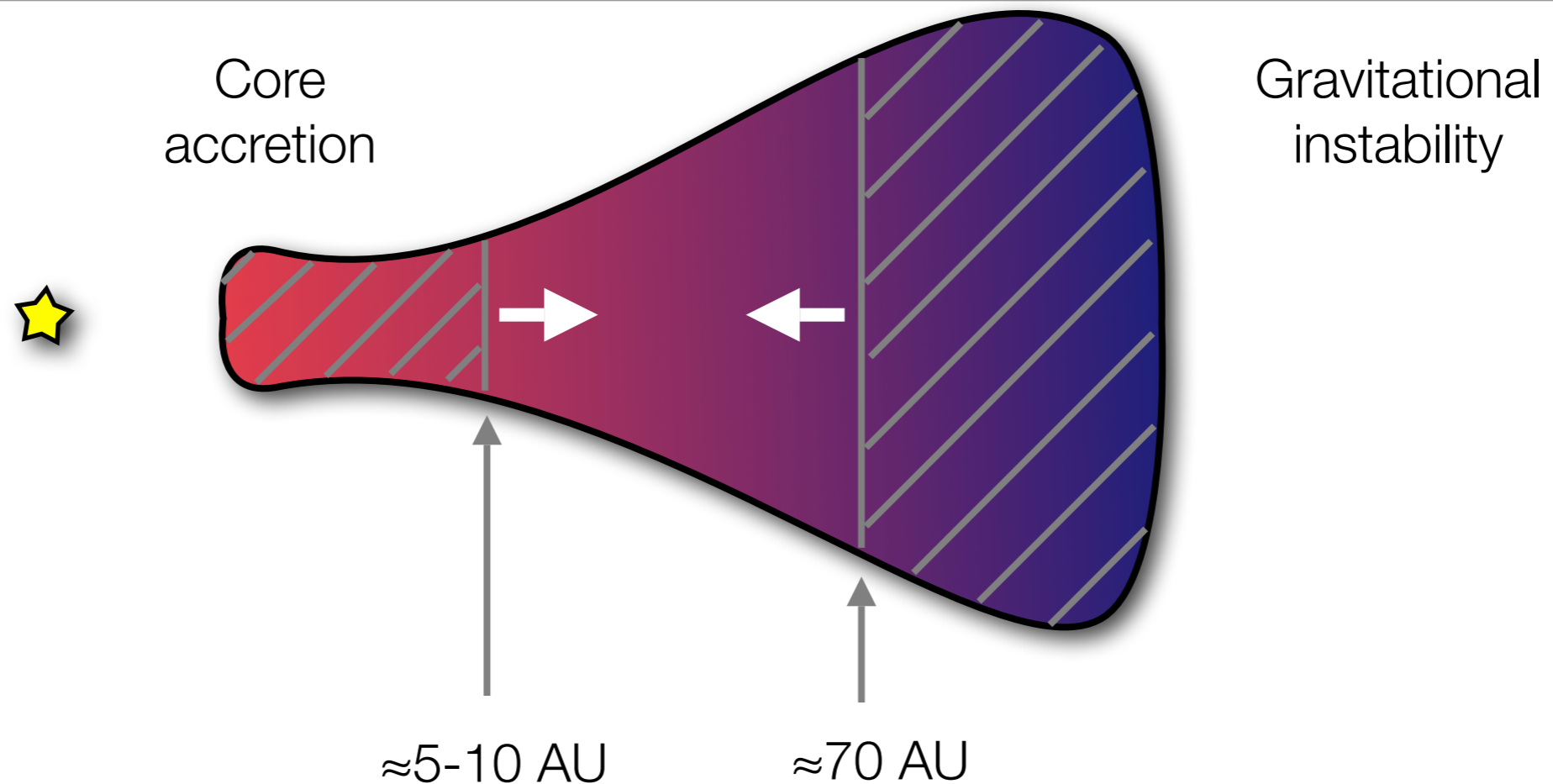


The inwards movement causes the inner spiral to become more dense, lowering the Toomre parameter and allowing further fragmentation

$$Q = \frac{c_s \kappa}{\pi \Sigma G}$$

Meru, in prep
See also Armitage &
Hansen 1999

Summary



1. Identified further areas of growth

Porous aggregates and collisions between high mass ratio aggregates help growth

2. Taking into account velocity distributions significantly helps early stage growth

1. Fragmentation is easier needing slower cooling than previously thought

2. Inwards movement of material due to a fragment can trigger further fragmentation at small radii